$\qquad$ SIGNATURE: $\qquad$ DATE: $\qquad$

121/2

## MATHEMATICS ALS ${ }^{3}{ }^{*}$ A'

## PAPER 2

## JULY/AUGUSTi 2012

## $21 / 2$ HRS

# KISUMU NORTH AND EAST JOINT EVALUATION TEST Kenya Certificate of Secondary Education Mathematics 

## Paper 2

$2^{1 ⁄ 2} \mathrm{hrs}$

## Instructions to candidates

1. Write your name and index number in the spaces provided above.
2. Sign and write date of examination in the spaces provided above.
3. This paper consists of TWO sections, section I and section II.
4. Answer all the questions in the section I and only five questions from section II
5. All answers and workings must be written on the question paper in the spaces provided below each question.
6. Show all the steps at each stage in the spaces below each question.
7. Marks may be given for correct working even if the answer is wrong.

For Examiners use only.

## SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |



## SECTION I (50MARKS)

## Answer all the questions in this section in the spaces provided.

1. Use logarithms to evaluate the value of

$$
\frac{(0.4 \times 27)^{\frac{1}{3}}}{(0.098+5.6)^{-2}}
$$

Give your 2 nswer correct to 4 significant figures.
2. Pipes S and T can fill a tank in 2 hours and 3 hours respectively. Pipe U can empty the full tank in 4 hours. How long will it take to fill the tank with all the pipes running?
3. Make $d$ the subject in the given formula.

$$
\begin{equation*}
U=\frac{V d^{2}}{2 w+d^{2}} \tag{3mks}
\end{equation*}
$$

4. In the figure below, the tangents DC and BC meet at point C , angle $\mathrm{BCD}=50^{\circ}$ while angle $\mathrm{ABE}=70^{\circ}$


Calculate the sizes of angles
i) $<\mathrm{CBD}$
ii) $<\mathrm{CDE}$
5. Solve for x in the equation below.

$$
\begin{equation*}
\log _{x} 4+\log _{4} x=2 \tag{4mks}
\end{equation*}
$$

6. Solve the equation $3 \operatorname{Sin} \mathrm{x}=2 \operatorname{Cos}^{2} \mathrm{x}^{2}$ where $0^{0} \leq x \leq 360^{\circ}$
. In the diagram below, CD is a tangent to the circle at point D . If $\mathrm{BC}=7 \mathrm{~cm}$ and $C D=9 \mathrm{~cm}$, calculate the length of the chord $A B$.

7. Calculate the relative error in $7.9 \div 4.3$
8. Determine the semi-interquartile kange for the given set of data.
b) Use the expansion in(a)above to find the value of (0.9) ${ }^{8}$
11.Mrs. Ondiek invested Ksh63560 in a bank where the interest was compounded quarterly at the rate of $12 \%$ per month. Determine the amount of money she had after $21 / 2$ years.
9. Simplify without using mathematical tables or calculator.

$$
\frac{6}{\sqrt{7}+\sqrt{3}}-\frac{4}{\sqrt{7}-\sqrt{3}}
$$

3 . The figure below is a square -based pyramid with vertex V. Point O is the intersection of diagonals $\mathrm{AC}_{\vee}$ and $\mathrm{BC} . \mathrm{VA}=\mathrm{VB}=\mathrm{VC}=\mathrm{VD}=12 \mathrm{~cm}$ and $\mathrm{AB}=\mathrm{BC}=4 \mathrm{~cm}$.

a) Name the projection of line VA on plane ABCD.
b) Find the angle between line VB and the plane ABCD.
14. An equation of a curve is given $\mathrm{as}_{5} \times y^{2}=5 x^{3}-7 x^{2}+3 x+2$ Find the equation of the tangent to the curve at $x=1$
15. Find the equation of a circle whose diameter has the end points (-2,6) and 6,2)
16. The distance between two places $P\left(\theta^{0} S, 35^{\circ} E\right)$ and $\left(\theta^{0} S, 145^{\circ} W\right)$ on the earth via South Pole is 3240 nm . Find
a) the value of $\theta^{\circ}$.
b) the distance between P and Q along the parallel of latitude in nautical miles.

## SECTION II(50 MARKS)

## Answer only five questions in this section.

17. The table below shows incame tax rates.
Income p.a in $\mathrm{K} £$
1-3000
Rate \%
10
$3001-5400$ j̀ 15
$5401-9,000 e^{\varepsilon^{5}} \quad 20$
9001-13,500 25
$13,5 \theta \%^{5}$ and above 30
(Ggnes earns a monthly salary of Ksh. 20,000 per month, Her house allowance is
Ksh. 15000P.M. She is entitled to a personal relief of Ksh. 1260P.M. Her deductions are NHIF sh.960, cooperative loan sh. 3500 and service charge of Ksh. 400 per month.

Calculate
a) the taxable income.
b) the tax charged on Agnes earning.
c) the tax paid.
d) the net salary.
18. In the figure below, E is the midpoint of $\mathrm{BC}, \mathrm{AD}: \mathrm{DC}=3: 2$ and AE intersect with BD at F.

a) Given that $A B=\underset{\sim}{b}$ and $A C=\underset{\sim}{c}$, express in terms of $\underset{\sim}{b}$ and $\underset{\sim}{c}$
i) $A E$
ii) $B D$
b) If $B F=t B D$ and $A F=s A E$, where t and s are scalars, find the values of t and s .
c) What is the ratio in which F divides $A E$.
19. Using a ruler and a pair of compasses only.
a) Construct a $\triangle \mathrm{ABC}$ in wherich $\mathrm{AB}=7.4 \mathrm{~cm}, \mathrm{AC}=8.2 \mathrm{~cm}$ and $\angle \mathrm{BAC}=45^{\circ}$. (3mks)
b) On the same diagranf ${ }^{(t)}$ construct $\triangle \mathrm{ACD}$ such that D , and B are on the opposite sides of line $\mathrm{AC}^{\mathrm{D}}$ is equidistant from A and C and $\mathrm{BD}=8.5 \mathrm{~cm}$. Measure AD .
c) Draw locưs of Q which passes through C and is parallel to BD .
d) The iormal from C meets BD at N . Mark the points $\mathrm{M}_{1}$ and $\mathrm{M}_{2}$ on the locus of Q such that $\mathrm{M}_{1} \mathrm{~N}=\mathrm{M}_{2} \mathrm{~N}=4.1 \mathrm{~cm}$. Measure the lengths $\mathrm{M}_{1} \mathrm{M}_{2}$ and CN .
20.a) i) On the grid (graph paper) plotaind draw triangle ABC where $\mathrm{A}(4,3), \mathrm{B}(4,6)$ and $\mathrm{C}(7,6)$.

## GRID

ii) Triangle ABC is given a rotation of $+90^{0}$ about $(0,0)$ to map onto $\mathrm{A}^{\mathrm{I}} \mathrm{B}^{\mathrm{I}} \mathrm{C}^{1}$. Plot $\mathrm{A}^{\mathrm{I}} \mathrm{B}^{\mathrm{I}} \mathrm{C}^{\mathrm{I}}$ and state its co-ordinates.
iii) Triangle $A^{I} B^{I} C^{l}$ is transformed by the matrix $\left(\begin{array}{rr}-1 & 0 \\ 0 & -1\end{array}\right)$ to map onto $\mathrm{A}^{11} \mathrm{~B}^{11} \mathrm{C}^{11}$ Plot $\triangle \mathrm{A}^{11} \mathrm{~B}^{11} \mathrm{C}^{11}$ and state its co-ordinates.
b) $\mathrm{A}^{\text {II }}{ }^{\text {III }} \mathrm{C}^{I I}$ is further transformed by a reflection on the line $\mathrm{x}=0$ to map onto A $^{\text {III }}{ }^{\text {IIII }} \mathrm{C}^{\text {III }}$. Plot $\mathrm{A}^{\text {III }} \mathrm{B}^{\text {III }} \mathrm{C}^{\text {III }}$ What single transformation will map $\mathrm{A}^{111} \mathrm{~B}^{111} \mathrm{C}^{111}$ onto triangle ABC?
21. A particle P moves in a straight line so that its velocity $\mathrm{Vm} / \mathrm{s}$ at time t seconds where $t \geq 0$ is given by $\mathrm{V}=28+\mathrm{t}-2 \mathrm{t}^{2}$ Find
a) The time when B is instantaneously at rest.
b) The speed of P at the instant when the acceleration of P is zero. ( 2 mks )
c) Given that P passes through point O of the line when $\mathrm{t}=0$
i) Find the distance of P from O when P is instantaneously at rest.(3mks)
ii) Find the distance covered by the particle during the $3^{\text {rd }}$ second.
(3mks)
22. The table below shows the masses if kg of some form three students in a school.

| Mass | 20-29 | 30-39 | $4^{4} 9^{9} 49$ | 50-59 | 60-69 | 70-79 | 80-89 | 90-99 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 5 | $12$ | 15 | 28 | 8 | 4 | 6 | 2 |

a) i) State the niédian class.
(iii) Using an assumed mean of 54.5 , calculate the mean mass.
b) Calculate the standard deviation of the data, give your answer correct to 2 decimal places.
23. The probability that it will rain $\operatorname{offor}^{\circ} \mathrm{C}$ a certain morning is $\frac{1}{3}$. If it rains, the probability that Sagero misses the busis $\frac{3}{4}$. If it does not rain, the probability that he catches the bus is $\frac{5}{6}$.
a) Represent the above information in a tree diagram.
b) Calculate the probability that on a given morning
i) it rains and he catches the bus.
ii) it rains and he misses the bus.
iii) he misses the bus.
iv) it does not rain and he misses the bus.
24. A small scale farmer wishes to buyome sheep and goats for rearing. A sheep costs sh. 400 and a goat costs sh. $300_{c}$ erhe farmer has enough space for only 20 animals and may spend at most sh. 6800 The number of goats should not exceed twice the number of sheep.
a) By letting $x$ and $x y$ to represent the number of sheep and goats he can buy respectively, write down all inequalities from the above information.
b) Represent the inequalities on the grid provided.

## PASTE A GRID

c) From your graph; find the maximum number of animals he can buy at the lowest cost.

