Name. $\qquad$ Index No $\qquad$
School
Date $\qquad$
Candidate's Signature. $\qquad$

## $121 / 2$

MATHEMATICS

## PAPER 2

JUNE /JULY 2012
$21 / 2$ HRS

## BUTERE DISTRICT JOINT EVALUATION - 2012 <br> Kenya National Examination Council (K.C.S.E)

121 /2
MATHEMATICS
PAPER 2
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## INSTRUCTIONS TO CANDIDATES

1. Write your name and index number in the spaces provided at the top of this page.
2. Sign and write the date of examination in the spaces provided above.
3. This paper consists of two sections: Section I and Section II.
4. Answer ALL questions in section 1 and ONLY FIVE questions from section II
5. All answers and workings must be written on the question paper in the spaces provided each question.
6. Marks may be given for correct working even if the answers are wrong.
7. Non - Programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.
8. Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.

## FOR EXAMINERS USE ONLY

Section I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Section II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

GRAND
TOTAL

# SECTION ${ }^{4}$ ( 50 MARKS) <br> <br> Answer all theriuestions in this section. 

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1. Use logarithms correct to 4 decinhal places, to evaluate.

$$
\frac{6.373 \log 4.948}{\sqrt{0.004636}}
$$

2. Rationalize the denominator and write the following in the form $\frac{1}{c}(\mathrm{a}+\sqrt{b})(\mathrm{d}+\sqrt{e})$ where a,b,c,d and e are constants. $\frac{3-\sqrt{7}}{\sqrt{6+1}}$
3. Without using tables or calculators evaluate.
$\frac{3.2 \div 2.5 \text { of } 0.16}{1.52+1.24 \times 2.6 \div 1.3}$
(3mks)
4. Solve the inequalities $1 / 2 x x^{e^{2}}-2<-2 x+1 \leq-2 x+1 \leq \frac{2}{5} x$ and show your solution on a number line.
5. The principal of Butere High School, decided to have a charity walk to raise money to build a dormitory. She will cover 10 km on the first day. Thereafter, she will cover 2 km more than the previous day.
Find:
a) The distance she will travel on the $13^{\text {th }}$ day.
b) How many days she will require to cover a total of 400 km .
6. Find the $x$ - coordinates of the points on the curve $y=3 x^{3}+18 x^{2}+2 x+3$ at which the gradient is 2 .
7. The transformations X and Y have the $\mathrm{e}^{\text {at }} \mathrm{s}^{0^{\circ}}$ image $A^{`} B^{`}$ of $A B$ where, $A\left(2^{2,2}\right)$ and $B(5,4)$, Under the combined transformation YX.
8. 远 A school bus was valued at sh 6,000,000 in January 2000. Each year, its value decreased by $12.5 \%$ of its value at the beginning of the year. Find the value of the bus in January 2005, giving your answer correct to 4.s.f
( 3 mks )
9. The length and breath of a rectangular card were measured to the nearest millimeter and found to be 14.5 cm and 10.6 cm respectively. Find the percentage error in the perimeter.
(3mks)
10. Solve the following equation;
$\operatorname{Sin}\left(2 \theta-30^{\circ}\right)=\frac{\sqrt{3}}{2}$ for $0^{\circ} \leq \theta \leq 180^{\circ}$
11. a) Draw a line $\mathrm{AB}=8.6 \mathrm{~cm}$ with A as the centre draw a circle radius 3 cm . Draw a tangent from $B$ to the circle.
b) Measure the length of this tangent
12. Make x the subject of the formula.

$$
\mathrm{H}=\mathrm{n} \sqrt{\frac{t+k x}{t-K x}}
$$

13. A circle of radius 7 units has it's centre at $^{6}$ the point of intersection between the lines $x+2 y$ $+1=0$ and $2 x+3 y-3=0$
Find the equation of the circle expressing it in the form $x^{2}+y^{2}+g x+f y+c=0 \quad(3 \mathrm{mks})$
14. a) Expand $(3 x-1 / 3 y)^{4}$ fully
b) By substituting suitable values of $x$ and $y$ in your expansion, obtain the value of $(29.5)^{4}$ to 4 significant figures.
( 2 mks )
15. A translation maps a point $\mathrm{P}(3,2)$ onto $\left.\mathrm{P}_{e} \psi^{5} 5,-4\right)$.
a) Determine the translation vector?
b) A point $\mathrm{Q}^{\prime}$ is the image of the point $\mathrm{Q}(2,5)$ under the same translation. Find the length of $\mathrm{P}^{`} \mathrm{Q}^{`}$ leaving the answers in surd form.
( 2 mks )
16. Two grades of tea, costing sh 100 and 150 per kg respectively are mixed in the ratio $3: 5$ by weight. The mixture is then sold at sh. 160 per kg . Find the percentage profit on the cost price.

## SECTION

Answer only five questionsin this section in the spaces provided.
17. In a safari rally drivers are to follow a route PQRST. Q is 375 km from P on a bearing of $075^{\circ}, \mathrm{R}$ is 105 km from Q and a bearing of $110^{\circ}$ from Q . The bearing of T from S is $040^{\circ}$ and a distance of 450 knq . ${ }^{5}$
a) By using a scale ofei cm to represent 30 km , draw a well labeled diagram to represent the route PQRST !.
b) ${ }^{x}{ }^{x}$ Hence determine.
i) The distance of P from R .
ii) The bearing of Q from R .
iii) The distance and bearing of P from S .
18. A cupboard has 7 white cups and 5 brown cups all identical in size and shape. There is a blackout in the town and Mrs. Wafula has to select three cups one after the other without replacing the previous ones.
a) Draw a tree diagram for the information.
b) Calculate the probability that shere $\mathrm{c}^{\circ} \mathrm{O}$
i) Two white cups and one brown cup
iii) At least one white cup.
iv) Three cups of the same colour
19. In a botanical experiment, the length of 60 leaves of a certain type of a tree were measured correct to the nearest 0.1 cm .

| Length <br> $(\mathrm{cm})$ | $3.0-3.4$ | $3.5-3.9$ | $4.0-4.4$ | $4.5-4.9$ | $5.0-5.4$ | $5.5-5.9$ | $6.0-6.4$ | $6.5-6.9$ | $7.0-7.4$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of <br> leaves | 1 | 4 | 9 | 14 | 12 | 10 | 6 | 3 | 1 |

a) State the modal class
(1mk)
b) Calculate the median length

## c) Using a workitg mean of 5.2 find;

i) The mean
ii) The standard deviation
(2mks)
20. The diagram below shows a right pyramid VABCD, v as the vertex. The base of pyramid is a rectangle $A B C D$, with $A B=4 C M$ and $B C=3 C M$. The height of the pyramid is 6 cm .

a) Calculate the
i) Length of the projection of VA on the base and the angle it makes with the base.
( 4 mks )
ii) Angle between the face VAB and the base.
b) $\quad \mathrm{P}$ is the midpoint of VC and Q is the midpoint of VD . Find the angle between the plane VAB and the plane ABPQ.

A company wishes to buy two types of squash machines; Electric and manual. A manual machine requires 4 attendants whereas an electric one requires two. An electric machine fills 300 packets per hour; a manual one can fill 200 packets per hour. At least 3000 packets need to be filled per hour and the number of attendants should not exceed 40.
a) Write down inequalities to describe these conditions and graph them. ( 7 mks )
b) If for every hour it is used, an electric machine brings a profit of shr. 200 and a manual one shr. 500 , determine the number of machines of each type that should be installed in order to maximize profit per hour.
c) Find the maximum profit
a) Draw the graph of $Y=-x^{2}+2 x+8$ for $-2 \leq x \leq 4$
b) Use 6 trapezia to estimate the area enclosed by the curve $y=-x^{2}+2 x+8$, the line $x=$ -2 and $X=4$ and the $\mathrm{x}-\mathrm{axis}$
c) Hence find the percentage error in area of (b) above and the exact area. ( 4 mks )
23. In the figure below $\mathrm{PQ}=\mathbf{Q}$ and $\mathrm{PR}=\mathbf{r} \mathrm{QM}: \mathrm{MR}=1: 2$. The point S is the midpoint of PQ . X is the intersection of PM and $\mathrm{SR} . \mathrm{SX}=\mathrm{hSR}, \mathrm{pX}=\mathrm{kPM}$ where k and h are constants.


Find:
a) $\quad Q R$ in terms of $q$ and $r$.
b) PM in terms of $q$ and $r$

## c) $\varsigma^{\chi}$ SR in terms of $q$ and $r$

d) Express SX in two ways in terms of $\mathrm{h}, \mathrm{r}$ and q and in terms of $\mathrm{k}, \mathrm{r}$ and q , hence determine the ratio in which $x$ divides $S R$.
( 6 mks )
24. Two tewns A and B lie on the same latitude in the northern hemisphere. When it is 8:00 am At , the time at B is 11:00 a.m.
a $\Phi^{\partial}$ Given that the longitude of A is $15^{0} \mathrm{E}$, find the longitude of B .
b) A plane leaves A for B and takes $31 / 2$ hours to arrive at B traveling along a parallel of latitude at $850 \mathrm{~km} / \mathrm{h}$.
Find:
i) The radius of the circle of latitude on which town A and B lie.
ii) The latitude of the two towns. $s^{2}\left(\frac{7}{6}\right.$ Take radius of the earth to be 6371 km$)$.

