NAME： $\qquad$

## SCHOOL：



## $121 / 2$

MATHEMANTCJÊS
PAPER $20^{2}$
JULAY ${ }^{〔}$ GU゙GUST 2007
2 安 准OURS

# BUNGOMA DISTRICT MOCK EXAMINATION Kenya Certificate Of Secondary Education 2007 

121 ／ 2
MATHEMATICS
PAPER 2
JULY／AUGUST 2007

## INSTRUCTIONS TO CANDIDATES

1．Write your name and index number in the spaces provided at the top of this page．
2．This paper consists of two sections：Section I and Section II．
3．Answer all questions in section I and any five questions from Section II．
4．Show all the steps in your calculations，giving your answers at each stage in the spaces below each question．
5．Marks may be given for correct working even if the answer is wrong．
6．Non－programmable silent electronic calculators and KNEC Mathematical tables may be used，except where stated otherwise．

For Examiner＇s Use Only
SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

Grand
Total

This paper consists of 16 pages．Candidates should check the question paper to ensure that all the pages are printed as indicated and no questions are missing．

## SECTION I ( 50 Marks)

## Answer all the questions in this section.

1. Given the gordditions that $\log \mathrm{a}=-1.3748$ and $\log \mathrm{b}=-1.5934$, evaluate $\log \sqrt{\frac{a}{b}}$.
2. Find the value of X in which $\operatorname{det}\left(\begin{array}{cc}1 & 3 \\ -2 & x\end{array}\right)=\operatorname{det}\left(\begin{array}{cc}x^{2} & 4 \\ 1 & 3\end{array}\right)$
3. Make x the subject of the formula.

$$
P=\frac{x^{1 / 2} y}{x^{1 / 2}-y}
$$

4. Use reciprocal, square afic cube root tables to evaluate to 4 significant figures, the expression.

$$
\begin{equation*}
\sqrt[3]{\frac{9 e^{e^{\frac{\varepsilon}{s}}}}{0.03 \S 46}+0.6042^{2}} \tag{3marks}
\end{equation*}
$$

5. Solve for x in the equation. $3 \cos ^{2} x+\sin x+1=0$

$$
0 \leq x \leq 360^{\circ}
$$

(4 marks)
6. A coffee blender mixes 6 parts of type A with 4 parts of type B. If type A costs sh 72 and type B costs him sh 66 per Kg respectively, at what price should he sell the mixture in order to make $5 \%$ profit? Give your answer to the nearest ten cents.
(3 marks)
7. Using a ruler and pair offcompasses only. Construct an equilateral triangle ABC of sides 4 cm construct the locus of $f$ a point $P$ such that $P$ is always on the same side of $B C$ as $A$ and $\angle \mathrm{BPC}=30^{\circ}$. Seade the region where Q can be found if Q is outside the triangle and angle $\mathrm{BQ} \mathrm{S}_{6}^{6^{2}} \mathrm{C} 80^{0}$.
8. A right circular cylinder is to be made so that the sum of its radius and its height is 6 cm . Find the maximum possible volume of the cylinder.
(3marks)
9. Expand $\left(3 x-\frac{1}{3} y\right)^{4}$ By giving suitable values of x and y in your expansion. Obtain the value of $(29.5)^{4}$ correct 4 d.p ( step by step)
10. A point $P(2,-3)$ undergoes transformation represented by the matrix $\left(\begin{array}{ll}3 & 0 \\ 0 & 1\end{array}\right)$. Find the co ordinate of the image of P .
11. Water flows at $3 \mathrm{~m} / \mathrm{s}$ through a pipe of radius 3.5 cm . How long does it take to fill a rectangular tank 9 m long, 7 m wide and 3 m deep?
(3marks)
12. A quantity $R$ values partly as $x$ and partly inversely as $y$. Find the equation connecting R, x and y , when $\mathrm{x}=1, \mathrm{y}=2$ and $\mathrm{R}=4$, When $\mathrm{x}=3, \mathrm{y}=2$ and $\mathrm{R}=10$. marks)
13. Calculate the interest gй sh 10,000 invested for $1 \frac{1}{2}$ years at $12 \%$ p.a. Compounded semiannually.

14. The radius of a circle is measured to the nearest meters as 7 m . Calculate the percentage error in the circumference. Leave your answer as a mixed number and take $\pi=\frac{22}{7}$.
15. The first, the fifth and \&feventh terms of an increasing arithmetic progression are three consecutive terms 㷂参 geometrical progression. If the first term of the arithmetic progression is 6. Find
(i) The cornamon difference of the arithmetic progression.
(ii) The common ratio of the geometric progression.
16. How long will it take a car 4 meters long moving at $75 \mathrm{~km} / \mathrm{h}$ to completely overtake a heavy commercial truck 11 m long moving in the opposite direction at $45 \mathrm{~km} / \mathrm{h}$ if the car is 5 m in front of the truck?

## SECTION II (50 Marks)

## Answer any five questions from this section.

17. The intensity I'of a lamp was measured for various values of voltage V across it and the result tabulated

| V(volts) | , 19 | 14.1 | 15.8 | 17.8 | 20.0 | 22.4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I (lux) ${ }^{2}{ }^{2} \sim^{20}$ | 81.8 | 301.2 | 362.3 | 507.9 | 691.2 | 922.0 |
| Log |  |  |  |  |  |  |
| LGA (I+200) |  |  |  |  |  |  |

It is believed that V and I conform to the Law in the form $\mathrm{I}=\mathrm{KV}^{\mathrm{n}}-200$, where K and n are constants Draw suitable linear graph and determine the values of K and n hence determine I in terms of V .
(10marks)
18. The following table shgows the marks scored in mathematic test by 40 students in Nasalayi secondary school.

| Marks |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No oof <br> sfudents | $6-10$ | $11-15$ | $16-20$ | $21-25$ | $26-30$ | $31-35$ | $36-40$ |

From thestabde table above
(a) Calcallate the mean and Median
(5mks)
(b) Draw the cumulative frequency curve

Use the graph to estimate the
(i) Interquartile range
(ii) Probability that a student picked at random scored between 8 and 29 marks. ( 1 mk )
19. (a) Complete the table foelow by filling in the blank spaces for the functions. $\mathrm{y}=2 \sin (\mathrm{x}+30)$ and $y=2 \cos 1 / 2 x$ for $0^{0} \mathbb{E}^{5} x \leq 210^{\circ}$

| $x$ | $x^{08}{ }^{\text {a }}$ | 30 | 60 | 90 | 120 | 150 | 180 | 210 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y=2 \sin (x+3 Q)^{2}$ | $c^{6.00}$ |  | 2.00 |  | 1.00 |  | -1.00 |  |
| $y=2 \cos d / y^{6}$ | 2.00 |  | 1.73 |  |  |  | 0.00 |  |

(b) An using completed table in (a) above draw the graphs of $y=2 \sin (x+30)$ and $y=2 \cos 1 / 2 x^{0}$. (c)

Take 2 cm to rep 1 unit on y axis and 2 cm rep $15^{\circ}$ on the x - axis.
(c) Use your graph to solve
(i) $2 \sin (x+30) \geq 2 \cos 1 / 2 x \quad$ for $0 \leq x \leq 210^{\circ}$.
(1 mark)
(ii) $2 \sin 1 / 2 x=0.5$
(d) State the amplitude and period.
(i) $2 \sin (x+30)$
(ii) $2 \cos \frac{1}{2} x$
20. The figure below shows, friangle OPQ in which $\mathrm{OP}=\mathbf{p}$ and $\mathrm{OQ}=\mathbf{q}$. Points D and E are such that $3 \mathrm{PD}=\mathrm{PQ}$ and $\mathrm{OE}=\frac{1}{2} \mathrm{t}$

(a) Express in terms of $\mathbf{p}$ and $\mathbf{q}$ vectors
(i) OD
(ii) $\mathbf{Q E}$
(b) If $\mathrm{OX}=\mathrm{k}$ OD and $\mathrm{QX}=\mathrm{h}$ QE where k and h are constants, express OX in terms of the following in simplified from.
(i) $\mathrm{k}, \mathbf{p}$ and $\mathbf{q}$
(ii) h, pand $\mathbf{q}$
(c) Find the value of h and k .
(d) If $\mathbf{r}=3 \mathbf{i}-\mathbf{j}+\mathbf{k}$ and $\mathbf{t}=\mathbf{j}+2 \mathbf{k} . \mathrm{P}=\mathbf{r}+\mathbf{t}$ find $|\mathbf{P}|$ to 4 s.f.
(2marks)
21. P and Q are two points griatitude $60^{\circ} \mathrm{S}$. Their longitudes are $30^{\circ} \mathrm{E}$ and $90^{\circ} \mathrm{W}$ respectively.

## Find:

(a) The distane between P and Q along the parallel of latitude (Take radius of earth $=6370$

(b) The shortest distance along the earth's surface between P and Q [to 1 decimal place]
(3 marks)
(c) A weather forecasters reports that the center of a cyclone at $\left(30^{\circ} \mathrm{S}, 120^{\circ} \mathrm{W}\right)$ is moving due south at 24 knots. How long will it take to reach a point $\left(45^{0} \mathrm{~S}, 120^{\circ} \mathrm{W}\right)$ ?
(d) If it is 1400 hrs at Q , What will be the time at P ?
22. A company makes brands A and B of breakfast cereal both of which are enriched with vitamins P and Q. The necessariy information about these cereals is given by the table below.

|  | Cereal |  | Minimum Daily Requirement |
| :---: | :---: | :---: | :---: |
|  | A | B |  |
| Vitamin P(unif8 ${ }^{\text {gram) }}$ | 1 | 2 | 100 |
|  | 5 | 3 | 300 |
| Cost/grayin $4^{\prime \prime}$ | Sh 20 | Sh 30 |  |

(a) Fornoall inequality to represent this information.
(b) Draw the inequalities on the graphs showing the region which satisfy the inequalities. (3 marks)
(c) From your graph determine the minimum daily requirements of vitamins P and Q at the lowest cost
(d) Determine the lowest cost.
23. The figure below shows $\mathcal{F}^{2}$ pulley with wheels center M and N , with a rubber belt ABCDEFA stretched round the $z^{6}$ heels. The diameters of the wheel are 24 cm and 8 cm and the centers are 20 cm apart. Point divides MN in the ratio 3:1]


Find the area of the shaded region
(10 marks)
24. The figure below shows $\mathcal{F}_{\text {fif }}$ frustrum with a rectangular base which measures 18 cm by 24 cm and the top measuring $6 \mathrm{c}_{\mathrm{E}}^{\mathrm{c}} \mathrm{h}$ by 8 cm . The slant edges are 26 cm long each

(a) Draw the net of the frustrum to scale 1:4
(b) Find the height of the original pyramid.
(c) Determine the angle between
(i) Line B G and EH
(ii) Plane BCHG and the base EFGH

