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Index No. $\qquad$ Signature $\qquad$
121/1
Mathematics Paper 1
June Exams
Form 4
$21 / 2$ Hours
Term 2, 2017

## SACHO HIGH SCHOOL Kenya Certificate of Secondary Education (K.C.S.E)

## INSTRUCTIONS TO CANDIDATES

$>\quad$ Write your name and Admission number in the spaces providedat the top of this page.
$>\quad$ This paper consists of two sections: Section I and Section II.
$>$ Answer $\boldsymbol{A L L}$ questions from section I and ANY FIVE from section II
$>\quad$ All answers and workings must be written on the question paper in the spaces provided below each question.
$>\quad$ Show all the steps in your calculation, giving your answer at each stage in the spaces below each question.
$>\quad$ Non - Programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.

## FOR EXAMINERS USE ONLY

## SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

GRAND TOTAL


## SECTION I

## (Answer all the questions in the spaces provided)

1. Evaluate $\frac{8 \frac{1}{8}-2 \frac{1}{2}}{5 \frac{3}{20}-1 \frac{1}{6} \text { of } 1 \frac{1}{5}}$
(3mks)
2. A bus service number 4 leaves a terminus every 15 minutes. Services 8 and 3 leaves after every 20 and 30 minutes respectively. If all the three services leave together at 6.00 am , what is the earliest time the three buses will leave together again?
3. Use tables of reciprocals and square roots to evaluate.
$\sqrt{\frac{2}{0.5893}+\frac{1.06}{846.3}}$
4. A Line passes through $A(1,1)$ and $B(x, y)$. The mid-point of $A B$ is $(3,5)$. If line $B C$ is perpendicular to $A B$, find the equation of line $B C$.
5. Solve for the equation $\left(\frac{27}{8}\right)^{x+7}-\left(\frac{4}{9}\right)^{-3 x}=0$
6. Elvis exchanged Ksh.600, 000 to Sterling pounds. After settling the bills worth $£ 1200$, he changed the balance to Euros. He then purchased goods worthy 200 Euros. Using the exchange rates below, calculate hisbalance in Kenyan shillings.

Buying (Ksh) Selling (Ksh)
1 Sterling pound $114.20 \quad 114.50$
1 Euro $101.20 \quad 101.30$
7. Find the mass of a wooden beam 4 m long, 25 cm wide and 18 cm deep if the density of the wood is $625 \mathrm{~kg} / \mathrm{m}^{3}$.
8. Solve the inequality below hence represent the solution in a number line

$$
3+2 x<3 x-1 \leq 2 x+7
$$

9. In the diagram below ABE is a tangent to a circle at B and DCE is a straight line. If $\angle \mathrm{ABD}=60^{\circ}, \angle \mathrm{BOC}=80^{\circ}$ and O is the centrie of the circle.


Find the value of $<\mathrm{BEC}$ and give reasons.
10. The marks obtaine by 10 pupils were $15,14,12,13,9,16,11,12,13$ and 17 . Calculate the standard deviation correct to 4 s.f.
11. Each exterior angle of a regular polygon is a fifth of the interior angle.
a) Find the size of the exterior angle
b) Find the number of sides of the polygon
12. The figure below shows a solid prism:-


Sketch the net of the prism above and show with arrows the path ACDB and F via E
14. Solve for $y$ in the equation.
15. The angle of elevation of the top of a flag post from apoint $x$ on level ground is $13^{\circ}$. The angle of elevation of the top of the flag post from another point $y$ nearer the flag post and 120 metres from x is $30^{\circ}$. Y is between A and the bottom of the flag post and the three points are collinear. Find the height of the flag post.
16. Simplify the expression $\frac{x-1}{x}-\frac{2 x-1}{3 x}$. Hence solve the equation $\frac{x-1}{x}-\frac{2 x-1}{3 x}=\frac{2}{5}$

## SECTION II

## (Answer ANY FIVE questions in the spaces provided)

17. Town $B$ is $20 \mathrm{~km} N 60^{\circ} \mathrm{W}$ from village $A$. Town $B$ is $25 \mathrm{~km} 040^{\circ}$ from town C. Village $D$ is due East of town C and dues South of village A
(a) Using a scale 1:500,000 draw a diagram showing a relative position of town $B$, town C, village A and village D
(b) Determine;
(i) Distance between village A and town C
(ii) Distance between tewn C and village D
(iii)Compass bearing of town C from village A
(iv)Compass bearing of village $D$ from town $B$
(c)Determine the area enclosed by the diagram in (a) above in hectares
18. John bought 3 brands of tea A, B and C. The cost price of the three brands were sh. 25 , sh. 30 and sh. 45 per kilogram respectively. He mixed the three brands in the ration 5:2:1 respectively. After selling the mixture he made a profit of $20 \%$.
a) How much profit did he make per kilogram of the mixture?
b) After one year the cost price of each brand was increased by $12 \%$ ?
i) How much did he sell one kilogram of the mixture to make $20 \%$ profit? Give your answer to the nearest 5cents.
iii) What would have been the percentage profit if he sold one kilogram of the mixture at Ksh.40.25.
19. The distance $S$ meters from a fixed point $O$, covered by a particle after $t$ seconds $B$ given by the equation $S=t^{3}-6 t^{2}+9 t+5$
(a) Calculate the gradient of the curve at $\mathrm{t}=0.5$ seconds
(b) Determine the values of S at the turning points of the curve
(c) Sketch the curve in the space provided.
20. The figure below shows a frustrum made from a right pyramid, such that $A B=D C=16 \mathrm{~cm}$, $\mathrm{BC}=\mathrm{AD}=10 \mathrm{~cm}, \mathrm{FG}=\mathrm{EH}=18 \mathrm{~cm}, \mathrm{GH}=\mathrm{FE}=7.5 \mathrm{~cm}, \mathrm{CH}=\mathrm{BG}=\mathrm{AF}=\mathrm{DE}=15 \mathrm{~cm}$. If the altitude of the frustrum is 14.6 cm , find:

(a)The altitude of the pyramid made from the frustrum.
(b) The surface area of the frustrum.
(c)The volume of the frustrum.
21. Alex and James live in two towns 240 km apart. One day at 9.45 am , Alex left his town and drove towards James' town at an average speed of $60 \mathrm{~km} / \mathrm{h}$. James left his town at $10.50 \mathrm{a} . \mathrm{m}$. on the same day and drove towards Alex's town at an average speed of $80 \mathrm{~km} / \mathrm{h}$. Determine
(a) the distance form Alex's town where the two met.
(b) the time of day they met
22. The figure below is a triangle OAB where $\mathrm{OA}=\mathbf{a}$ and $\mathrm{OB}=\mathbf{b}$. A point R divides AB in the ratio 2: 5 and a point T divides OB in the ratio 1:3. OR and AT intersect at D .

(a)Find in terms of $\mathbf{a}$ and $\mathbf{b}$.
(i) BT.
(ii) $\mathbf{O R}$
(iii)AT
(b) Given that $\mathbf{A D}=k \mathbf{A T}$ and $\mathbf{R D}=h \mathbf{R O}$ where $k$ and $h$ are scalars. Find the values of $k$ and $h$. Hence express AD in term of $\mathbf{a}$ and $\mathbf{b}$.
23. (a) The members of a photography club decided to buy a camera worth Ksh 4000 by each one contributing the same amount of money. Fifteen members fail to pay their contribution and as a result each of the other members has to pay Ksh 60 more. Find the number of members in the club.
(b) What is the percentage increase in the contribution per member?
24. (a) Complete the table below for the functions $y=3 \sin x$ and $y=2 \cos x$. (2mks)

| $x$ | $0^{c}$ | $\frac{\pi^{c}}{6}$ | $\frac{\pi^{c}}{3}$ | $\frac{\pi^{c}}{2}$ | $\frac{2 \pi^{c}}{3}$ | $\frac{5 \pi^{c}}{6}$ | $\pi^{c}$ | $\frac{7 \pi^{c}}{6}$ | $\frac{4 \pi^{c}}{3}$ | $\frac{3 \pi^{c}}{2}$ | $\frac{5 \pi^{c}}{3}$ | $\frac{11 \pi^{c}}{6}$ | $2 \pi^{c}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $3 \sin x$ |  |  | 2.6 | 3 |  |  | 0 | -1.5 | -2.6 | -3 |  | -1.5 |  |
| $2 \cos x$ |  | 1.7 | 1.0 |  |  | -1.7 | -2 | -1.0 |  |  | 1.0 | 1.7 | 2 |

(b) Using a scale of 2 cm to represent 1 unit on the y - axis and 1 cm to present $30^{\circ}$ on the x -axis ,draw the graphs of $\mathrm{y}=3 \sin \mathrm{x}$ and $\mathrm{y}=2 \cos \mathrm{x}$ on the same axes on the grid provided.

(c) From your graphs:
(i) State the amplitude of $y=3 \sin x$.
(ii) Find the values of x for which $3 \sin x-2 \cos x=0$.
(iii) Find the range of values of $\mathbf{x}$ for which $3 \sin \mathbf{x} \geq 2 \cos \mathbf{x}$

