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School: $\qquad$
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Date: $\qquad$

121/2
MATHEMATGCS
PAPER $2{ }^{j} \partial^{2}$
JULY / AUGUST 2011
TIMES2. ${ }^{1}$ HOURS
SOTIK DISTRICT JOINT EVALUATION TEST

## Kenya Certificate of Secondary Education (K.C.S.E)

## Mathematics

Paper 2

## INSTRUCTIONS TO CANDIDATES:

- Write your name and index number in the spaces provided above.
- Sign and write the date in the space provided above.
- This paper contains two sections: Section I and Section II.
- Answer all the questions in Section 1 and any five questions from Section II.
- All working and answers must be written on the question paper in the spaces provided below each question.
- Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.
- Marks may be given for correct working even if the answer is wrong.
- Non-programmable silent electronic calculators and KNEC mathematical tables may be used


## For Examiners' Use Only.

Section I

| Questions | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Section II

| Questions | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |

GRAND
TOTAL
$\square$

This paper consists of 16 printed pages. Candidates should check to ascertain that all pages are printed as indicated and that no questions are missing

1. Use logarithms in all steps to evaluate:
$\frac{2.53^{2} \mathrm{X} 83.45}{\sqrt{0.4562}}$
$a^{2}$
2. Evaluate:
$\frac{1 / 2 \text { of } 31 / 2+11 / 2(21 / 2-2 / 3)}{3 / 2}$
$3 / 4$ of $21 / 2 \div 1 / 2$
3. The table below is part of tax table for monthly income for the year 2010.

Monthly taxable income in Ksh.
Under Ksh. 9681
From Ksh. 9681 but under 18801
Tax rate $\%$ in each sh.

From Ksh. 18801 but under Kshs. 27921
10\%
20\%
In the year 2010, the tax on Koech's monthly income was Ksh.1916. Calculate Koech's monthly income.
4. (a) Expand and simplify the expression

(b) Use the expression in (a) above to find the value of $14^{5}$.
5. Make C the subject of the formula.
$\mathrm{T}=\mathrm{x} \sqrt{\mathrm{c}^{2}+\mathrm{d}^{2}}$
6. A variable $\mathbf{P}$ varies as the square of $\mathbf{Q}$ and inversely as square root of $\mathbf{R}$. Find the percentage change in $\mathbf{P}$ when $\mathbf{Q}$ is increased by $5 \%$ and R reduced by $19 \%$.
7. The distance between Sotik and Nakuru is 130 km . car x starts from Sotik at 8.00 a.m and travels at $40 \mathrm{~km} / \mathrm{hr}$ towards Nakuru, $\mathrm{q}^{\circ}$ second car y starts traveling from Nakuru at 8.15 a.m towards Sotik at an average speed of $35 \mathrm{~km} / \mathrm{hr}$. At what time will the two cars meet?

Use matrix method to solve simultaneous equations.
$3 x+7 y=11$
$x-y+4=0$
9. PQRS is a cyclic quadrilateral in which $\mathrm{PQ}=6 \mathrm{~cm}, \mathrm{QR}=2 \mathrm{~cm}, \mathrm{RS}=6.5 \mathrm{~cm}, \mathrm{PR}=7.2 \mathrm{~cm}$ and angle PRS $=70^{\circ}$.


Determine values of x .
10. In the figure below, AB is a tangent, meeting chord CDE at $\mathrm{B} . \mathrm{DE}=\mathrm{xcm}$.


NDetermine:
(a) the value of x
(b) the length of AB
11. Without using mathetical tables and calculators simplify:

$$
\begin{equation*}
\frac{2}{3-\sqrt{7}}-\frac{2}{3+\sqrt{7}} \tag{3mks}
\end{equation*}
$$

12. Find the values of $\theta$ in $2 \sin 3 \theta=-1.0893$ for $0^{\circ} \leq \theta \leq 180^{\circ}$
13. Find the equation of the tangeht to the circle $x^{2}+y^{2}-8 x+2 y+7=0$ at the point (3,2). Give your answer in the form $y=a x+b$.

Aman accumulated sh. 71,105 after investing sh. 50,000 at a rate of $18 \%$ p.a. Compounded quarterly. Find the time taken in years to accumulate this amount.
15. The masses of 100 objects measured to the nearest kg are given in the following table. Draw a histogram to illustrate the data.

| Mass (kg) | $1-5$ | $6-10$ | $11-20$ | $21-25$ | $26-$ <br> 40 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. f objects | 7 | 16 | 38 | 33 | 6 |

16. Draw an equilateral triangle of siok 80 m to represent Mr. Laal's farm. Laal wants to plant some flowers in the field. The flowers must $b \mathrm{~b}$ at most 60 m from $A$ and nearer to $B$ than to $C$. If no flower is to be more than 40 m from BC , show by shading the exact region where the flowers may be planted. ( 4 mks )


## SECTION B (50 MARKS)

 Answer any five questions in this section in the spaces provided.17. The $n^{\text {th }}$ term of a seeffes is given by $3 n+4$.
(a) Write down the first four terms of the series.
(b) Find the sum of the first twenty terms of the series.
(c) Find the $30^{\text {th }}$ term.
(d) Show that the sum of the first $n$ terms of the sequence is given by $S_{n}=3 / 2 n^{2}+11 / 2 n$. Hence or otherwise, find the largest integral value of $n$ such that $S_{n} \geq 130$.
18. In a square PQRS, $A$ is the miond-point of $\overrightarrow{P Q}$ and $B$ is the mid-point of $\overrightarrow{Q R}$, while $C$ is a point on $\overrightarrow{B P}$ such that $\overrightarrow{2 \mathrm{BC}}=\overrightarrow{3 \mathrm{CP}}$. The co-ordinates of $\mathrm{P}, \mathrm{Q}$ and S are $(4,4),(14,4)$ and $(4,14)$ respectively. Find:

(ii) co-ordinates of R
(b) Show that A, C, S are collinear.
19. The points X and Y are both om latitude $39^{\circ} \mathrm{N}$. The longitude of X is $73^{\circ} \mathrm{W}$ and the longitude of Y is $18^{\circ} \mathrm{W}$. Two ships P and Qseave X at the same time and travel to Y along the line of latitude. The ships $P$ and $Q$ travel at constant speeds of $25 \mathrm{~km} / \mathrm{hr}$ and $20 \mathrm{~km} / \mathrm{h}$ respectively. Taking the radius of the earth to be $6371 \mathrm{~km}_{2}^{2}$ add $^{2} \pi=\frac{22}{7}$;Calculate:-

## (a) The distange Q still has to travel when P reaches Y .

## $Q_{0}^{2} 0^{0}$

(b) At the same time a third ship R leaves Y traveling due west at an average speed of $15 \mathrm{~km} / \mathrm{hr}$. Calculate the longitude of the point at which R meets P .
20. A supermarket is stocked with plates which come from two suppliers A and B. They are bought in the ratio of $3: 5$ respectivels, $10 \%$ of plates from $A$ are defective and $6 \%$ of the plates from $B$ are defective.
(a) A plate is chosen $\begin{array}{r}\text { y } \\ \text { a }\end{array}$
(i) it is from A
(ii) it is from B and it is defective.
(iii) it is defective
(b) Two plates are chosen at random. Find the probability that: (i) both are defective
(ii) at least one is not defective.
21. (a) Copy and complete the table below for the function $y=4+5 x-x^{2}$ for $-2 \leq x \leq 7$.

| x | -2 s | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | ${ }^{4}$ |  |  |  |  |  |  |  |  |  |  |

(b) Draw the geaph of the function $y=4+5 x-x^{2}$ for $-2 \leq x \leq 7$, in the grid provided. (3mks)

(c) Use your graph to solve
(i) $x^{2}=+3 x-4$

"
(1)

(ii) $x^{2} s^{2} 4=5 x$
(d) Write down the equation of the line of symmetry.
(e) State the co-ordinates of the maxima point of the graph $y=4+5 x-x^{2}$.
22. A company wishes to buy two types of squash packing machines; electric and manual. A manual machine requires 4 attendarits whereas an electric one requires 2 . An electric machine fills 300 packets per hour; a maqual one can fill 200 packets per hour. At least 3,000 packets need to be filled per hour and the nunfber of attendants should not exceed 40.
(a) Write down in qualities to describe these conditions and graph them.
(b) If for every hour it is used, an electric machine brings a profit of sh. 200 and a manual one sh. 500 , determine the number of machines of each type that should be installed in order to maximize profit per hour.
(c) Find the maximum profit.
23. Matrix $P$ is given by
a) Find $\mathrm{P}^{-1}$
b) Two instifititions, Masomo High School and Tumaini High School, purchased beans at sh. b per bag and made at sh. m per bag. Masomo purchased 8 bags of beans and 14 bags of maize for sh. 47,600. Tưnåini purchased 10 bas of beans and 16 bags of maize for sh. 57,400.
(Ci) Form matrix equation to represent the information above
ii) Use the matrix $\mathrm{P}^{-1}$ to find the prices of one bag of each item.
c) The price of beans later went up by $5 \%$ and that of maize remained constant. Masomo bought the same quantity of beans but spent the same total amount of money as before on the two items. State the new ratio of beans of maize.
(3mks)
24. In a certain mathematical relationship, the values of $A$ and $B$ are found to obey the relationship $B=C A+K A^{2}$ where $C$ and ${ }^{2}$ are constants.
Below is a table of values of A and B.

| A | 1 | $22^{2}$ | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | 3.2 | 6.75 | 10.8 | 15.1 | 20 | 25.2 |

(a) Bycorraiving a suitable straight line graph, determine the values of C and K . ( 8 mks )

(b) Hence write the relationship between A and B.
(1mk)
(c) Determine the value of B when $\mathrm{A}=7$

