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121/2
MATHEMATICS
PAPER 2
JULY/AUGUST 2014
TIME: $\mathbf{2}^{1 ⁄}$ ² HOURS

Date: $\qquad$

## NYAMIRA SUB-COUNTY JOINT EVALUATION EXAM

## Kenya Certificate of Secondary Education (K.C.S.E)

121/2
Mathematics
Paper 2
$21 / 2$ hours

## INSTRUCTIONS TO THE CANDIDATES

- Write your name and index number in the spaces provided above
- This paper contains two sections; Section 1 and Section 11.
- Answer all the questions in section 1 and only five questions from Section 11
- All workings and answers must be written on the question paper in the spaces provided below each question.
- Marks may be given for correct working even if the answer is wrong.
- Non programmable silent electronic calculators and KNEC Mathematical tables may be used EXCEPT where stated otherwise
- Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.


## FOR EXAMINERS'S USE ONLY

## Section 1

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Section 1I

| Question | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |  |

GRAND TOTAL


This paper consists of 15 printed pages. Candidates should check carefully to ascertain that all the pages are printed as indicated and no questions are missing.

## SECTEON I (50 MARKS ).

## Answer All Questigins from this section in the spaces provided

1. Without using a calculator or mathematical table evaluate

$$
\frac{1}{3} o f\left(2 \frac{3}{4}-5 \cdot \frac{1}{-6} \times \frac{1}{2}\right) \times 3 \frac{6}{7} \div \frac{9}{4}
$$

2. The interior angle of a regular polygon is 1620 . determine the sum of all interior angles of the polygon
3. Simplify $\frac{2 x-2}{6 x^{2}-x-12} \div \frac{x-1}{2 x-3}$
4. Mogaka invested Ksh. 32,000 in a bank compounded quarterly at a rate of $20 \%$ p.a. another person invested sh. 40,000 compounded semi-annđally at a rate of $12 \%$ p.a. after how long will the amount be equal for both of them. Leave youraniswer to one decimal place
5. The figure below $\angle \mathrm{A}=62^{\circ}, \angle \mathrm{B}=40^{\circ}, \mathrm{BC}=8.4 \mathrm{~cm}$ and CN is the bisector of $\angle \mathrm{ACB}$


Calculate the length of CN to 1 decimal place
6. Make $x$ the subject of the formula
$v=m \sqrt{\frac{a-x}{x}}$
7. Expand $\left(\left(1-\frac{3}{2} x\right)^{6}\right.$ up to the term in $x^{3}$. Hencerice use the expansion to evaluate $(1.03)^{6}$
8. In the figure below ABCD is a cyclic quadrilateral and BD is a diagonal. EADF is a straight line. $\angle \mathrm{CD}$. $=68^{\circ} \angle \mathrm{BDC}=45^{\circ}$ and $\angle \mathrm{BAE}=98^{\circ}$


Calculate the size of
(a) $\angle \mathrm{ABD}$
(b) $\angle \mathrm{CBD}$
9. The first, the third and the seventh term of an increasing arithmetic progression are three consecutive terms of a geometric progression. If the first term of the arithmetic progression is 10 , find the common difference of the arithmetic progression
10. Simplify $\frac{3-\sqrt{7}}{3+\sqrt{7}}-\frac{\sqrt{7}}{3-\sqrt{7}}$ leaving your ansever in the form $a+b \sqrt{7}$ where a and b are constants
11. Findsthe values of x in the equation

$$
e^{e^{e^{e}}} \frac{243 x 3^{2 x}}{729 x 3^{x} \div 3^{(2 x-1)}}=81
$$

12. Form the three inequalities that satisfy the given region R


13 Find without using mathematical tables or a calculator the value of $x$ which satisfy the equation

$$
\log _{2}\left(x^{2}-9\right)=3 \log _{2} 2+1
$$

14. The cosst of 2 brands of coffee A and B per kilogram are 59.40 and $\operatorname{Sh} .72$ respectively. The two brafids are mixed in the ratio $x: y$ and sold at a profit of $20 \%$ above the cost. If the selling price per dilogram mixture is Ksh.72. find the value of $x$ and $y$
15. The figure below represents a rectangular based pyramid $\mathrm{VABCD} . \mathrm{AB}=12 \mathrm{~cm}$ and $\mathrm{AD}=16 \mathrm{~cm}$. Point O vertically below V and $\mathrm{VA}=\mathrm{VC}=\mathrm{VB}=\mathrm{VD}=26 \mathrm{~cm}$


Calculate the angle between edge VD and the base ABCD
16. Exchange rates in a commercial bank were given as follows

|  | Buying | Selling |
| :---: | :---: | :---: |
| 1 US dollar | Ksh. 73 | Ksh. 75 |
| 2 sterling pound | Ksh. $123^{8}$ | Ksh. 126 |

Bosibori arrived from the US with 6300US dollars and exchanged the amount for Kenya shillings. She spent Ksh. $146,00^{\circ} 0$. She converted the rest of the monies into sterling pounds. Determine the amount he had in'sterling pounds. Leave your answer to the nearest hundreds (3mks)

## SECTION Be 50 MARKS)

Answer any five questions from the section in the spaces.
17. The table below shows the distribution 0 of marks of 40 candidates in a test

| Marks | $1-10$ | $11-20$ | $21-41-50$ | $31-40$ | $41-50$ | $51-60$ | $61-70$ | $71-80$ | $81-90$ | $91-100$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 2 | 2 |  |  |  |  |  |  |  |  |

(a)(i) Find the valae of $x$
(1mk)
(ii) State the modal class
(b)(i) Calculate the mediun
(ii) Using an assumed mean of 55.5 and $d=\frac{x-A}{10}$ find the actual mean
(c) Calculate the standard deviation
18. In the figure below $A$ and $B$ are centres of cireles. $P Q=12 \mathrm{~cm}$ is an internal tangent, $A B=15 \mathrm{~cm}$ and the ratio of the radii is $2: 3$. Calculate
(a) The radii of the circles
(b) AT and TQ
19. Using mid-ordinates rules, estimate the areadit ${ }^{t^{5}}$. and $\mathrm{x}=8$ and x -axis
(b)(i) Uséintergration to determine the exact area under the curve
(ii) Find the percentage error in calculating the area using the mid-ordinate rules
(2mks)
20. Two variables qualities $x$ and $y$ are believed follow the rule $y=m x+n x^{2}$. The following table gives their corresponding values in an experiment.

| x | 1 | 2 |  | ${ }_{2} \mathrm{c}_{5} \mathrm{c}^{\text {e }}$ | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 6 | 8 |  | 6 | 0 | -10 | -24 | -42 | -64 |

(a) Use the given table and suitable straight line graph to find the value of the constants $m$ and $n$

(b) Use the graph to find the law connecting x and y
© Hence calculate the value of $y$ when $x=31 / 2$
21. A cinema has seats for 400 people. The seatseare in two catergories; $A$ and $B$ which are charged at Sh. 200 and Sh. 500 per show respectively $\mathrm{y}_{5}$ The number of catergory B booked per show does not exceed that of catergory A. for the haleex expenses to be covered, atleast 70 category B seats must be booked and they must be more than quarter of the total number of seats booked.
(a) Write down inequalities other than $><\geq 0$ and $y \geq 0$ to represent the conditions satisfied by the seats per show

## (b) Represent the ${ }^{5}$ se inequalities on a graph

(c) If the hall is charged at sh. 45000 per day and the operator runs 3 shows per day, find the maximum possible profit in a day
22. A plane leaves $\mathrm{P}\left(75^{\circ} \mathrm{N}, 30^{\circ} \mathrm{E}\right)$ and follows a lo ingitude via the north pole flying at 300 knots to Q it takes 10 hrs to reach point Q
(a) Calculate
(i) The distance covered by the plane in nautical miles
(ii) Whie position of Q
(b) After spending 2 ours at Q , it then flies westwards to T which is 1360 km west of Q , find
(i) the longitude of T (using $\mathrm{R}=6370 \mathrm{~km}$ ) to the nearest degree
(ii) The local time at T when the local at T which the local time at Q is 5.30 pm
23. (a) A triangular garden ABC is such that $\mathrm{AB} 8 \mathrm{~cm} \angle \mathrm{BAC}=45 \mathrm{o}$ and $\angle \mathrm{ABC}=75 \mathrm{o}$. Using an appropriate scale draw the garden using azruler and a pair of compasses only
(b) A water taper ${ }^{2}$ is to be mounted in the garden that it is equal in distance from $A, B$ and $C$. on the diagram in (a) above show the position of P
(c) A section of the plot is enclosed such that a region R is formed under the following conditions
(i) $\mathrm{CR} \geq 1.5 \mathrm{~cm}$
(ii) $R$ is more than $2 m$ from line $A B$
(iii) $R$ is nearer to $C B$ than $C A$. shade the region $R$
24. In the triangle OAB below $\mathrm{OA}=\underset{\sim}{\mathrm{a}} \mathrm{OB}=\underset{\sim}{b}$ and $\theta^{\circ} \overbrace{}^{5^{5^{\circ}}}=3 / 2 \mathrm{OA}$. M divides OB in the ratio 3:2

(a) Express in terms of $a$ and $b$ the vectors
(i) AB
(ii) MC
(b) Given that $\mathrm{MN}=\mathrm{hMC}$ and $\mathrm{BN}=\mathrm{kBA}$, express vector MN in two different ways and hence find the values of $h$ and $k$
(6mks)
(c) Show that the points M,N and Care collinear

