NAME: $\qquad$
SCHOOL: $\qquad$ CANDIDATES SIGNATURE:
DATE:

121/2
MATHEMATICS
PAPER 2
JULY/AUGUST-2014.
TIME: $2 \underline{1 ⁄ 2}$ HOURS

## KISII SOÛUHT SUB COUNTY JOINT EVALUATION EXAM - 2014 <br> Kenya Certificate of Secondary Education (K.C.S.E).

421/2
MATHEMATICS
PAPER 2
JULY/AUGUST-2014.
TIME: 2112 HOURS

## INSTRUCTIONS TO CANDIDATES:

(a) Write your name and index number in the spaces provided above
(b) Sign and write the date of examination in the spaces provided above.
(c) This paper consists of TWO sections: Section I and Section II.
(d) Answer $\boldsymbol{A} L \boldsymbol{L}$ the questions in section I and only five from Section II
(e) All answers and working must be written on the question paper in the spaces provided below each question.
(f) Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.
(g) Marks may be given for correct working even if the answer is wrong.
(h) Non-programmable silent electronic calculators and KNEC Mathematical tables may be used except where stated otherwise.

## FOR EXAMINER'S USE ONLY

Section I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Section II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

$\square$

This paper consists of 16 printed pages.
Candidates must check to ascertain that all pages are printed as indicated and that no question(s) is/are missing.

1. Evaluate without using Mathematical tables $\mathbb{Q}^{5} \mathrm{a}$ calculator.

$$
2 \log 5-\frac{1}{2} \log 6+2 \log 40
$$

2. Solve for x given that the following is a singular matrix
3. Make d the subject of the formula.

$$
a^{2}=\sqrt{\frac{1+d^{2}}{b^{2}}-\frac{b}{3}}
$$

4. Simplify $\frac{3}{\sqrt{7-2}}+\frac{1}{\sqrt{7}}$ leaving your answer in the form $a+b \sqrt{c}$, where $\mathrm{a}, \mathrm{b}$ and c are rational numbers.
5. Calculate the percentage error in the volume of a cone whose radius is 9.0 cm and slant length 15.0 cm .
6. The table below shows corresponding values of $x$ and $y$ for a certain curve.

| y | 1.0 | 1.2 | 1.4 | 1.6 | 1.8 | 2.0 | 2.2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| x | 6.5 | 6.2 | 5.2 | 4.3 | 4.0 | 2.6 | 2.4 |

Using 3 strips and mid-ordinate rule, estimate the area between the curve x axis, the line $\mathrm{x}=1$ and $\mathrm{x}=2.2$.
8. 14 people can build 10 huts in 30 days. Find the number of people working at the same rate that will build 18 similar huts in 27 days.
9. The coordingates of two airports M and N are $\left(60^{\circ} \mathrm{N}, 35^{\circ} \mathrm{W}\right)$ and $\left(60^{\circ} \mathrm{N}, 15^{\circ} \mathrm{E}\right)$ respectively. Calcurate;
(iv ${ }^{人}{ }^{\wedge}$ The longitude difference.
(ii) the shortest time an aeroplane whose speed is 250 knots will take to fly from M to N along a circle of latitude.
10. (a) Expand $(x-0.2)^{5}$ in ascending powers of x .
(b) Use your expansion up to the fourth term to evaluate $9.8^{5}$.
11. The figure below is a cuboid ABCDEFGH . $A B^{\circ}=12 \mathrm{~cm}, \mathrm{BC}=5 \mathrm{~cm}$ and $\mathrm{CF}=6.5 \mathrm{~cm}$.

(a) State the projection of AF on the plane ABCD .
(b) $Q^{\rho^{\circ}}$ Calculate the angle between AF and the plane ABCD correct to 2 decimal planes. ( 3 mks )
12. Show that $\frac{\sin x(\cos x+1)}{\operatorname{Cos} x}=\sin x+\tan x$.
13. The mid-point of AB is $(1,-1.5,2)$ and the position vector of a point A is $-\underset{\sim}{1+} j$. Find the magnitude of $\overrightarrow{A B}$ where O is the origin.
14. Draw a line of best fit for the graph of $y$ againgst $x$ using the values in the table below. Hence determine the equation connecting y and $\theta^{2}$.

| x | 0.4 | 1.0 | - | Q. 0 | 2.5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| y | 0.5 | 1.0 | $1.2 e^{\text {e }}$ ( ${ }^{\text {c }}$ | 1.5 | 2.0 |


15. A coffee dealer mixes two brands of coffee, $\mathrm{y}^{s^{\circ}} \mathrm{a}^{\circ} \mathrm{y}$ to obtain 40 kg of the mixture worth Ksh. 2,600. If brand $x$ is valued at Ksh. 70 per $\mathbb{R g}$ and brand $y$ is valued at Ksh. 55 per kg. Calculate the ratio in its simplest form in which bexhids x and y are mixed.
16. The figure below shows a circle centre $\mathrm{O} . \mathrm{AB}$ and PQ are chords intersecting externally at a point C. $\mathrm{AB}=9 \mathrm{~cm}, \mathrm{PQ}=5 \mathrm{~cm}$ and $\mathrm{QC}=4 \mathrm{~cm}$. Find the length of BC .


## SECTION H2 450 MARKS)

## Answer only fivequestions in this section

17. (a) Salome invested Ksh. 250,00@for $21 / 2$ years in an account which paid $16 \%$ compound interest p.a. The interestas compounded quarterly. At the end of $21 / 2$ years she withdrew all the amount and spent it to the nearest thousands to buy four similar motor cycles. She earned an averagê of Ksh. 10,000 from each motorcycle per month.
(i) the $a^{2} n^{2}$ ount she withdrew at the end of $21 / 2$ years.
(ii) $e^{\text {t }}$ the cost of each motorcycle.
(iii) $x^{2^{\ell}}$ the total earnings from the motorcycles for 3 years.
(b) $e^{2}$ She decided to sell the motorcycles after depreciating at an average rate of $20 \%$ p.a for the 3 years.
Find:-
(i) the new value of each motorcycle after depreciation.
(ii) the profit earned from her initial investment to the nearest shilling.
18. The table below shows the distribution of agef $s^{5}$ in years of 50 adults who attended a clinic:-

| Age | 21-30 | 31-40 | 41-50 | 58-60 | 61-70 | 71-80 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 15 | 11 | $17 \mathrm{c}^{\text {e }}$ | 4 | 2 | 1 |

(a) State the medium class
(b) Using a working ${ }^{\text {m mean }}$ of 45.5 , calculate:-
(i) the sinean age
(ii) $e^{-e^{6} \mathrm{H} \text { e }}$ standard deviation
(iii) $\otimes^{2^{2}}$ Calculate the $6^{\text {th }}$ docile.
19. An arithmetic progression (AP) has the first tefrm a and the common difference d .
(a) Write down the third, ninth and twenty fifth terms of the AP in terms of a and d. (1mk)
(b) The AP above is increasing and the third, ninth and twenty fifth terms form the first three consecutive terms of a Gemetric Progression (G.P) The sum of the seventh and twice the sixth terms of the AP is 78. Calculate:-
(i) the first tertm and common difference of the AP.
(ii) the $s x_{1} \mathrm{~m}^{2} \mathrm{~m}$ of the first nine terms of the AP.
(iii) $e^{\text {Th }}$ he difference between the fourth and the seventh terms of an increasing AP.
20. The probability that three candidates; Anthozy, Beatrice and Caleb will pass an examination are $3 / 4,2 / 3$ and $4 / 5$ respectfully. Find the jorobability that:-
(a) all the three candidates will
(b) all the three candidates, evill not pass.
(c) only one of them wasil pass
(d) only two of thệm will pass.
(e) at most two them will pass.
21. (a) Complete the table below for the function $y=(3-x)(x+1)$

| x | -3 | -2 | -1 | $0 \times 0^{08}$ | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{x}+1$ | -2 | -1 |  | $\mathrm{do}^{\text {cos}}$ |  | 3 | 4 |  |
| $3-\mathrm{x}$ | 6 | 5 |  |  | 2 | 1 |  | -1 |
| y | -12 | -5 | $8^{\text {e }}$ | 3 | 4 |  | 0 | -5 |

(b) Use the values inthe table to draw the graph of $y=(3-x)(x+1)$. Use the following scale.
Horizontal axis 2 cm for 1 unit
Verticat axis 1 cm for 1 unit.
(3mks)
(c) Use, your graph in part (b) above to solve the following quadratic equations
(ii) $\quad-x^{2}+2 x+3=0$
(ii) $-x^{2}+x+6=0$

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\#$ |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  | , |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

22. Use a ruler and a pair of compasses only all genstructions in this question.
(a) Construct the rectangle ABCD sueh that $\mathrm{AB}=7.2 \mathrm{~cm}$ and $\mathrm{BC}=5.6 \mathrm{~cm}$.
(b) Constructs on the same diagram the locus $L_{1}$ of points equidistant from $A$ and $B$ to meet with another locus $\mathrm{L}_{2}$ of eqoints equidistant from AB and BC at M . measure the acute angle formed at M by $\mathrm{L}_{1}$ and $\mathrm{L}_{2}$.
(c) Construct on the diagram the locus of point K inside the rectangle such that K is less than 3.5 cm . 4 rom point M . Given that point $K$ is nearer to $B$ than $A$ and also nearer to BA than $\mathrm{Be}^{5}$, shade the possible region where K lies. Hence calculate the area of this region. Coņ̂ect to one decimal place.
23. The diagram below, not drawn to scale shows part of the curve $y=x^{2}+5$ and the line $y=8-2 \mathrm{x}$. The line intersects the curve at points $\mathrm{C}_{5}$ arid D . Lines AC and BD are parallel to the y -axis.

(a) $Q^{2}$ Determine the coordinates of C and D .
(b) Use integration to calculate the area bounded by the curve and the x -axis between the points C and D .
(c) Calculate the area enclosed by the lines CD, CA, BD and the x -axis.
(d) Hence determine the area of the shaded region.
24. A tailoring business makes two types of garments A and B. Garment A requires 3 metres of material while garment B requires $21 / 2$ metres of material. The business uses not more than 600 metres of material daily in making both garments. It must make not more than 100 garments of type A and nor less than 80 of ty fee B each day.
(a) Write down three inecualities from this information other than $x \geq 0$ and $x \geq y$, where x is the number of garments of type A and y the number of garments of type B. (3mks)
(b) Graph these inequalities.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  | - | - |  |  | - |  |  |  | , | - |  | , |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  | - |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | $4$ |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  | , |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  | - |  |  |  | , | - |  | - |  |  |  | - | $\nabla$ |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | - |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  | , |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\square$ |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  | - |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  | , |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  | - |  |  |  |  |  |  | - |  |  |  |  | - |  |  | - | - | - |  | - |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  | $7$ |  |  |  |  | - |  |  |  |  |  |  |  | - | $\dagger$ |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | , | - |  |  |  |  | - |  |  |  |  | - |  |  |  |  |  |  |  |  | , |  |  | - |  |  |  | - | , |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $11$ |  |  | $1$ |  |  |  |  |  |  |
|  | , |  |  |  |  |  |  |  |  | - | - |  |  |  |  | - |  | $\sim$ |  |  |  | , |  |  | $\cdots$ |  |  |  | , | , |  |  | - |  |  |  | O | $\square$ |

(c) If the business makes a profit of sh $8 \mathbb{Q}^{5}{ }^{5}$ garment A and a profit of sh. 60 on garment B , how many garments of each typeriust it make in order to maximize the profit and what is the total profit?

