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121/2
MATHEMATICS
PAPER 2
JULY/AUGUST 2014
TIME: $\mathbf{2}^{\mathbf{1}} \mathbf{2} \mathbf{~ H O U R S}$

Date: $\qquad$

## HOMA-BAY SUB-COUNTY JOINT EVALUATION EXAM

## Kenya Certificate of Secondary Education (K.C.S.E)

121/2
Mathematics
Paper 2
$21 / 2$ hours

## INSTRUCTIONS TO THE CANDIDATES

- Write your name and index number in the spaces provided above
- This paper contains two sections; Section 1 and Section 11.
- Answer all the questions in section 1 and only five questions from Section 11
- All workings and answers must be written on the question paper in the spaces provided below each question.
- Marks may be given for correct working even if the answer is wrong.
- Non programmable silent electronic calculators and KNEC Mathematical tables may be used EXCEPT where stated otherwise
- Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.


## FOR EXAMINERS'S USE ONLY

## Section 1

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Section 1I

| Question | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |

GRAND TOTAL


This paper consists of 15 printed pages. Candidates should check carefully to ascertain that all the pages are printed as indicated and no questions are missing.

## SECTION bY50 MARKS ).

## Answer All Questions fröm this section in the spaces provided

1. Evaluate using logarithms

$$
\sqrt[5]{\frac{41.9 \times \log 1.159}{2.3 \times 10^{3}}}
$$

2. Ad unsiness lady bought 180 mangoes at Shs. 60 for every five mangoes. She sold some of them at Shhs. 30 for every three and $33 \frac{1}{3} \%$ the rest at Sh. 30 for every four. If she made a $33 \frac{1}{3} \%$ loss, calculate the number of mangoes sold at Shs 30 for every four
3. Write an equation of a circle that has a diameter whose end points are at $(2,7)$ and $(-6,15)$ in the form $x^{2}+y^{2}+a x+b y+c=0$ where $a, b$ and $c$ are integers
4. Miss Jaber bought a motor cycle at Shs. 160 Q 60 . The depreciation rate was $6 \%$ per annum determined semi annually. How long wilkie take the motor cycle to be valued at a quarter of its original cost
5. Given that $d=\sqrt[3]{\left(\frac{y-1}{y+1}\right)}$ express y in terms of d
6. An arithmetic progression of 41 terms in such that the sum of the first five terms in 560 and sum of the last five terms is -250 . Find the first term
7. (a) Expand and simplify the binomial expression $(2 x-y)^{5}$

8. The graph below is part of the straight line graph obtained from the initial equation $V=a^{n}$

(a) Write down the equation of the straight line in the form $y=m x+c$
(b) Use the graph to calculate the values of a and n
9. In the figure below kite ABCD represents a part of a county government logo. The logo has symmetry order 4 about O . Complete the figure to show the logo

10. The velocity V of a body moving in a straighat 1 ine at any time t given by $\mathrm{V}=3 \mathrm{t}-2$. Its distance S at time $\mathrm{t}=0$ is equal to 4 m . Calculate the distionce when $\mathrm{t}=4$ seconds
11. The sides of a triangle were measured and recorded as $4 \mathrm{~cm}, 6.2 \mathrm{~cm}$ and 9.50 cm . Calculate the percentage error in its perimeter, correct to 2 decimal places
(3mks)
12. The size of an interior angle of a regular polygon is $x^{2}$ while its exterior angle is $3 x$. Find the number of sides of the polygon
(4mks)
13. Without using logarithms table, solve the equation

$$
\log (5 x-4)=\log (x-2)+\frac{1}{3} \log 27
$$

14. A rectangle $A B C D$ is such that $A B=6 \mathrm{~cm}$, and $B C=5 \mathrm{~cm}$. A variable point $P$ moves inside the rectangle such that $\mathrm{AP} \leq \mathrm{PB}$ and $\mathrm{AP}>2.5 \mathrm{~cm}$. Show the region where P lies
15. Without using a calculator or mathematical table, express $\frac{\sin 60^{\circ}}{1-\cos 30^{\circ}}$

In surd form and simplify
16. An angles of 0.9 radians at the centre of the circle subtends an arc of length 28.8 cm . Find
(a) The radius of the circle
(b) The area of the sector enclosed by the arc and radii

## SECTION Be 50 MARKS)

## Answer any five questions from the section in the spaces provided.

17. Mr. Alvin George, a civil servant getsa monthly salary of Shs. 48,000. He lives in a government house where he pays nominal rent of Shs. 2500 . Besides this he gets an automatic house allowance of Shs. 12000 and medical allowanee of shs. 8000 per month. He gets a gamily relief of sh. 1065 per month. The rates of income tax are shown below
Income tax in $\mathrm{K} £$ per mionth rates in shs. Per $\mathrm{K} £$

1-400
401-1200
$10 \%$ 15\%

## 1201-24400

 25\%2401-3600 $35 \%$

3601 and above $45 \%$

Calculate:
(a) His taxable income per month in Kenya pounds
(b) Net tax per month in Kshs.
(c) Net salary
18. The vertices of a rectangle are $\left.\mathrm{A}(-1,-1) \mathrm{B}\left(-4, \mathrm{I}^{1} \mathrm{C}\right)-4,-3\right)$ and $\mathrm{D}(-1,-3)$
(a) On the grid provided, draw the rectande and its image $A_{1} B_{1} C_{1} D$ under a transformation whose matrix is $\left(\begin{array}{cc}-2 & 0 \\ 0 & -2\end{array}\right)$

(b) $\mathrm{A}_{2}, \mathrm{~B}_{2}, \mathrm{C}_{2}, \mathrm{D}_{2}$ is the image of $\mathrm{A}_{1}, \mathrm{~B}_{1}, \mathrm{C}_{1}, \mathrm{D}_{1}$ under a transformation matrix $\mathrm{P}=\left(\begin{array}{cc}\frac{1}{2} & 1 \\ 1 & \frac{1}{2}\end{array}\right)$
(i) Determine the co-ordinates of $\mathrm{A}_{2} \mathrm{~B}_{2} \mathrm{C}_{2} \mathrm{D}_{2}$
(ii) On the same grid draw the quadrilateral $\mathrm{A}_{2} \mathrm{~B}_{2} \mathrm{C}_{2} \mathrm{D}_{2}$
(c) Find the area of $\mathrm{A}_{2} \mathrm{~B}_{2} \mathrm{C}_{2} \mathrm{D}_{2}$
19. A solution whose volume is 120 litres is made up of $35 \%$ water and the rest alcohol. When y litres of alcohol is added the percentage of water dirps to $15 \%$
(a) Find the value of $y$
(b) The new solution is diluted further by addition of seventy litres of water. Calculate the percentage of alcohol in the resulting solution
(c) A blend is made by mixing 10 litres of the solution in (b) above with 20 liters of the original solution. Calculate in the simplest form, the ratio of water to that of alcohol in the blend
20. A passenger plane takes off from airport $\mathrm{A}\left(60^{\circ} \mathrm{N}, 5^{\circ} \mathrm{E}\right)$ and flies directly to another airport $\mathrm{B}\left(60^{\circ} \mathrm{N}, 17^{\circ} \mathrm{E}\right)$ and then flies due North for 800 nautical miles ( nm ) another airport C
(a) Find the position of airport C

(b) कind the distance between airport A and B in nautical miles
(c) If the plane at an average speed of 300 knots , find total flight time
(d)Given that the plane left air port A at 9.20am. Find the local time of arrival at airport C(2mks)
21. In a certain country, the probability of a schoof A topping in county exams is $1 / 3$. If it tops the probability of it topping in KCSE is $5 / 7$ otherwise the probability of it topping in KCSE is $2 / 9$. If the school tops in KCSE the probability oferts appearing in the newspaper is $2 / 5$, otherwise the probability of its appearing in news paper is $^{5} 4 / 11$
(a) Draw a tree diagram to représent the above information
(b) Use the tree diagram to find the probability that:
(i) The school tops in the two exams and appears in the newspaper
(ii) The school did not appear in the newspaper
(iii) The school topped in atleast one exam and did not appear in the newspaper
(iv) The school appeared in the newspaper
22. The diagram below shows a design model of of two circles centre $A$ and $B$ radii 0.5 cm xand 0.8 cm respectively and the distance between their


Calculate in km:
(i) The length of leg CD
(ii) The length of the leg DEG ( $\pi=3.142$ )
(iii) The length of the leg HIC ( $\pi=3.142$ )
(iv) During a race, the course is manned by race officials placed 500 m apart and each is paid

Kshs.2300/= per day. How much is needed to pay race officials for one day event
(4mks)
23. A relief organization has to transport atleast people and atleast 18 tonnes of supplies to a site. There are two types of vehicles available type A and B. type A can carry 900 kg of supplies and 6 people while type B can carry 1350 kg of supplies and 5 people. There are at most 12 vehicles of each type available. By putting $X$ to represent the number of vehicles of type $A$ and $y$ to represent the number of vehicles of type $B$
(a) Write down all the fousinequalities to represent the above information

(b) Qn the grid provided, draw all the inequalities in (a) above

(c) Use the graph in (b) above the determine the least number of vehicles required at the site ( 2 mks )
24. Given that $y=2 x^{0}+\cos 1 / 2 x^{0}$, complete the tabffe below for the missing values of $y$, correct to 1 decimal place

(b) On the grid provide below, draw the graph of $y=\sin 2 x^{0}+\cos 1 / 2 x^{\circ}$ for $0 \leq x \leq 360^{\circ}$ Take the scale 1 cm for $30^{\circ}$ onthe x -axis. 2 cm for 0.5 units on the y -axis.

(c) Use the graph to estimate
(i) The minimum value of $y$

L(fii) The value of $X$ for which $1 / 2 \sin 2 x+1 / 2 \cos 1 / 2 x \geq 0.25$

