NAME:
INDEX NO: $\qquad$
SCHOOL
Date: $\qquad$
Candidate's signature: $\qquad$
121/2
MATHEMATICS
Paper 2
July/August 2017
Time: $2^{1 ⁄ 2}$ Hours

## SCHOOL BASED FORM 4 EXAM JULY-AUGUST 2017

Kenya Certificate of Secondary Education (K.C.S.E) MATHEMATICS
Paper 2
July/August 2017
Time : $21 / 2$ Hours

## INSTRUCTIONS TO CANDIDATES

(a) Write your NAME and INDEX number in the spaces provided above.
(b) Write the DATE of examination in the spaces provided above.
(c) This paper consists of TWO sections. Section I and Seefion II.
(d) Answer ALL the questions in section I and only FIVE questions from Section II
(e) All answers and working must be written on the qुuestion paper in the spaces provided below each question.
(f) Show ALL the steps in your calculations, giving your answers at each stage in the spaces below each question.
(g) Marks may be given for correct wofking even if the answer is wrong.
(h) Non- programmable silent electronnic calculators and KNEC mathematical tables may be used except where stated otherwise.
(i) Candidates should check the question paper to ascertain that all the papers are printed as indicated and that no questions are chissing.

## FOR EXAMINER'S USE ONLY

## SECTION 1

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

## GRAND TOTAL

## SECTION A (50 MARKS)

## ALL QUESTIONS IN THIS SECTION

1. If $A=2.3, B=8.7$ and $C=2.0$. Find the percentage error in $\frac{A+B}{C}$
2. Simplify $\frac{2 \sqrt{5}}{\sqrt{3-\sqrt{5}}}$ leaving the answer in the form $\mathrm{a}+\mathrm{b} \sqrt{c}$, where $\mathrm{a}, \mathrm{b}$ and c arefational numbers. ( 2 mks )
3. Starting from seven minutes tQ noon the minutes hands of a clock moved so that the clock is showing 27 minutes to one.
(a) Find the angle through which the minute hand moved.
(b) Given that the minute hand is 6.37 cm long. Find the length of the arc it describes in that time.
4. In the figure below TA and TB are tangents to the circle centre O . Given that $\angle \mathrm{ATB}=20^{\circ}$. Find $\angle \mathrm{PAT}$.

( 3 mks )
5. In a school the form three students are 90 . The ratio of boys to girls is $7: 2$. Find the number of girls required to join the existing class so that the ratio of boys to girls is 5:4.
(3 mks)
6. A wire 180 cm long was used to make a model of a triangular-based prism. The cross-section has side of length 10 cm each. Calculate the volume of the resulting prism.
7. Find the value of $x$ given that $\log _{2}\left(x^{2}-2\right)-\log _{2}(\sqrt[1]{2} x+5)-1=0$
8. Write down the first four terms of the expression of $(2-1 / 4 \mathrm{x})^{9}$ in ascending powers of x giving your answer in simplest forms. Hence find the value of $(1.975)^{8}$ to the nearest 3 d.p.
9. Determine the centre and the radius of the circle given by equation.

$$
x^{2}+y^{2}-6 x+4 y-12=0
$$

10. (a) Draw line $\mathrm{MN}=7 \mathrm{~cm}$ and shinw the locus of a point P which is such that $\angle \mathrm{MPN}=90^{\circ}$.
(b) On the locus of P in the diagram in (a) above, construct the locus of T which is such that it is equidistant from M and N .
11. A box contains 3 red balls, 7 blue balls and 2 green balls. A ball is taken at random. What is the probability of it being neither red nor green.
12. In an examination there are two papers each with total marks of 50 . To pass the examination a candidate must score at least 20 marks on each paper and at least 50 marks on the two papers combined. If $x$ and $y$ represent marks on paper I and paper II respectively. Write down three difequalities representing the above information.
13. The gradient of a curve at the point ( $x, y$ ) is $5 x+\frac{3}{x^{2}}$ if it passes through (1,2). Find its equation. ( 4 mks )
14. A ship sails due North from latitude $20^{\circ}$ S for a distance 1440 nm . Find the latitude of the point it reaches.
15. Find $x$ if $\operatorname{Cos} x=\frac{\sqrt{3}}{2}$ for $-180^{\circ} \leq 8 \leq 180^{\circ}$.
 magnitude of p to 4 S. $\tilde{\sim}$
(4 mks)

## SECTION II (50 Marks)

## Answer any Five Questions in this section

17. An amount of money was shared among five businessmen. Njoroge, Mwanzia, Ahamed, Wanyama and Kiprotich. Njoroge got $\frac{3}{8}$ of the total while Mwanzia got $\frac{2}{5}$ of the remainder. The remaining amount was shared equally among the other three of which each received KSh. 600.
(a) How much was shared among the five.
(b) Determine how much Mwanzia got.
(c) Njoroge, Mwanzia and Kiprotich invested their money and earned a profit of KSh. 1200. A third of the profit was left to maintain the business and the rest was shared according to their investment. Calculate how much each got.
18. Three consecutive term of a geometric progression are $3^{2 x+1}, 9^{x}$ and 81 respectively.
(a) Calculate the value of x .
(b) Find the common ratio.
(c) Calculate the sum of the first 4 terms of this series.
(d) Given that the fifth and the seventh terms of the G.P form the first two consecutive terms of an arithmetic sequence, calculate the sum of the fist 20 terms of the sequence.
19. The equation of a curve is given by $y=3 \cos x-4 \sin x$.
(a) Complete the table below correct to 1 d.p
(2 mks)

| x | 0 | 30 | 60 | 90 | 120 | 150 | 180 | 210 | 240 | 270 | 300 | 330 | 360 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 3 |  |  | -4 |  |  | -3 |  |  | 4 |  |  | 3 |

(b) On the grid provided, draw the graph of $\mathrm{y}=3 \cos \mathrm{x}-4 \sin \mathrm{x}$ for $0 \leq \mathrm{x} \leq 360$
(4 mks)
(c) Use your graph to solve. $3 \cos x=4 \sin x-1$
(2 mks)
(d) Find the range of values of $x$ for which $3 \cos x-4 \sin x+4<0$
(2 mks)
20. The figure below shows a cube of side $10 \mathrm{~cm} . \mathrm{M}$ is the midpoint of AF .


Find
(i) length HM
(ii) the angle HM and ABCD .
(iii) angle between HM and MC
21. P varies directly as the square of Q and inversely as R .
(a) (i) Given that $\mathrm{P}=2$ when $\mathrm{R}=5$ and $\mathrm{Q}=4$, find the equation connecting P Q and R .
(ii) If $\mathrm{P}=4.5$ and $\mathrm{R}=5$. Find the positive value of Q .
(b) If Q increases by $5 \%$ and R decreases by $10 \%$. Find the percentage change in P .
22. A particle moves such that its displacement $S$ metres after $t$ seconds from a fixed point is given by $S=3 t^{3}-6 t^{2}+4 t+5$. Determine
(a) The displacement of the particle at $\mathrm{t}=2$.
(b) The velocity of the particle when $t=3$.
(c) The displacement of the particle when the particle was momentarily at rest.
(d) The acceleration of the particle when $t=1.5$ seconds.
23. A number of students were asked to cut 30 cm length of binding wire without measuring. Later 100 pieces are collected and measured correct to the nearest 0.1 cm and the data filled on the table below.

| Length <br> $(\mathrm{cm})$ | $28.0-28.4$ | $28.5-28.9$ | $29.0-29.4$ | $29.5-29.9$ | $30.0-30.4$ | $30.5-30.9$ | $31.0-31.4$ | $31.5-31.9$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 5 | 8 | 30 | x | 10 | 20 | 10 | 4 |

(a) Calculate the value of $x$
(b) State the model class
(c) Using 29.7 as working mean, calculate (i) the mean.
(ii) the standard deviation.
24. Two quantities $p$ and $n$ are connected by the equation $P=A K^{n}$, where $A$ and $K$ are constant. The table below shows corresponding values of $n$ and $p$.

| $n$ | 2 | 4 | 6 | 8 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $P$ | 9.8 | 19.4 | 37.4 | 74.0 | 144.4 |

(a) State the linear equation connecting $p$ and $n$.
(2 mks)
(b) On the grid provided, draw a suitable straight line.

(c) Use your graph to estimate the value of A and K .

