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121/2
MATHEMATICS
PAPER 2
JULY / AUGUST 2014
TIME: 2½ HOURS

# NANDI NORTH SUB-COUNTY JOINT EVALUATION 2014 

Kenya Certificate of Secondary Education (KCSE) MATHEMATICS
PAPER 2
TIME: 2½ HOURS

## INSTRUCTIONS TO CANDIDATES

a) Write your Name and Index Number in the spaces provided at the top of this page.
b) Sign and write the date of examination in the spaces provided above.
c) This paper contains TWO sections: section I and section II
d) Answer all the questions in section I and any FIVE questions from section II.
e) All answers and working must be written on the question paper in the spaces provided below each question.
f) Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.
g) Marks may be given for correct working even if the answer is wrong.
h) Non-programmable silent electronic calculators and KNEC mathematical tables may be used except where stated otherwise.

FOR EXAMINER'S USE ONLY:

## Section I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Section II

GRAND TOTAL

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |



# Answer ALL QGestions in this section 

1. Use logarithm table to evaluate: $\alpha^{5}$
(4mks)

2. What must be added to $1 / 4 x^{2}+\frac{1}{9}$ in order to make it a perfect square?
(2mks)
3. Expand $\left(x-a / x^{2}\right)^{6}$ in ascending powers of $x$, up to the term independent of $x$. If this independent term is 1215 , find the value of $a$.
4. An angle of 1.75 radians at the centre of a circle subtends an arc of length 24.8 cm . Find the diameter of the circle.
5. $A B C D E F G$ is a rectangular box in which $A B, A D, A E$ are $3 \mathrm{~cm}, 4 \mathrm{~cm}$ and 5 cm long respectively. M is the midpoint of $\mathrm{F}_{\mathrm{F}} \mathrm{G}$.


Find the length $A M$ and determine the inclination of $A M$ to EFGH.
6. Use square roots, reciprocals and square tables to evaluate the expression: (3mks) $(0.00546667)^{1 / 2}+\left(\frac{3}{0.043279}\right)^{2}$
7. A member of a county assembly sold his car for shs. 1,250,000 and deposited this money in a savings account in one of the banks in Kaiboi town. The banks paid $18 \%$ p.a compounded quarterly. After two years, the member of the county assembly withdrew a half of the amount from the account. He left the rest for a further two and a half years. Calculate the total interest he earned in the $41 / 2$ year period. ( 4 mks )
8. Given that $x^{0}$ is an angle in the third quadrant such that $16 \sin ^{2} x^{0}+4 \cos x^{0}=10$. Find $\tan \mathrm{x}$.
9. Two ${ }^{\chi}$ variables $P$ and $L$ are such that $P$ varies partly as $L$ and partly varies inversely as the square root of $L$.
${ }^{5}(a)$ Determine the relationship between $P$ and $L$ given that $L=16$ when $P=500$ and $L=25$ when $P=800$.
(b) Hence find $P$ when $L=81$.
10. The angle of elevation from the base of a wall to the top of the flag post 70 metres away is 62 . The angle of depression from the top of the flag post to the wall is $25^{\circ}$.
Calculate:-
(a) The height of the flag post.
(b) The height of the wall.
11. Given that $\log 3=1.583$ and $\log 5=2.322$, evaluate without using table or calculator:
12. Two values of $\mathbf{a}$ and $\mathbf{b}$ are such that $7.1 \leq 7.3$ and $12.5 \leq b \leq 12.7$. Calculate the pereéntage error in b, giving your answer correct to 2 decimal places.
13. The following figure is a solid and its incomplete net.
(a) Complete and label the net.

(b) Hence or otherwise, find the surface area of the solid.
14. Solve for $x$ in the equation: $9^{x+1}-54=3^{2 x+1}$
15. तf ${ }^{2}$ e points $P(-6,5)$ and $Q(2,-1)$ are the ends of a diameter of a circle centre $M$. ©Determine:-
(a) The coordinates of $M$.
(b) The equation of the circle in the form $x^{2}+y^{2}+a x+b y+c=0$.
16. Solve the simultaneous equations:

$$
\begin{aligned}
& y+2 x+1=0 \\
& x^{2}+x y=-6
\end{aligned}
$$

## Answer ONLY FIVE questions din this section in the spaces provided

17. Mr. Maiyo, who works in a sugaficane plantation, owns a bicycle which he sometimes rides to work. Out of the $21, w^{2}$ orking days in a month, he rides to work for 18 days. If he rides to work, the probatbility that he is bitten by a rabid dog is $4 / 15$ otherwise it is only $1 / 13$. When he is bitten by the dog, the probability that he will get treated is $4 / 5$ and if he does not get treated, the probability that he will get rabies is $\frac{5}{7}$.
(a) Draw a tree chlăagram using the given information.
(b) Using the tree diagram in (a) above, determine the probability that;
(i) Maiyo will not be bitten by a rabid dog.
(ii) He will get rabies.
(iii) He will not get rabies.
18. Tax rates in operation in a certain year in Kenya are as given in the table below.

| Income | Tax Rates |
| :---: | :---: |
| (kf p.a.) $2^{\text {c }}$ | (sh. Per £) |
| 1-4,512 | 2 |
| 4,5130 9,024 | 3 |
| 9,025-13,536 | 4 |
| 13,537-18,048 | 5 |
| \% ${ }^{\chi} 18,049-22,560$ | 6 |
| j> ${ }^{\text {s }}$ ( Over 22,560 | 6.5 |

(a) Mr. $A^{e^{y_{0}}} \mathrm{oech}$ pays Ksh. 2,172 P.A.Y.E. monthly. He was entitled to a house adlowance of Ksh. 5,000 and a medical allowance of Ksh. 2,000 and gets a , ${ }^{2}$ monthly tax relief of Ksh. 1,093. Calculate his monthly basic salary.
(b) Mr. Koech's other deduction per month were as follows:-

NHIF - Kshs. 320
Co-op Loan - Kshs. 4,000
Calculate Koech's net pay per month.
(2mks)
19. Using a ruler and a pair of compasses oaly:
(a) Three points $A, B$ and $C$ are vertices of a triangle $A B C$ such that $A B=8 \mathrm{~cm}, B C=$ 5 cm and $A C=6.4 \mathrm{~cm}$. Draw tyiangle $A B C$ with $A B$ as the base.
(b) Construct the locus of $P$ serch that it is equidistance from the sides $A B, B C$ and AC.
(c) On the opposite side point $C$ on $A B$, construct the locus $L$ such $\angle A L B=60^{\circ}$.
(d) Hence determine the area of the major sector bounded by the locus L.
20. (a) Complete the table below for the functions $y=4 \operatorname{Cos} 2 x$ and $y=3 \operatorname{Sin}\left(2 x+30^{\circ}\right)$ giving the values to 1 decimal place. $0^{\circ}$ ( 2 mks )

|  | $-30^{0}$ | $0^{0}$ | $30^{\circ}$ | $60^{\circ}$ | $90^{\circ}$ | $120^{\circ}$ | $150^{\circ}$ | $180^{\circ}$ | $210^{\circ}$ | $240^{\circ}$ | $270^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $4 \operatorname{Cos} 2 \mathrm{x}$ | 2.0 | 4.0 | $2)^{\circ}$ |  | -4.0 | -2.0 |  | 4.0 | 2.0 |  | -4.0 |
| $3 \mathrm{Sin}\left(x+30^{\circ}\right)$ | 0.0 | $1.5{ }^{\text {e }}$ | 2.6 | 3.6 |  | 1.5 | 0 |  | -2.6 |  | -2.6 |

(b) Draw the graphsiff $y=4 \operatorname{Cos} 2 x^{\circ}$ and $y=3 \operatorname{Sin}\left(x+30^{\circ}\right)$ for $-30 \leq x \leq 270^{\circ}$ on the same axes. Use

(c) Use your graphs in (b) above to solve the equation:
(i) $3 \operatorname{Sin}\left(x+30^{\circ}\right)-4 \operatorname{Cos} 2 x=0$.
(ii) $3 \operatorname{Sin}\left(2 x+30^{\circ}\right)+1=0$
(d) Determine the period of the function $\mathrm{y}=4 \operatorname{Cos} 2 \mathrm{x}$.
21. An aircraft takes off from the airport $\mathrm{X}\left(65^{\circ} \mathrm{N}, 36^{\circ} \mathrm{E}\right)$ and flies by the most direct route to another airport $Y\left(R^{0} N, 144^{\circ} \mathrm{W}\right)$ covéring a distance of 4800 nm .
(a) Find $\mathrm{R}^{0}$

(b) If instead, the aircraft had flown along the meridian $144^{\circ} \mathrm{W}$ to point Y , find how mucbrfurther it would have flown.
(c) Two aircrafts takes off from X to Y at the same time. Given that both fly at the same speed and one flies on the direct route and the other takes the route described in (b) above, state the position of the second aircraft when the first is landing at Y .
22. The diagram shown below represents the area between the curves $y=x^{2}+2$ and $y=$ $10-x^{2}$ and $y$-axis.


Find:-
(a) Ere coordinates of $Q$ (a point of intersection)
(b) The area of the shaded region, by use of mid-ordinate rule with 8 ordinates( 6 mks )
(c) Use integration method to calculate the same area as in (b) above.
23. Two quantities of $p$ and $r$ are given below:

| $P$ | 1.2 | 1.5 | 2.0 | 25 | 3.5 | 4.5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $r$ | 1.58 | 2.25 | 3.39 | $e^{2} .4 .74$ | 7.86 | 11.5 |

(a) State the linear equatiod $c^{c^{s}}$ connecting $p$ and $r$.
(b) Using the scalle 2 cm to represent 0.1 units on both axes, draw a suitable straight line graph on the grid provided;


Hence estimate the value of $k$ and $n$.
(c) Write an equation connecting p and n .
24. An aircraft leaves point $A$ and flies on abearing of $020^{\circ}$ to a second point $B$, which is 600 km from $A$. From $B$, the aircraft the flies on a bearing of $320^{\circ}$ to a third point $C$ which is 1000 km from $B$. The aircraft then flies directly back to $A$ from $C$ at a speed of $200 \mathrm{~km} / \mathrm{hr}$. By scale drawingefind:-
(a) Time taken to fly directly ${ }^{\text {from }} \mathrm{C}$ to A .
(b) The bearing in which it would fly from $C$ to $A$.
(c) Locate point $D$ on a bearing $170^{\circ}$ from $C$ and $280^{\circ}$ from $A$. Calculate $B D$ in kilometers.
(d) What is the bearing of $D$ from $B$ ?

