Name $\qquad$
$\qquad$ Class $\qquad$
121/1
MATHEMATICS
PAPER 1
JUNE/ JULY 2013
TIME: $\mathbf{2}^{1 / 2} \mathbf{H R S}$

## LENOCET EVALUATION TEST KENYA CERTIFICATE OF SECONDARY EDUCATION

## MATHEMATICS

## PAPER 1

TIME: $\mathbf{2}^{1}{ }_{2} \mathbf{H R S}$

## Instructions to candidates

(a) Write your Name and Index number in the spaces provided above.
(b) This paper consists of TWO sections: section I and section II.
(c) Answer ALL questions in section I and only five questions from section II.
(d) All answers and working must be written on the question paper in the spaces provided below each question.
(e) Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.
(f) Marks may be given for correct working even if the answer is wrong.
(g) Non-programmable silent electronic calculators and KNEC mathematical tables may be used except where stated otherwise.
(i) This paper consists of 19 printed pages.
(j) Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.

## For Examiner's use only

## Section I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Section II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

$\underset{\text { GRAND }}{\text { GRAL }} \square$

## SECTION 150 MARKS

## Answer all questighs in this section in the spaces provided

1. Evaluate without using a calculator $e^{e^{2+}}$

$$
\frac{\frac{2}{3} \times\left(1 \frac{3}{7}-\frac{5}{8}\right)}{\frac{3}{4}+1 \frac{5}{7} \div \frac{4}{7} \text { of } 2 \frac{1}{3} \times x}
$$

2. Name and draw the net of the following figure.

3. Given that the ratio $x: y=3: 5$, find the ratio
$(5 x-2 y):(x+2 y)$
4. In the figure below, ADC is a chord of a circle with centre O passing through $\mathrm{A}, \mathrm{B}$ and C . $B D$ is a perpendicular bisector of $A C . A D=4 \mathrm{~cm}$ and $B D=1 \mathrm{~cm}$.


Calculate the radius OA of the circle.
5. Simplify $\frac{9 x^{2}-1}{3 x^{2}+2 x-1}$
6. John bought five pens and ten books at a total cost of Sh. 400. Ten similar pens and four books cost Sh. 320. Find the total cost of four pens and two books.
7. The size of an interior angle of a regular polygon is 3 times that of its exterior angle. Determine the number of sides of the polyฆon.
8. The mass of a wire $m$ grams $(\mathrm{g})$ is partly a constant and partly varies as the square of its thickness tmm when $\mathrm{t}=2 \mathrm{~mm}, \mathrm{~m}=40 \mathrm{~g}$ and when $\mathrm{t}=3 \mathrm{~mm}, \mathrm{~m}=65 \mathrm{~g}$. Determine the value of $m$ when $t=4 \mathrm{~mm}$.
9. A tourist comes to Kenya with 1940 Euros which she exchanges for Kenya shillings. During her stay she spends Ksh. 75,000 on transport and another Ksh. 50,000 on accommodation. As she leaves, she exchanges the remaining amount to sterling pounds. Given that the exchange rates at the time was as follows.

|  | Exchange rates |  |
| :--- | :--- | :--- |
| Foreign currency | Buying | Selling |
| 1 Euro | Sh. 104.51 | Sh. 104.79 |
| 1 Sterling pound | Sh. 119.96 | Sh. 120.28 |

How much sterling pounds did she have at herdeparture?
10. Solve for x and y in,
$\hat{y}^{y^{y^{e}}} 2^{2 x-3 y}=16$

$$
5^{x-2 y}=1
$$

11. A straight line through the points $P(2,1)$ and $Q(4, h)$ is perpendicular to the line whose equation is $3 y+2 x=5$. Determine the value of $h$ and the equation of line $P Q$ in the form $y=m x+c$
12. Two flag posts $A$ and $B$ stand vertically on ade vel ground some distance apart. Post A
 and the angle of elevation of the top of ofost $B$ from the top of post $A$ is $33.9^{\circ}$. Calculate the height of post B. (Give your answer to 2 decimal places)
13. Use the reciprocal and square tables to evaluate
$\frac{3}{123.4}+0.9829^{2}$
14. In the figure below, O is the centre of the cifole. $\mathrm{AB} \not \uparrow \nsim \mathrm{OC}$ and angle $\mathrm{ABO}=40^{\circ}$. Find angle ACO.
15. The figure below shows a histogram.


Complete the frequency distribution table below.

| Length $x$ cm | Class width | Frequency density | Frequency |
| :--- | :---: | :---: | :---: |
| $7.5 \leq x<9.5$ |  | 1.2 | 24 |
| $9.5 \leq x<11.5$ |  |  |  |
| $11.5 \leq x<15.5$ |  |  | 48 |
| $15.5 \leq x<21.5$ | 6 |  |  |

16. A map is drawn to a sclae of $1: 50,000$. Find fie area in $\mathrm{cm}^{2}$ on the map of a field with an actual area of $60000 \mathrm{~m}^{2}$.


## Answer only FIVE questions in this section in the spaces provided

17. A bus left Mombasa and travelled towards Machakos at an average speed of $60 \mathrm{~km} / \mathrm{hr}$. After $2 \frac{1}{2} \mathrm{hrs}$, a car left Mombasa and travelled along the same road at an average speed of $100 \mathrm{~km} / \mathrm{h}$. If the distancê between Mombasa and machakos is 500 km , determine:
(a) (i) The distance of the bus from Machakos when the car took off.
(ii) The distance the car travelled to catch up the with the bus.
(b) Immediately the car caught up with the bus, the car stopped for 25 minutes. Find the new average speed at which the car travelled in order to reach Machakos at the same time as the bus.
18. (a) Given that $\mathrm{y}=7+3 \mathrm{x}-\mathrm{x}^{2}$, complete the táble below.

| x | -3 | -2 | -1 | 0 | Cel | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y |  | -3 |  |  |  |  |  | 3 |  |  |

(b) Using a suitable scale, draw the graph of $y=7+3 x-x^{2}$
c) On the same grid draw a straight line $y=4-x$
(d) Use the graph to solve the equation $x^{2}-4 x-3=0$

19. Nanyuki Municipal Council intends to introdte open litter bins of the shape shown in the diagram below. Each bin is a frustrum of af ight pyramid standing on a square base ABCD of side 4.5 m . The plane PQRS is paralle ${ }^{\text {el }}$ to the plane ABCD and is $2 / 3$ up the vertical height of the original pyramid. $\mathrm{PQ}=\mathrm{QR}=4.5 \mathrm{~m}$ and the height of the frustrum is 1.5 m .

(a) Calculate the total surface area of the frustrum.
(b) Paint is sold in two litres container which cost Sh. 375 each. $1_{4}$ litre of paint is adequate for painting $5 \mathrm{~m}^{2}$ surface. Find the cost of painting the external surface of ten such bins.
(c) Calculate the volume of one bin.
20. A school planned to buy y textbooks for ađtotal cost of Ksh. 7500. A discount of Ksh. 50 per textbook was given and the school roas able to get five extra textbooks for the same amount of money.
(a) Write an expression in terins of $y$, for the
(i) original price of eadh textbook
(ii) price of each textbook after the discount.

L(b) Form an equation in $y$ and hence determine the number of textbooks the school bought.
(c) Calculate the discount offered to the school as a percentage.
21. Four towns $X, T, Y$ and $Z$ are such that $T$ is $84 \mathrm{R}_{\mathrm{m}}^{\mathrm{m}}$ directly to the North of X and Y is on a bearing of $\mathrm{N} 65^{\circ} \mathrm{W}$ from X at a distance of 60 km . Z is on a bearing of $340^{\circ}$ from Y and at a distance of 30 km .
(a) Using a scale of 1 cm represeent 10 km , make an accurate scale drawing to show the relative positions of the torions.
(b) From your scale drawing, find
(i) the bearing and distance of T from Y .
(ii) the bearing and distance of X from Z .
(c) Calculate the total area covered by the quadrilateral ZTXY in square kilometres.
22. The table below shows distribution of marks fôr 100 candidates in a mathematics test.

| Marks | $0-9$ | $10-19$ | $20-29$ | $30 * 39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ | $90-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> candidates | 5 | 9 | 9 | $\sigma^{8} 11$ | X | 15 | 11 | 9 | 7 | 5 |

(a) Find the value of $x$.


(b) $c^{\wedge}{ }^{\hat{y}}$ Using a scale of 1 cm to represent 10 marks and 1 cm to represent 5 students, draw a cumulative frequency curve.
(c) Use your graph to estimate, (i) the median
(ii) the quartile deviation

23. Draw triangle ABC with $\mathrm{A}(3,4) \mathrm{B}(1,3)$ and $\mathrm{C}^{\circ}(2,1)$
(a) Draw triangle $A^{I} B^{\mathrm{I}} \mathrm{C}^{\mathrm{I}}$, the image offriangle ABC under a rotation of positive $90^{\circ}$ about $(0,0)$
(b) Draw triangle $\mathrm{A}^{I I} \mathrm{~B}^{10^{I I}}$ the image of triangle $\mathrm{A}^{\mathrm{I}} \mathrm{B}^{\mathrm{I}} \mathrm{C}^{\mathrm{I}}$ under a reflection in the line $y=x$
(c) Draw triangle $\mathrm{A}^{\text {III }} \mathrm{B}^{\text {II }} \mathrm{C}^{\text {III }}$ the image of triangle $\mathrm{A}^{\mathrm{II}} \mathrm{B}^{\mathrm{II}} \mathrm{C}^{\text {II }}$ under a translation $e^{2^{S}} \mathrm{~T}=\left[\begin{array}{c}-3 \\ 1\end{array}\right]$
(d) Describe a single transformation that maps $\triangle \mathrm{ABC}$ onto $\Delta \mathrm{A}^{\text {III }} \mathrm{B}^{\text {II }} \mathrm{C}^{\text {III }}$
(e) State the type of congruence between the object and the final image.
24. In a college there are fewer than 40 students $\alpha$. both. The football team comprises more than eleven players while the basketball team comprises more than six players. There are moredian three times as many football players as basketball players.
(a) Taking the number of football players and basketball players to be x and y respectively, write down four inequalities representing the above information.
(b) On the grid provided, draw the inequalities in (a) above
(c) Find the maximum possible number of; (i) basketball players
(ii) football players


