SCHOOL $\qquad$ SIGN

121/1
MATHEMATICS ALT. A
PAPER 1
JULY/AUGUST 2012
TIME $2 \underline{1} 2$ HOURS

## KERICHO DISTRICT JOINT KCSE TRIAL EXAMINATION-2012

Kenya Certificate of Secondary Education (K.C.S.E)
121/1
MATHEMATICS ALT. A
PAPER 1
gULY/AUGUST 2012
TIME $2 ½$ HOURS

## INSTRUCTIONS TO THE CANDIDATES

(a) Write your name and the index number in the spaces provided above.
(b) Sign and write the date of examination in the spaces provided.
(c) This paper consists of TWO sections: Section I and II.
(d) Answer ALL the questions in section I and only FIVE questions from section II.
(e) All answers and working must be written on the question paper in the spaces provided below each question.
(f) Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.
(g) Marks may be given for correct working even if the answer is wrong.
(h) Non-programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.
FOR EXAMINERS USE ONLY.
SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |



1. Use logarithms tables to evaluate
2. By using the substitution $y=2^{x}$, solve the equation. $5 \times 2^{2 x+1}-3 \times 2^{x}-34=0$
3. Simplify completely

$$
\frac{3 x^{2}-1}{x^{2}-1}-\frac{2 x+1}{x+1}
$$

4. Without using mathematical tables evaluate.

$$
\frac{20 \times(-3)(-0.1) 7(-2)^{3}}{8 \div 0.4}
$$

5. A circle centre $o$, has the equation $x^{2}+y^{2}=4$ The area of the circle in the first quadrant is divided into 5 vertical strips each of width 0.4 cm .
a) Use the equation of the circle to complete the table below for values of y correct $2(1 \mathrm{mk})$ decimal places.

| X | 0 | 0.4 | 0.8 | 1.2 | 1.6 | 2.0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 2.00 |  |  | 1.60 |  | 0 |

b) Use the trapezium rule to estimate the area of the circle.
6. Three quantities $t, x$ and $y$ are such that $t$ varies directly as $x$ and inversely as the square root of $y$. Find the percentage decrease in $t$ if $x$ decreases by $44 \%$.
(4mks)
7. A circle whose centre ( $-2,5$ ) passes through point $\mathrm{P}(10,10)$. Find the equation of the circle in the form of $a x^{2}+b y^{2}+c x+d y+k=0$. Where $a, b, c$ d and k are constants.

In the figure below $O \underset{\sim}{A}=3 \underset{\sim}{i}+4 \underset{\sim}{i}$ and $O B=8 \underset{\sim}{i} \underset{\sim}{i}$ C is a point on $\underset{\sim}{A B}$ such that $A C: C B=3: 2$, and $\underline{\mathrm{D}}$ is a point such that $\mathrm{OB} / / \mathrm{CD}$ and $2 O B=C D$


Determine the vector $D A$ in terms of $i$ and $j$
(3mks)
9. Given that $\log 4=0.6021$ and $\log 6=0.7782$, without using mathematical tables or a calculation, evaluate $\log 0.096$.
(3mks)
10. The figure below shows three circles each otyers externally.


If the centes of the circle form a triangle with sides of length $9 \mathrm{~cm}, 7 \mathrm{~cm}$ and 6 cm .Calculate the radii of the circles.
11. If $\operatorname{Cos} \theta=\frac{-15}{17}$ and $\theta$ is obtuse, find without using tables the values of a) $\tan \theta$.
b) $\sin \left(180^{\circ}-\theta\right)$
12. The angles of a quadrilateral are $3 x, 2 x, x+1 f^{\text {and }}$ and $2(x-7)$ degrees. Find the smallest angle.
13. On the diagram below, the line whose equation is $7 y-3 x+30=0$ passes through points $A$ and $B$. Point A is on the x -axis while point B is equidistant from $\mathrm{x}-$ and $\mathrm{y}-$ axis


Calculate the coordinates of points A and B.
14. A Kenyan businessman bought goods from Jápan worth 2,950,000 Japanese Yen.On arrival in Kenya, custom duty of $20 \%$ was changed on the value of the goods. If the exchange rates were as follows.

If the exchange rates were as follows:-
1 us dollar = 118 Japanese yere
1 us dollar $=76$ Kenya shilling's
Calculate the duty paid in Kenya shillings.
a) Construct a net of the triangular prism shown, where the cross section is an equilateral triangle.

b) Calculate the surface area of the prism.
(2mks)
16. Find the positive number m for which
$\int_{1}^{m} 4 x^{3} d x=80$

## SECTION IL (50 MARKS)

Answer ANY FIVE questions from this section in the spaces provided
17. Two types of tea in Kericho grade A anaf grade B1 are mixed. Grade A costs sh. 85 per kg, and grade B costs sh. 70 per kg.
a) If the tea are mixed in the ratio $2: 1$, find the cost 2 kg of the mixture.
b) The tea is to be sold in 2 kg boxes at a $30 \%$ profit. Find the selling price of the tea. $(2 \mathrm{mks})$
c) At the end of the week the price of a 2 kg box is reduced to sh. 125 . Find the percentage reduction in the price .
(2mks)
d) Origianally 200 kg of grade A and 100 kg of grade B were bought 240 kg of the mixture was sold at the price of part $b$, and the rest was sold at the reduced price of part C. Find the overall percentage profit.
(3mks)
18. Mr. Barmuriat a farmer in Ainamoi division $\overbrace{\mathbb{*}}$ Kericho District has a triangular field, ABC . The ratio of the length $\mathrm{AB}: \mathrm{AC}=6: 7$. If $\mathrm{BC}=48 \mathrm{~m}$ and the perimeter of the field is 118 m ,.

b) A water tap is installed inside the field such that the tap is equidistant from each of the vertices of the plot. Calculate the distance of the tap from vertex A.
c) Find the size of the acute angles between the edges AB and BC .
19. A cylindrical water tank can be filled to a dejtith of 2.1 meters by a pipe p in 2 hours. Pipe Q takes 7 hours to fill the tank to the same depth. $\mathrm{E}^{9}$ pe R can empty this amount of water in 6 hours.
a) i) Starting with the tarik empty, P runs alone for one how. How many centimeters deee will the water in the tank than be?
ii) If pipe P is now turned off and pipe R left open for one hour what depth of water will remain in the tank?
b) If the tank is initially empty, and pipe P and Q are both running and pipe R is left open, how long will it take to fill the tank to a depth of 2 meters?
20. In the figure below, $O$ is the centre of the cirgfe radius 3 cm and $A B$ is a chord such that its shortest distance from O is 1 cm .


## Calculáte:

a) The length of the chord AB.
b) Angle AOB
c) The area of the minor sector OAB.
d) The area of the shaded segment.
21. If $x^{2}+y^{2}=29$ and $x+y=3$
a) Without solving for x and y deterermine the values of
i) $x^{2}+2 x y+y^{2}$
ii) $e^{2 e^{x^{2}} x y}$
iii) $x^{2}-2 x y+y 2$
(2mks)
iv) $x-y$
b) Find the values of $x$ and $y$.
22. A frequency distribution of marks obtained $b_{2} y 920$ candidates is to be represented in a histogram. The table below shows the grouped marks $\%$ frequencies for all the groups and also the area and height of the rectangle for the group $30{ }_{\sigma}{ }^{\alpha} 60$ marks.

| Marks | 0-10 | e8-30 | 30-60 | 60-70 | 70-100 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | $12{ }^{\text {c }}$ | 40 | 36 | 8 | 24 |
| Area of rectangle | $e^{\text {e }}$ |  | 180 |  |  |
| Height of rectangle | - |  | 6 |  |  |

a) i) Completesthe table.
(4mks)
ii) On the ${ }^{\text {g }}$ grid provided below, draw the histogram.

b) i) State the group in which the median mark lies.
ii) A vertical line drawn through the median mark divides the total area of the histogram into two equal parts. Using this information or otherwise, estimate the median mark.
23. Four points B,C Q and b lie on the same plafe. Point $Q$. Point B is 42 km due south - west of point Q . Point c is 50 km on a bearing of $560^{\circ} \mathrm{E}$ from Q . Point b is equidistant from B 1 Q and C .
a) Using the scale : 1 cm represents 10 km , construct a diagram showing the positions of B,C, Q and D.
b) Determine the:
i) distance between B and C .
ii) bearing of $D$ from $Q$.
iii) bearing of $D$ from $B$.
24. In the figure below $D A$ is a diameter of the cifccle ABCD centre o , radius 10 cm . TCs is a tangent to the circle at $\mathrm{c}, \mathrm{AB}=\mathrm{BC}$ and angle DACo

(a) Find the size of the angle
i) ACS
ii) BCA
b) Calculate the length of
i) AC
ii) AB
(4mks)

