NAME

## INDEX NO

$\qquad$
SCHOOL SIGN

DATE $\qquad$

121/2
MATHEMATICS ALT. A
PAPER 2
JULY/AUGUST 2012
TIME $2 ½$ HOURS

## MARAKKET WEST DISTRICT JOINT EVALUATION TEST2012(MAWESSE) Kenya National Examination Council (K.C.S.E)

## 12182

## MATHEMATICS ALT. A

## PAPER 2

JULY/AUGUST 2012
TIME $2 ½$ HOURS

## INSTRUCTIONS TO THE CANDIDATES

(a) Write your name and the index number in the spaces provided above.
(b) Sign and write the date of examination in the spaces provided.
(c) This paper consists of TWO sections: Section I and II.
(d) Answer ALL the questions in section I and only FIVE questions from section II.
(e) All answers and working must be written on the question paper in the spaces provided below each question.
(f) Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.
(g) Marks may be given for correct working even if the answer is wrong.
(h) Non-programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.

FOR EXAMINERS USE ONLY.

## SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

1. Use logarithms only to evaluate


#### Abstract

A shamba is in the shape of a parallelogram with the lengths of the adjacent sides being 12 cm and 15 cm . If the area of the parallelogram is $72 \mathrm{~cm}^{2}$, find the angle between these two sides.


3. Solve for t given that $28 \mathrm{~cm}(3 \mathrm{t})-100$ for $90^{\circ} \leq t \leq 360^{\circ}$
4. Make x the subject of the formula

$$
P=2 t \sqrt{\frac{x}{3 x-4}}
$$

5. In the figure below LM is a diameter of the circle and LMN is a straight line. The line PQR is a tangent to the circle at Q . Angle $\mathrm{NQR}=32^{\circ}$ and angle $\mathrm{QML}=50^{\circ}$.


Calculate
(a) angle MQN
(b) angle QNM
6. Expand $\left(1+\frac{3}{x}\right)^{5}$ upto the fifth term
7. Find the equation of the normat to the curve $y=2 x^{2}+3 x+4$ at $x=2$
8. $e^{4}$ Find the percentage error in calculating the volume of a sphere radius 4.9 cm .
9. Mama Jeru deposited sh. 1850 for 18 months at an interest rate of $16 \%$ p.a compounded half yearly.
How much interest did she pay at the end of the of the period?
10. Find the equation of the locus of all points equidistant from P and Q where $\mathrm{P}(6,9)$ and $\mathrm{Q}(0,-5)$
(3mks)
11. Simplify by rationaling the denominator leavifig your answer in surd form.

$$
\frac{1}{\sqrt{2}-1}-\frac{\sqrt{2}}{\sqrt{2}+1}
$$

The position vector of A and B are $\underset{\sim}{a}=4 j+4 j-6 k$ and $\underset{\sim}{b}=10 \mathrm{i}+4 \mathrm{j}+12 \mathrm{k}$. Dis a point on AB such that $\mathrm{AD}: \mathrm{DB}$ is $2: 1$.
Find the co-ordinates of D.
13. Find the area of the region enclosed by the curve $y=x-6$ and the line $x=-1$ and $x-2$.
(3mks)
14. In the fig. ABCDGH is a rectangular based weddge with $\mathrm{AD}=6 \mathrm{~cm}$ and $\mathrm{CD}=15 \mathrm{~cm}$. The midpoint of AD is N and $\mathrm{DG}=\mathrm{GA}=\mathrm{BH}=\mathrm{HC}=9 \mathrm{~cm}$. If $G \mathrm{H}=7 \mathrm{~cm}$, calculate the angle between planes ADG and the base ABCD.

15. Avariable $u$ is partly constant and partly as the square of $t$. When $t=2, u=0$ and when $t=1, u=3$. Find (a) the law connecting u and t .
(b) the value of u when $\mathrm{t}=\frac{1}{4}$
16. An equilateral triangle of sides 9 cm is completely enclosed in a circle of radius rcm.Find the least value of $r$.
(2mks)

## 

Answersonly five questions
17. A cattle dip is 150 cm wide and 12 m Fong. The depth of the water increases uniformly from a shallow end of 60 cm to a maximu $\mathrm{m}_{\mathrm{m}}^{\mathrm{h}}$ of 6 m .
(a) Find the volume of water that can be held by the full dip in litres
(b) If the dip is drained by a pipe of radius 15 cm at the rate of $6 \mathrm{~m} / 1$, how long will it take to drain a full dip?
18. R1 denotes reflection along line $x=14 . \mathrm{R} 2$ demetes reflection along line $x=2 . T$ denote translation vector $\left(\frac{-1}{2}\right)$

A triangle ABC has vertices $\mathrm{A}(6), 4), \mathrm{B}(3,4)$ and $\mathrm{C}(3,6)$
(a) Show the image $A^{1} B_{1}^{1} E^{G}$ under $R^{1}$
(b) Find and draw $A^{11} B^{11} C^{11}$ the image of $A^{1} B^{1} C^{1}$ under $R^{2}$.
(c) Find and draw $A^{41} \mathrm{~B}^{11} \mathrm{C}^{11}$ the image of $\mathrm{A}^{11} \mathrm{~B}^{11} \mathrm{C}^{11}$ under T .
(d) Describe a sijgle transformation which maps the object onto the final image.
19. The probability that a pupil goes to school $\operatorname{bef}^{2 y^{-5^{\circ}}}$ a boda-boda is $\frac{2}{3}$ and by a matatu is $1 / 4$. If he uses a boda-boda the probability that he is late to school is $\frac{2}{5}$ and if he uses a matatu the probability of being late is $\frac{3}{10}$. If he use other means of transport the probability of being late is $\frac{3}{20}$.
(a) Draw a tree diagzam to represent this information.
(b) Find the probability that he will be late for school.
(c) Find the probability that he will be late for school if he does not use a matatu.
(d) What is the probability that the will not be late to school
20. (a) Fill the table below and use it to drawithe graph of $\mathrm{y}=2 \cos \left(\theta-30^{\circ}\right)$ for $0^{\circ} \leq \theta \leq 360^{\circ}$.

| $\theta$ | $0^{0}$ | $30^{0}$ | $60^{0}$ | $90^{\circ}$ | 1280 | 150 | $180^{0}$ | $210^{0}$ | $240^{\circ}$ | $270{ }^{0}$ | $300^{\circ}$ | $330^{0}$ | $360{ }^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \theta-30^{0} \\ & \operatorname{Cos}\left(\theta-30^{\circ}\right) \\ & \mathrm{y}=2 \cos (\theta-30) \end{aligned}$ |  | 1 | $30^{\circ}$ | $55^{+e^{\text {x }}}$ |  | $\begin{aligned} & 120^{0} \\ & -0.5 \end{aligned}$ | - | -1 | $\begin{aligned} & 210^{0} \\ & -1.732 \end{aligned}$ |  | $\begin{aligned} & 270^{0} \\ & 0 \\ & 0 \end{aligned}$ | 1 | $330^{\circ}$ |

(b) State the amplitưde and period of the graph
(c) Use yequr graph to solve the equation $\cos \left(\theta-30^{\circ}\right)=0.25$
21. A plane flies from airport $\mathrm{x}\left(60^{\circ} \mathrm{S}, 30^{\circ} \mathrm{E}\right)$ due arorth to airport $\mathrm{Y} \cdot\left(30^{\circ} \mathrm{N}, 30^{\circ} \mathrm{E}\right)$ at 180 knots.
 the same speed.

## (a) (i) Calculate the total disfance covered by the plane in nautical miles

(ii) Calculate the total time taken to complete the journey from X through Y to Z .
(4mks)
(b) From a certain latitude a plane is first visible over the north pole. The plane is flying at a height of 800 km above the North Pole, calculate the latitude angle
(2mks) ( $\mathrm{R}=6370 \mathrm{~km}$ )
23. Without using a et square or a protractor
(a) Construct a horizontal line $\mathrm{AB}, 6 \mathrm{c} \mathrm{a}^{\circ}{ }^{\circ}$ long and triangle ABC such that $\angle \mathrm{ABX}=30^{\circ}$ and line $\mathrm{AB}=10 \mathrm{~cm}$.
(b) $e^{\rho^{\sigma^{5}}}$ Construct a perpendicular from a to meet BC produced at N .

Measure CN.
(c) Construct triangle $A^{I} B C$ such that the area of triangle $A^{1} B C$ is three quarters of triangle $A B C$ and $A^{1}$ is on the same side of $B C$ as $A$ and lies on $A B$.measure $A^{1} B$.
(4mks)
23. The marks obtained by 50 candidates in an examination were recorded as shown

| Marks | $0-9$ | $10-19$ | $20-29{ }_{5}{ }^{2}$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No of <br> candidates | 4 | 10 | $12 e^{2}$ <br> $\mathrm{c}^{2}$ | 9 | 8 | 5 | 2 |

Draw a cumulative frequency curve hence use your graph to estimate
(a) the median
(b) the quartile derviation
(c) the percentage of candidate failing if 25 marks is the pass mark
(d) the range of marks scored by the middle $60 \%$ of he candidates
24. (a) Claire earns sh. 15,900 p.m and gets attax relief of sh.7,200 p.a.How much should she pay as income tax p.m if taxation rates aैंe as shown below.

| Income (KE)p.a | Rate 9Ksh(per k£) |
| :---: | :---: |
| 1-4512 ${ }^{4}{ }^{\text {c }}$ | 2 |
| 4513-9024 | 3 |
| 9025-13536 | 4 |
| 13537 and abover | 5 |

(4mks)
(b) Mr.Mutuku earns sh.15,500 p.m .He is housed by his employer and pay a rent of sh. 1200 per month for taxation purposes his taxable income is raised by 155.If he gets tax relief of sh. 720 per month calculate his P.A.Y.E
(6mks)

