NAME $\qquad$ .CLASS $\qquad$
121/1
MATHEMATICS
PAPER 1
TIME: $21 / 2$ HOURS

## END OF TERM 12019 EXAMINATIONS FORM 4 MATHEMATICS PAPER 1

## INSTRUCTIONS TO CANDIDATES

(a) Write your name and index number in the spaces provided.
(b) This paper consists of two sections I and II
(c) Answer all the questions in section I and ONLY FIVE questions in section II.
(d) All answers and working must be written on the question paper in the spaces provided below each question.
(e) Show all the steps in your calculation giving your answer at each stage in the space below each question.
(f) Marks are given for correct working even if the answer is wrong.
(g) Use calculators and KNEC mathematical tables except where stated otherwise.

FOR EXAMINER'S USE ONLY
SECTION


SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |

## GRAND TOTAL



## SECTION I (50 MARKS)

## ANSWER ALL OUESTIONS IN THIS SECTION

1. Evaluate
(3marks)

$$
\frac{11+(-2) \times(-6) \div 3}{11-40 \div(2 \times 4)}
$$

2. Express the numbers: 935 and 19845 as a product of their pfime factors; hence evaluate $\frac{935}{19845}$ leaving your answer in prime factor form.
3. Two special grades of baking flour costing ksh. 200 and ksh. 250 per kg respectively are mixed in the ratio $3: 5$ by mass. The mixture is then sold at ksh. 240 per kg . Find the percentage profit on the cost correct to 1 d.p.
(3marks)
4. A prism of length 15 cm has a uniform triangular cross-section of sides measuring $8 \mathrm{~cm}, 7 \mathrm{~cm}$ and 5 cm . Determine the volume of the prism.
5. The size of each interior angle of a regular polygon is four times the size of the exterior angle. Find the number of the polygon.
6. Use logarithms to 4 decimal places to evaluate;
7. A straight line L 1 is perpendicular to another line L 2 whose equation is $3 y+4 x=12$. If the two lines meet at point $P$ which lies on the $x$-axis, find:(i) the coordinators of pcint $P$.
(ii) The equation of line Ll in the form $\mathrm{y}=\mathrm{mx}+\mathrm{c}$
8. Convert $154.50^{\circ}$ into radians and write your answer in terms of $\pi^{\mathrm{c}}$
9. Given that $\tan \theta^{0}=3 \cdot \frac{3}{7}$ find $\operatorname{Cos}(90-\theta)$ as a decimal.
10. Solve the simultaneous inequalities given below and list all the integral values of x . (3marks) $\frac{3-x}{2} \geq \frac{1+1}{3} \geq \frac{2 x+1}{-3}$
11. Solve the following equation for $\mathrm{x}:-$ $9^{x}+3^{2 x-1}-1=107$
12. A Kenyan bank buys and sells foreign currency as shown below.

|  | Buying (ksh) | Selling (ksh) |
| :--- | :--- | :--- |
| 1 US dollar (\$) | 100.00 | 101.20 , |
| 1UK pound $(£)$ | 145.00 | 145.95 |

A tourist arrived in Kenya with 9600 which he converted into ksh. at a commission of $5 \%$. He later used $3 / 4$ of the money before changing the balance of dollarsat no commission. Calculate to the nearest dollar, the amount he received.
13. Simplify the expression.
(3marks)

$$
\frac{8 x-18 x^{3}}{3 x^{2}-4 x-4}
$$

14. Given that $\underset{\sim}{a}=\underset{\sim}{2 i}+3 \underset{\sim}{j}$ and $\underset{\sim}{b}=\underset{\sim}{i}-5 \underset{\sim}{j}+7 \underset{\sim}{k}$, evaluate $|2 \underset{\sim}{a}+\underset{\sim}{b}|$
15. A train of length 80 m crosses a bridge 24 m long in 5 seconds. Calculate the average speed of the train in $\mathrm{km} / \mathrm{h}$.
16. Below is part of a sketch of solid cuboid ABCDEFGH. Complete the sketch.(3marks)

## SECTION II (50 MARKS) <br> ANSWER ONLY FIVE QUESTIONS IN THIS SECTION.

17. The following data was obtained from masses of pregnant women in a maternity clinic.

| Masses (kg) | $1.5 \leq \mathrm{x}<5.5$ | $5.5 \leq \mathrm{x}<7.5$ | $7.5 \leq \mathrm{x}<13.5$ | $13.5 \leq \mathrm{x}<15.5$ | $15.5 \leq \mathrm{x}<20.5$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| No. of women | 16 | 20 | 18 | 14 | 15 |

(a) Represent the information on a histogram, on the g rid provided.
(4marks)
(b) Use the information in the table above to estimate (i) the mean mass
(c) the median mass
18. The figure below shows an open tank whose external dimensions are 12 m by 8 m by 6 m . The materials making the tank has a thickness of 0.5 m .

(a) Calculate the amount of liquid it can hold when full.
(2marks)
(b) Find the volume of the material making the tank.
(c) If the tank can be emptied at a rate of 20 litres per minute by an outlet pipe, how long would it take to empty a full tank?
19. Four towns $P, Q, R$ and $S$ are such that $Q$ is 168 km from $P$ on a bearing of $063^{\circ}$. $R$ is 288 km on a bearing of $30^{\circ} \mathrm{E}$ from Q . S is due west of R on a bearing of $161^{\circ}$. Using the scale of 1 cm to represent 40 km .
(a) Show the relative position of $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ and S .
(4marks)
(b) From the diagram, find
(i) The bearing of S from Q
(ii) The bearing of P from R
(iii) The distance of PS and SR
20. A certain number of form four students agreed to contribute equally to buy a gift worth sh. 1200 for their class prefect's birthday. Five students pulled out and so the others agreed to contribute an extra sh. 10. Their contribution enabled them to buy a gift worth sh. 200 more than they originally expected.
(a) If the original number of students was $x$, write an expression of how much each was originally going to contribute.
(lmark)
(b) Write down two expressions of how much each contributed after the five students pulled out.
(c) Calculate how many students made the contribution.
(d) Find how much each contributed.
21. (a) The points $A(2,6), B(1,1), C(3,4)$ and $D(5,3)$ are the vertices of a quadrilateral $A B C D$. Plot points $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D on the grid provided and join them to form quadrilateral ABCD .
(b) Locate and write down the co-ordinates of point $A^{\prime} B^{1} C^{\prime} D^{1}$ image of $A B C D$ under a rotation of positive $90^{\circ}$ about the origin. On the same grid draw image quadrilateral $A^{\prime} B^{1} C^{\prime} D^{1}$ (3marks)
(d) Reflect $A^{\prime} B^{\prime} C^{\prime} D^{\prime}$ on the $x$-axis and draw the second image of the quadrilateral $A^{\prime \prime} B^{\prime \prime} C^{\prime \prime} D^{\prime \prime}$ (3marks)
(d) Draw the mirror line $M$ for the reflection of $A B C D$ whose image is $A^{4} B^{11} C^{\prime \prime} D^{11}$ (2marks)
22. $A, B, C$ and $D$ is a rhombus. The equation of line $A B$ is $y=x+3$ and that of $A D$ is $y+x=5$. The coordinate of $C$ is $(1,-2)$.
Find,
(i) The coordinate of $\mathrm{A}, \mathrm{B}$ and D
(6marks)
(ii) The coordinate of the mid point AB .
(iii) The length of AC correct to 2 d.p.
(iv) The equation of BD .
23. OABC is a trapezium such that the coordinates of $\mathrm{O}, \mathrm{A}, \mathrm{B}$ and C are $(0,0),(2,-1)(4,3)$ and ( $0, \mathrm{y}$ ).
(a) find the value of $y$
(2marks)
(b) $M$ is the mid-point of $A B$ and $N$ is the mid point of $O M$. Find in column form.
(i) The vector ${ }_{\sim}^{A N}$
(3marks)
(ii) The vector $\underset{\sim}{\mathrm{N}} \mathrm{C}$
(iii) Vector $A C$
(1mark)
(c) Hence show that $\mathrm{A}, \mathrm{N}$ and C are collinear
23. Given that $y=x^{2}+5 x-4$, complete the table below.
(2marks)

| x | -6 | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y |  |  |  |  |  |  |  |  |  |

(b) On the grid provided draw the graph of $y=x^{2}+5 x-4$ for $-6 \leq x \leq 2$
(3marks)
(c) Use your graph to solve the following equations.
(i) $x^{2}+5 x-4=0$
(ii) $x^{2}+6 x=0$

