

Name Adm. No.

Class

121 / 2

MATHEMATICS ALT 1

2 ½ HRS

FORM 3

Trial 6

2018

FORM THREE

Kenya Certificate of Secondary Education

Instructions

- (a) Write your name, class and admission number.
- (b) Answer all the questions in section I and ONLY Five in section II.
- (c) Show all the calculations in the spaces provided
- (d) KNEC mathematical tables and non-programmable calculators may be used.

For Examiners Use

Section 1

| | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|-------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| | | | | | | | | | | | | | | | | |

Section 11

| | | | | | | | | |
|----|----|----|----|----|----|----|----|-------|
| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| | | | | | | | | |

| |
|-------------|
| Grand total |
| |

SECTION I

1. Evaluate using logarithms.

[4 Marks]

$$\frac{\sqrt[3]{0.04689}}{51.64 \times 0.793}$$

2. Find the value of k if the expression $4x^2 - 10x + k + 3$ is a perfect square [2 Marks]

3. A rectangular block has a square base whose sides are exactly 8 cm. Its height, measured to the nearest millimeter is 3.2 cm. calculate the greatest possible error in calculating its volume [4 Marks]

4. A matrix is given by $T = \begin{pmatrix} 6 & 5 \\ -3 & 5 \end{pmatrix}$. Find T^{-1} [2 Marks]

5. The vectors a, b, c are given as $a = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$, $b = \begin{pmatrix} 4 \\ -3 \end{pmatrix}$ and $c = \begin{pmatrix} 0 \\ 4 \end{pmatrix}$. Another vector q is such

that $q = 2a - 3b + 2c$. Calculate $|q|$ correct to 3 decimal places.

[3 Marks]

6. Simplify by rationalizing the denominator;

[2 Marks]

$$\frac{3}{2\sqrt{3} - \sqrt{2}}$$

7. A scientific calculator is marked at sh. 1560. Under hire purchase it is available for a down payment of sh. 200 and six monthly instalments of sh. 250 each. Calculate;

a. The Hire purchase price.

[2 Marks]

b. The extra amount paid out over the cash price.

[1 Mark]

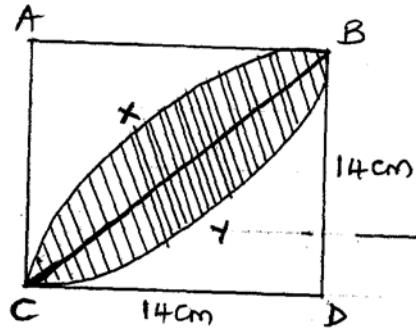
8. Solve the equation;

$$\log(x + 24) - 2 \log 3 = \log(9 - 2x)$$

[3 Marks]

9. In the figure below, ABCD is a square of side 14 cm. CXB and CYB are arcs of circle centre A and D respectively. Calculate the area of the shaded region

[3 Marks]

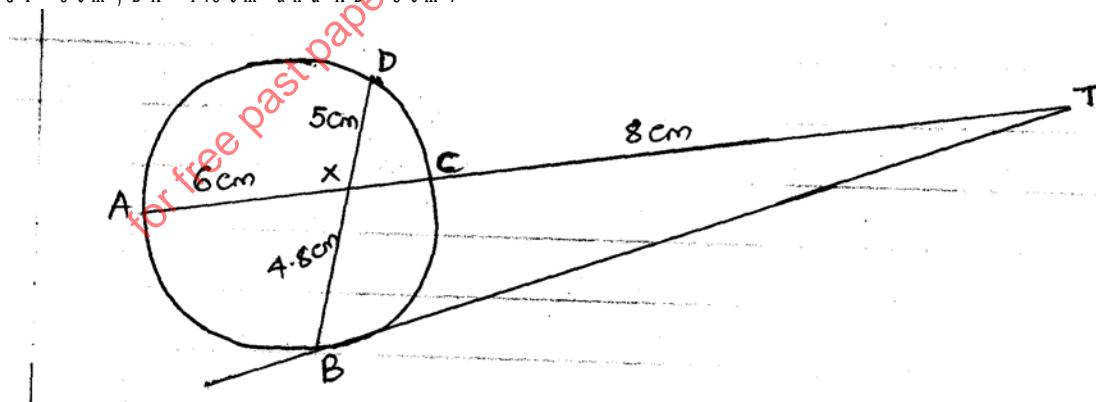


10. Make x the subject of the formula;

[3 Marks]

$$p = \frac{a \sqrt{x^2 + b^2}}{y}$$

11. In the figure below, BT is a tangent to the circle at B . AXC and BXD are straight lines. $AX = 6\text{ cm}$, $CT = 8\text{ cm}$, $BX = 4.8\text{ cm}$ and $XD = 5\text{ cm}$.



Find the length of;

a. XC

[2 Marks]

b. BT

[2 Marks]

12. Find the value of x if the matrix $\begin{pmatrix} x & 1 \\ 4 & x - 3 \end{pmatrix}$ is a singular matrix. [3 Marks]

13. The first - term of an arithmetic sequence is -7 and the common difference is 4.
a. List the first 6 terms of the sequence [2 Marks]

b. Determine the sum of the first 30 terms of the sequence [2 Marks]

14. A manufacturer sells a bottle of fruit juice to a trader at a profit of 40%. The trader sells it for sh.

84 at a profit of 20%. Find.

a. The traders buying price. [2 Marks]

b. The cost of manufacture of one bottle. [1 Mark]

15. ABC is a triangle whose base BC = 35. The point X on BC is such that BX = 21 cm, AX = 16 cm and angle AXB = 60°. Calculate;

a. The length of AB

[1 Mark]

b. The length of AC

[1 Mark]

c. The size of angle BAC

[1 Mark]

16. A small cone of height 8 cm is cut off from a bigger cone to leave a frustum of height 16 cm. If the volume of the smaller cone is 160 cm^3 , find the volume of the frustum.

[3 Marks]

SECTION II Answer ANY 5 questions in this section

(50 marks)

17. The position vectors of A and B with respect to the origin are $(\begin{smallmatrix} -8 \\ 5 \end{smallmatrix})$ and $(\begin{smallmatrix} 1 \\ 2 \\ 5 \end{smallmatrix})$ respectively. Point M is the mid-point of AB and N is the mid-point of OA.

a. Find;

i. The coordinates of N and M

[3 Marks]

ii. The magnitude of NM

[3 Marks]

b. Express vector \underline{NM} in terms of \underline{OB}

[1 Mark]

c. Point P maps onto P' by a translation $(\begin{smallmatrix} -5 \\ 6 \end{smallmatrix})$.

Given that $OP = OM + 2MN$.

[3 Marks]

Calculate the coordinates of P'

18. Complete the table below for the function $y = 2x^2 + 4x - 3$

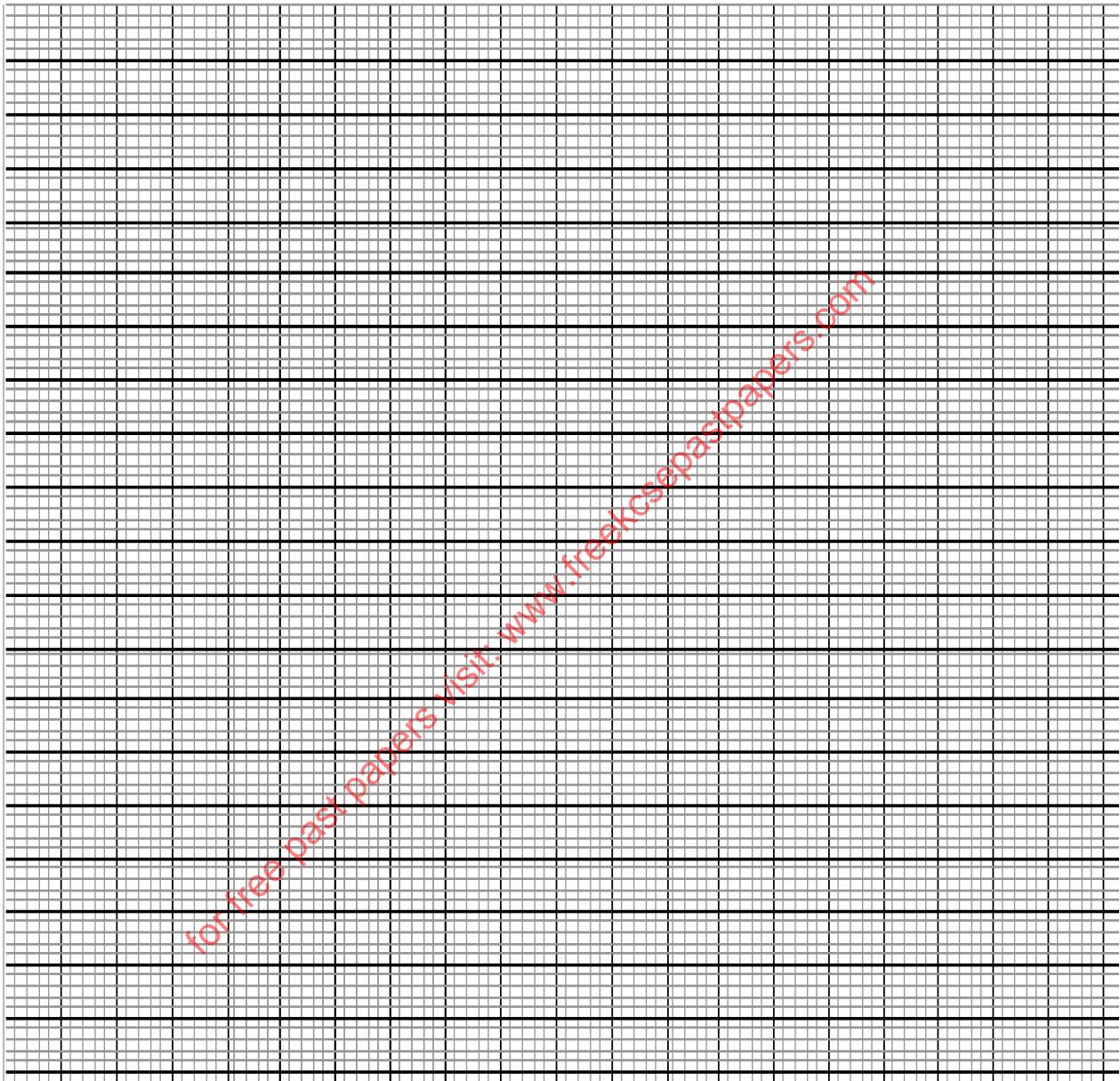
a.

[2 Marks]

| | | | | | | | |
|---|-----|-----|-----|-----|---|---|---|
| x | - 4 | - 3 | - 2 | - 1 | 0 | 1 | 2 |
|---|-----|-----|-----|-----|---|---|---|

| | | | | | | | |
|--------|----|--|----|---|---|--|----|
| $2x^2$ | 32 | | | 1 | 0 | | |
| 4x | | | | | | | |
| -3 | | | -3 | | | | -3 |
| y | | | -3 | | | | |

- b. On the grid provided, draw the graph of the function
 $y = 2x^2 + 4x - 3$ for $-4 \leq x \leq 2$ and use your graph to determine the roots of the quadratic equation $2x^2 + 4x - 3 = 0$ to 1 decimal place. [3 Marks]



c. Use your graph to solve the roots of the quadratic equations.

i. $2x^2 + x - 5 = 0$

[2 Marks]

ii. $2x^2 + 3x - 2 = 0$

[2 Marks]

19. The table below shows the masses to the nearest kilograms of 65 animals in a farm.

| | | | | | | |
|------------|-------|-------|-------|-------|-------|-------|
| Mass in Kg | 26·30 | 31·35 | 36·40 | 41·45 | 46·50 | 51·55 |
| Frequency | 9 | 13 | 20 | 15 | 6 | 2 |

Use the table to find.

- a) Modal and median class [2 Marks]

- b) Mean of the data [3 Marks]

- c) The median mass [3 Marks]

- d) The percentage of animals with a mass between 36 kg and 45 kg. [2 Marks]

20.

- a. A matrix T is given by $T = \begin{pmatrix} 4 & 5 \\ 6 & 4 \end{pmatrix}$
Find T^{-1} [2 Marks]

- b. Truphen bought 20 bags of maize and 25 bags of beans at a total cost of sh. 77,000. If she had bought 30 bags of maize and 20 bags of beans, she would have spent sh. 7,000 more.

i. Form a matrix equation from this information. [1 Mark]

ii. Determine the cost of a bag of maize and a bag of beans. [3 Marks]

- c. She sold all the maize and beans at a profit of 10% on a bag of maize and 12½% on a bag of beans. Calculate the total percentage profit. [4 Marks]

21. At the beginning of the year 2000, Kanyora bought two houses, one in Thika and the other in Nakuru each at 1,240,000. The value of the house in Thika appreciated at a rate of 12% p.a.
- a. Calculate the value of the house in Thika after 9 years to the nearest shilling. [2 Marks]

- b. After n years, the value of the house in Thika was 2,741,245 while the value of the house in Nakuru was 2,917,231.
- Find n [4 Marks]
 - Find the annual rate of appreciation of the house in Nakuru. [4 Marks]

22. The table below shows income tax rates.

| <u>Taxable income in k£ per month</u> | <u>Rate in shs. per k£</u> |
|---|----------------------------|
| 1 - 325 | 2 |

| | |
|-------------|---|
| 326 - 650 | 3 |
| 651 - 975 | 4 |
| 976 - 1300 | 5 |
| 1301 - 1625 | 6 |
| Over 1626 | 7 |

Waketi earns a basic salary of 20,500. He has a house allowance of sh. 6,000 per month, medical allowance of sh. 4,000 per month and transport allowance of sh. 3,000 per month. He claims a tax relief of sh. 1,056 per month.

a. Calculate

i. Waketi's taxable income in k£ per month. [2 Marks]

ii. Gross tax. [3 Marks]

iii. Net Tax [2 Marks]

b. His net income per month has the following deductions

Health insurance fund - sh. 150

Loan interest - sh. 200

Service charge - sh. 200

Sacco loan - sh. 2,500

Calculate his net income per month. [3 Marks]

23. P varies directly as the square of Q and inversely as R.

a. If Q increases by 5% and R decreases by 10%, find the percentage change in P

[5 Marks]

b. Given that $P = 2$ when $R = 5$ and $Q = 4$, find the positive value of Q when $P = 4.5\text{ cm}$ and $R = 5\text{ cm}$.
[5 Marks]

- 24.
- a. The first term of an arithmetic progression is 2. The sum of the first 8 terms of the AP is 240.
- Find the common difference of the AP.
[2 Marks]
 - Given that the sum of the first n terms of the AP is 1,560. Find n
[2 Marks]

b. The 3rd, 5th and 8th terms of another A.P from the first three terms of a G.P. If the common difference of the A.P is 3.

Find.

i. The first term of G.P

[4 Marks]

ii. The sum of the first 9 terms of the G.P to 4 s.f.

[2 Marks]

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