# MATHEMATICS PAPER I FORM III 

## Time: $21 / 2$ hours

NAME $\qquad$ ADM NO CLASS

## Instructions

i) Answer all questions in section I and any five questions in section II
ii) Show all your workings in the spacers provided.
iii) Use recommended calculator and mathematical tables

FOR EXAMINERS USE ONLY


1) Evaluate without using calculator

$$
\frac{\left(1 \frac{3}{7}-\frac{5}{8}\right) \times \frac{2}{3}}{\frac{3}{4}+1 \frac{5}{7} \div \frac{4}{7} \text { of } 2 \frac{1}{3}}
$$

2) A two digit number is such that the sum of the ones and the tens digits $s$ is ten. If the digits are reversed, the number formed exceeds the original by 54 . Find the number
3) Simplify

4) Find all integral values of $x$ which satisfy the inequalities.

$$
2(2-x)<4 x-9<x+11
$$

5) Simplify the expression

$$
\frac{p^{2}-4 m^{2}}{2 m^{2}-7 m p+3 p^{2}}
$$

6) The sides of a rectangle water tank are in the ratio $1: 2: 3$. If the volume of the tanks is $1024 \mathrm{~cm}^{3}$. find the dimension of the tank.
7) The length and width of a rectangle figure is 6.1 cm and 5.3 cm respectively. Calculate the percentage error in the perimeter of the rectangle
8) Find the values of which satisfy the equation.
(2mks)
$2 \cos \left(2 \beta+30^{\circ}\right)=\sqrt{3}$ in the domain $0^{\circ} \leq \beta \leq 360$
9) Use logarithms to calculate

$$
\left(\frac{0.5342 \times 0.07627}{23.47}\right)^{\frac{1}{3}}
$$

10) Solve the logarithmic equation below for the value of x
$\log _{10}(3 x+1)-\log _{10}(x-2)=\log _{10} 10$
11) Given the $\operatorname{Sin} \beta=\frac{\sqrt{2}}{\sqrt{3}}$. Find the value of $\frac{\operatorname{Tan} \beta+\operatorname{Sin} \beta}{\operatorname{Cos} \beta}$
12) Calculate the missing angles where $O$ is the centre

13) Solve using completing square method
14) Calculate the compound interest on sh. 9,000 for 2 years at $12.5 \%$ p.a compounded half yearly.

15) In the figure below, if a circle is drawn passing through $A, B$ and $C$ what would be the radius of the circle

16) A bicycle wheel turns 30 times in covering 132 m . find
i) The radius of circle
ii) Express the speed in $\mathrm{km} / \mathrm{h}$

## SECTION II

## ANSWER FIVE QUESTIONS ONLY (50 MARKS)

17) Income rates for income earned were charged as follows

| Income in kshs. p.m | Rates in kshs. Per sh.20 |
| :---: | :---: |
| $1-8400$ | 2 |
| $8401-18000$ | 3 |
| $18001-30000$ | 4 |


| $30001-36000$ | 5 |
| :---: | :---: |
| $36001-48000$ | 6 |
| 48001 and above | 7 |

A civil servant earns a monthly salary of kshs. 19200. His house allowances is ksh. 12000 per month. Other allowances per month are transport kshs. 1300 and medical allowances kshs. 2300 . he is entitled to a family relief of kshs. 1240 per month. Determine
i) His taxable income per month
ii) Net tax

In addition, the following dedurctions are made

| NHIF | -ksh .230 |
| :--- | :--- |
| Service chárge | -ksh .100 |
| Loan repayment | -ksh .4000 |
| Cooperative shares | -ksh .1200 |

Calculate his net salary per month
18) The diagram represents a solid frustram with a base radius 21 cm and top 14 cm . the frustram is 22.5 cm high and id made of a metal whose density is $3 \mathrm{~g} / \mathrm{cm}^{3} .\left(\pi=\frac{22}{7}\right)$
a) Calculate
i) The volume of the metal in the frustrame
ii) The mass of the frustram in kg
b) The frustrum is melted down and recast into a solid cube. In the process $20 \%$ of the metal is lost. Calculate to decimal places the length of each side of the cube.
19) Using a ruler and d pair of compasses only draw a parallelogram $A B C D$ such that angle $D A B=75^{\circ}$, length $A B=6 \mathrm{~cm}$ and ${ }^{\circ} \mathrm{BC}=4 \mathrm{~cm}$ D drop a perpendicular to meet AB at N .
a) Measure length DN
b) Find the area of parallogram
20) The distance between town $A$ and $B$ is 360 km . a minibus left $A$ at $8.15 \mathrm{a} . \mathrm{m}$. and travelled towards B at an average speed of $90 \mathrm{~km} / \mathrm{h}$. A matatu left B two and a third hours later in the same day and travelled towards A at an average speed of $110 \mathrm{~km} / \mathrm{h}$.
a) i) At what time did the two vehicles meet?
ii) How far from A did the vehicles meet
b) a motorist started from his home at 10.30a.m on the same day and travelled at an average speed of $100 \mathrm{~km} / \mathrm{h}$. he arrived at B at the same time as the minibus. Calculate the distance from A to his house.
21) A triangle $X Y Z ; x(-1,-1), y(-2,-4)$ and $z(-6,-9)$ is reflected in the line $x$-axis, to obtain $X^{1} Y^{1} Z^{1}, X^{1} Y^{1} Z^{1}$ is reflected on the line $y=x$ to obtain $X^{2} Y^{2} Z^{2}, X^{2} Y^{2} Z^{2}$ is rotated to obtain $X^{3} Y^{3} Z^{3}$. The rotation is $+90^{\circ}$ about origin.
i) On the grid provided show the objects and the images
ii) State the coordinates of the images
22) Complete the table below of the function


Use your graph to solve
i) $\quad x^{2}-5 x+3=0$
ii) $\quad x^{2}-5 x+3=-3$
iii) $\quad x^{2}-6 x+6=0$
23) The angle of depression of a point A on the ground from the top of a post is $18^{\circ}$ and that of another point $B^{\circ}$ on the same line as $A$ and nearer to the post is $25^{\circ}$. If $A$ and $B$ are 70 m apart.
a) Draw asketch to represent positions of A and B
b) Using your sketch calculate
i) The height of the post from the ground level (1dp)
ii) The distance of point $A$ from the foot of the post


