121/1
MATHEMATICS (ALT.1)
PART 1
21/2 HOURS

## KENYA CERTIFICATE OF SECONDARY EDUCATION (K.C.S.E) MATHEMATICS (Alt.1)

## PAPER 1

$21 / 2$

## Instructions to the candidates

- Write your name and index number in the spaces provided above
- Sign and write the date of the examination in the spaces provided above
- This paper contains two sections; I and section II.
- Answer ALL the questions in section I and any five questions from section II.
- All working and answers must be written on the questioncpaper in the space provided below each question
- Show all the steps in your calculations, giving youranswer at each stage in the spaces below each question
- Marks may be given for correct working evencif the answer is wrong
- Non Programmable silent electronic calcưtator and KNEC mathematical may be used EXCEPT where stated otherwise
- Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questionsjare missing.


## SECTION I

| Question | 1 |  |  |  | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Marks |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

SECTION Ii

| Question | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Marks |  |  |  |  |  |  |  |  |

## PAPER 1 SECTION I (Answer all questions in this section in the spaces provided)

1. Evaluate without using a calculator
$\frac{2^{3 / 4}+1^{1 / 6}-2^{5 / 9}}{2^{3 / 4} \text { of } 1^{1 / 6}: 2^{4 / 9}}$
2. Simplify

$$
\frac{\mathrm{b}}{a^{2}-a b}+\frac{\mathrm{a}+\mathrm{b}}{a b}
$$

3. A train is supposed to start at 11:58 p.m and to reach its destination af $1: 49$ p.m. if it starts 4 minutes late and arrives 18 minutes late, how long it takes 10 make the journey.
(2 marks)
4. A rectangular container measuring 15 cm by 12 cm contains water to a depth of 10 cm . find the new height of water if 1.08 litres of water is drawnfrom the container.
5. The angles of a pentagon are $x, 1 \frac{1}{2} x, 21 / 2, X(x-20)$ degrees. Find the value of $x$
(3 marks)
6. Solve for x in the equation
$25^{x}+5^{2 x}=50$
7. Kamau bought two similar shirts at the same price each. He sold one shirt at Ksh 624 making a profit of $\mathrm{x} \& \%$. He sold the other shirt at Ksh. 416 making a loss of X \%. Calculate the buying price of each shirt.
8. The figure below shows a circle center O with POS as Diameter. QOR is equilateral triangle and $\mathrm{PT}=\mathrm{ST}$. given that angle $\mathrm{POQ}=64$, find the size of angle:

(i) PTQ
(1 mark)
(ii) STR
( 2 marks)
9. Solve logarithms to evaluate

$$
\frac{8.329 \times \sqrt[3]{0.07686}}{(0.09533) 2}
$$

10. Given the inequalities $-14 \leq 4-3 x<10$

Solve the inequalities and represent the solution on a number line
(3 marks)
11. The figure below shows a solid cone of diameter 21 cm and height 8 cm . Calculate to decimal place.

a) The slant height of the cone
b) The total surface area of the cone take $\pi=22 / 7$
12. Factorise :- $12 a^{2} b^{2}+11 a b-5$
13. A school bought 40 text book at a total cost of ksh. 18,000. Some books cost ksh 400 each, while others cost ksh, 600 each. Find the number of text books which were bought at ksh. 400 each
14. The coordinates of points $A, B$ and $C$ are $A(-2,4), B(3,1)$ and $C(13,-5)$ show that points $A, B$ and $C$ are collinear.
15. The vertices of a rectangular pentagon lie on the circumference of a circle of radius 5 cm . calculate the length of a side of the pentagon.
16. An employer increased the salaries of his employees in the ratio of 21: 20. Find the new salary of an employee who was receiving ksh 30,900.

## SECTION II

## Answer any FIVE questions from this section

17. The diagram below represents the cross section of a bridge with a solid part and a tunnel through which a river flows. The tunnel is 8 m long and its cross-section is a semi-circle of radius 3.5 m . The bridge is 5 m high and its solid part is filled with concrete.

a) Calculate
i) The cross sectional area of the solid part (take $\pi=22 / 7$ )
ii) Volume of concrete used to fill the solid part
b) Concrete is made by mixing gravel, sand and cement in the ratio 5:4:1 by mass. Given that the density of concrete is $1.8 \mathrm{~g} / \mathrm{cm}^{3}$ and one bag of cement has a mass of 50 kg . Calculate
i) Total mass of cement used
ii) Number of bags of the cement used in constructing the bridge
18. Plot the points $A(0,2) B(2,3) C(2,1)$ and $D(4,0)$ on the grid below and join them in the order ABCD.
a) Reflect the figure in the $y$-axis
b) Reflect the new figure in a) above (both object and its image) ${ }^{\text {in }}$ the x -axis (2 marks)
c) Show in your diagram the lines of symmetry of the figure
d) What's the order of symmetry of figure formed ine above
19. The figure below shows a rectangle $A B C D$ in which $A B=X \mathrm{~cm}$ and $B C=2 \mathrm{xcm}$ point $P$ and Q are on AD and CD respectively such that $\mathrm{PD}=6 \mathrm{~cm}$ and $\mathrm{DQ}=2 \mathrm{~cm}$.

a) Find in terms of $x$
i) Area of triangle BCQ
ii) Area of triangle BAP
iii) Area of triangle BPQ
iv) Given that the area of triangle ABP is $40 \mathrm{~cm}^{2}$
i) Find the value of $x$
ii) Find the area of the shaded region
20. The mass of the number of form 2 students were measured to the nearest kilogram and recorded in the table below

| 40 | 39 | 37 | 41 | 43 | 41 | 43 | 38 | 40 | 43 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 45 | 42 | 47 | 48 | 46 | 49 | 50 | 53 | 46 | 47 |
| 39 | 44 | 48 | 51 | 46 | 46 | 54 | 45 | 44 | 46 |
| 50 | 54 | 52 | 47 | 52 | 51 | 53 | 49 | 44 | 52 |
| 46 | 43 | 50 | 49 | 48 | 47 | 46 | 48 | 51 | 41 |

a) Find the modal class
b) Use the above data to complete the frequency table below

| Class (kg) | Frequency F | mid-point $x$ | Deviation <br> $\mathrm{D}=\mathrm{x}-44$ | fd | $\mathrm{Fd}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $37-39$ |  |  |  |  |  |
| $40-42$ |  |  |  |  |  |
| $43-45$ |  |  |  |  |  |
| $46-48$ |  |  |  |  |  |
| $49-51$ |  |  |  |  |  |
| $52-54$ |  |  |  |  |  |
|  | $\sum \mathrm{~F}=$ |  | $\mathrm{Fd}=$ | $\sum \mathrm{Fd}^{2}=$ |  |

c) Use the completed table to calculate
i) The mean mass
ii) The standard deviation
21. After following his customer @ $5 \%$ disgount on the price marked a sales agent sold a second hand bus at ksh $1,140,000$. The owner of the bus received ksh $1,003,200$ from the sales agent after the agent deducted his commission.
a) Determine the marked price of the bus.
b) Calculate the percentagecommission the agent received.
c) By selling the bus this way the owner incurred the loss of $25 \%$ calculate the amount he had paid the for the bus
d) Calculate the price of a new bus given that the amount the owner received was only $30 \%$ of the price of a new bus.
(2 marks)
22. The figure below shows a sketch of the curve $y=-x^{2}+2 x+11$ and the line $y=7-x$. the line cuts the curve at P and Q

## DIAGRAM

a) Find the coordinates of P and Q
b) Calculate the area of trapezium PQRS
c) Use integration to find the area under the curve between P and Q
d) Hence find the area of the shaded
23. A point $P$ divides line $A B$ internally in the ratio $2: 1$
a) given that the coordinates of $A$ and $B$ are ( $3,-6$ ) and ( 6,9 ) respectively find the Coordinators of P
b) A point $Q$ is on the $y$-axis such that $P Q$ is perpendicular to $A B$. Find
i) The gradient of PQ
ii) The equation of line $P Q$
iii) Determine the coordinates of Q and hence the length of PQ
24. A school hired a number of buses and matatus to transport a group of students to Nairobi. The number of matatus was three times the number of buses. The hire charges were ksh. 3500 per matatu and ksh. 6500 per bus. The total cost of hiring the vehicles were ksh. 85000. Each matatu can carry 13 students while a bus can carry 65 students.
a) Determine the number:
i) of buses hired
ii) of matatus hired
b) Calculate the number of students transported to Nairobi if each vehicle was filled to capacity and number of vehiclesjuade a double trip
c) Each student contributed ksh. 85 towards the cost of the trip and the school paid the remaining amount. How huch did the school pay?


