Name: $\qquad$
$\qquad$

School: $\qquad$
Date: $\qquad$

121/2
MATHEMATCCS
PAPER $20^{2} \partial^{2}$
JULY
TIME: $2.1 / 2$ HOURS

## MUMIAS DISTRICT JOINT EVALUATION EXAM

## Kenya Certificate of Secondary Education (K.C.S.E.)

## Mathematics

Paper 2

## INSTRUCTIONS TO CANDIDATES:

- Write your name ,index number, Signature and write date of examination in the spaces provided
- The paper contains two sections: Section I and Section II.
- Answer all the questions in section I and any five questions in section II.
- Answers and working must be written on the question paper in the spaces provided below each question.
- Marks may be given for correct working even if the answer is wrong.
- Non programmable silent electronic calculators and KNEC mathematical tables may be used.


## FOR EXAMINER'S USE ONLY

## SECTION 1

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| Question | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |

This paper consists of 12 printed pages. Candidates should check to ascertain that all papers are printed as indicated and that no questions are missing.

## SECTION I (50 MARKS)

## Answer all the questions in this section.

1. Simplify the expreşon $\sqrt{3}-\sqrt{2}$ giving your answer in the form of $\mathrm{a}+\mathrm{b} \sqrt{\mathrm{c}}$.
2. The diameter of circle has its ends with co-ordinates $A(6,10)$ and $B(0,2)$. Determine the equation of the circle giving your answer in the form of $x^{2}+y^{2}+a x+b y+c=0$.
3. Find the limits within which the area of a parallelogram whose base is 8 cm and height is 5 cm lies.

Hence find the relative error in the area.
(4mks)
4. Make $y$ the subject of the formula.

$$
\begin{equation*}
2 a=\sqrt{\underline{b-2 a}+b} \tag{3mks}
\end{equation*}
$$

$$
\delta^{\circ}
$$

5. Given that the matrix $\left(\begin{array}{ll}4 & \mathrm{k}-6 \\ 8 & 6\end{array}\right)$ is a singular matrix, find the value of $k$.
(2mks)
6. In the circle below, two chords PQ and RS intersect externally at T. Find the length of TS if QT=3cm and $\mathrm{RS}=5 \mathrm{~cm}$ and $\mathrm{PQ}=9 \mathrm{~cm}$.

7. Expand $\left(\mathrm{x}^{-1} / 2 \mathrm{x}\right)^{6}$ upto the fourth term and state its constant term, hence use the first four terms to solve (9.95) to (4 s.f)
8. State the nature of the turning points of the curve.
$y=x^{3}+6 x^{2}-15 x+24$
9. Town X is east of town Y where town Y is $\left(15^{\circ} \mathrm{N}, 3^{\circ} \mathrm{W}\right)$. The local time at X is 2.00 pm when the local time at $Y$ is 4.00 pm . Find the position of town $X$.

Solve for $\theta$ for $-90 \leq \theta \leq 180$ o in the equation $3 \sin ^{2} \theta-1=2 \sin \theta$.
(3mks)
12. The probability that a healthy animal being brought into contact with an infecting agent and gets the germ is 0.80 . The probability that an animal infected with germs develops the disease is 0.90 . The probability that an animal which has developed the disease will survive is 0.75 . What is the probability that a healthy animal brought into contact with the infecting agent will die?
13. $\mathrm{OA}=3 \mathrm{i}+4 \mathrm{j}-6 \mathrm{k}$ and $\mathrm{OB}=2 \mathrm{i}+3 \mathrm{j}+\mathrm{AK}$. P divides a line AB in the ratio $3:-2$. Write down the co-ordinates of P.
14. Evaluate using logarithms.
$\sqrt{\frac{\operatorname{Tan} 80^{\circ}}{76.8 \times 0.7034}}$
15. A contractor employs 40 men to do a piece of work in 60 days each man working 9 hours a day. He is then requested to do the job in 48 days. How many more men working 10 hours a day does he need to employ.
16. Find the number of terms in the series


Answer only five questions in this section.
17. In the figure below GO is the centre of the circle and PTQ is the tangent at T . If $\mathrm{PT}=\mathrm{ST}$ and angle $\mathrm{SRT}=52^{\circ}$. Determine the size of the angles below giving reasons:

(a) PTS
(b) RTQ
(c) TSR
(d) TQR
(e) PSQ
18. A transporter wishes to transfer 1000 bags of sugar to a go-down. He has two types of lorries to use, FTR with capacity of 80 Bags and a canter with the capacity 20bags. The canter has to make at most
 than 30, and the canter has to make more than 10 trip.
(a) Write
(Take trips milade by FTR be x and trips made by canter be y )
(b) Represent the information above on the graph provided.
(c) If the FTR uses Ksh. 1800 worth of fuel per trip, estimate the maximum amount that can be spent on fueling the lorries.
19. Three hundred and sixty litres of a homogeneous paint is made by mixing three paints $\mathrm{A}, \mathrm{B}$, and C . The ratio by volume of paint $A$ to paint $B$ is $3: 2$ and paint $B$ to paint $C$ is 1:2. Paint A costs sh. 180 per litre, paint $B$ sh, 240 per litrre and paint $C$ sh. 127.50 per litre. Determine:
(a) The volume of each type of paint in the mixture.
(b) The amount of money spent in making one litre of the mixture.
(c) The percentage profit made by selling the mixture at sh. 221 per litre.
20. (a) Complete the table below giving your values correct to 2 decimal places.

|  | $15^{\circ}$ | $30^{\circ}$ | $45^{\circ}$ | $60^{\circ}$ | $75^{\circ}$ | $90^{\circ}$ | $105^{\circ}$ | $120^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3 \cos x^{\circ}$ |  | 2.60 |  | 1.50 | 0.78 | 0 | -0.75 |  |
| $4 \sin (2 x-10)^{0} x^{2}-0.69$ | 1.37 |  | 3.94 | 3.76 |  | 0.69 |  | -3.00 |

(b) Taking 1 cra to represent $15^{\circ}$ on the x -axis and 2 cm to represent 1 unit on the y-axis. Draw the graphsof $\frac{y}{}{ }^{3} 3$ Cos $x$ and $y=4 \operatorname{Sin}(2 x-10)$ on the same set of axes on the grid provided.

(c) Use your graph to find the values of $x$ for which $3 \cos x-4 \sin \left(2 x-10^{\circ}\right)=0$
(d) State (i) the amplitude of the graph $y=3 \operatorname{Cos} x$.
(ii) the period of the graph $y=4 \sin \left(2 x-10^{\circ}\right)$
21. The table below shows marks Obtained by students in a mathematics mock paper.

| Marks | $5^{1 \mathscr{O}^{2}-14}$ | 15-19 | 20-24 | 25-29 | 30-34 | 35-39 | 40-44 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No of students | 8 | 12 | 18 | 20 | 15 | 4 | 3 |

(a) Calculate the median mark.
(b) On the grid provided draw an ogive and estimate the:

(i) Semi-inter quartile range
(ii) $8^{\text {th }}$ decile
22. The figure below is a square pyramid ABCDV with $\mathrm{AD}=\mathrm{DC}=6 \mathrm{~cm}$, and height $\mathrm{VO}=10 \mathrm{~cm}$.

(a) State the projection of VA on the base ABCD .
(b) Find:
(i) The length of VA
(ii) The angle between VA and ABCD
(iii) The angle between VDC and ABCD.
(iv) Volume of the pyramid.
23. A particle $P$ moves in a straight line so that its velocity, $\mathrm{Vm} / \mathrm{s}$ at time t seconds where $\mathrm{t} \geq 0$ is given by $\mathrm{V}=28+\mathrm{t}-2 \mathrm{t}^{2}$.

Find;

(a) The time when $P$ is instantaneously at rest.
(b) The speed of P at the instant when the acceleration of P is zero.
(c) Given that P passes through the point O of the line when $\mathrm{t}=0$.
(i) Find the distance of P from O when P is instantaneously at rest
(ii) Find the distance covered by the particle during the $3^{\text {rd }}$ second.
24. The two variable P and Q are eonnected by $\mathrm{Q}=\mathrm{K}\left(\mathrm{a}^{\mathrm{p}}\right)$ and the table of values of P and Q is given below.

(a)
(1mk)
(b) Draw the linear graph.
(5mks)

(c) Find the value of a and k .
(3mks)
(d) Write the equation connecting Q and p .

