

#### **CIFA PART II SECTION 3**

# **CORPORATE FINANCE**

TUESDAY: 26 November 2019.

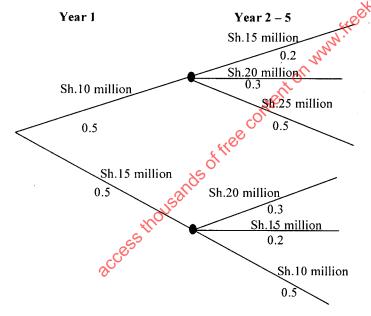
Time Allowed: 3 hours.

Answer ALL questions. Marks allocated to each question are shown at the end of the question. Show ALL your workings.

# **QUESTION ONE**

- (a) With reference to agency theory, highlight four causes of agency problems that could arise between shareholders and government. (4 marks)
- (b) Zimco Limited is considering acquiring a new machine at a cost of Sh.20 million. The machine is expected to have a useful life of five years with a nil salvage value after five years.

The expected net cash flows and associated probabilities of occurrence are summarised below:



The company's required rate of return for this investment is 11%.

# Required:

(i) Expected net present value (ENPV) of the project using decision tree analysis.

(6 marks)

(ii) Expected standard deviation of the project.

(4 marks)

(iii) If the net present value of the project is less than Sh.2 million, the firm will be exposed to financial distress.

Determine the probability that the firm will avoid financial distress (Assume a normal distribution). (2 marks)

(c) Nevok Industries Ltd. is currently an all equity financed firm. The firm expects to generate earnings before interest and taxes (EBIT) of Sh.10 million over the next year. Currently, Nevok Industries Ltd. has 10 million outstanding ordinary shares. The shares are currently trading at a price of Sh.7.50 per share at the security exchange. The firm is considering changing its capital structure by borrowing Sh.15 million at an interest rate of 8% per annum and use the proceeds to purchase 2 million ordinary shares at a price of Sh.7.50 each.

Assume that the firm's EBIT is not expected to grow in the future and that all earnings are paid as dividends.

#### Required:

Using Modigliani and Miller (MM) propositions I and II, show that an increase in expected earnings per share (EPS) for Nevok Industries Ltd. will not lead to an increase in the share price. (4 marks)

(Total: 20 marks)

#### **OUESTION TWO**

Baobab Limited has not been paying dividends since inception. The Chief Finance Officer (CFO) of the company has (a) been directed by the Board to develop a dividend policy to guide on the payments of dividends in the future.

### Required:

In light of the above statement, explain three advantages and three disadvantages of dividend payments to shareholders. (6 marks)

(b) (i) Distinguish between "permanent working capital" and "seasonal working capital". (2 marks)

(ii) Xee Ltd. currently sells goods on terms of "net 30". The firm is considering adoption of terms "3/15 net 45". This change will effectively increase its average collection period from 35 days to 40 days.

The firm's current turnover is an average of Sh.50 million per annum. However, the relaxation of the terms of sale will increase annual sales by 20%.

The firm's cost of sales is 40% of turnover. 80% of the sales are made of credit basis. All credit customers will take advantage of the 3% discount offer.

Bad debts are estimated at 5% of credit sales and inventory levels are 10% of gross turnover.

The minimum required rate of return is 12% and the firm pays corporation tax at a rate of 30% per annum.

(Aşsume 365 days in a year).

#### Required:

Using suitable calculations, advise Xee Ltd. on whether to adopt the revised credit policy.

(9 marks)

(c) SLM Ltd. has cash out flows of Sh.100,000 every day, seven days a week. The interest rate is 5% and the fixed cost of replenishing cash balance is Sh.100 per transaction.

The year has 365 days.

Required:
The optimal initial cash balance using the Baumol-Allias-Tobin (BAT) model.

(3 marks)

(Total 20 marks)

#### **OUESTION THREE**

Identify three symptoms of financial distress in a firm. (a)

(3 marks)

(b) Eagle Limited is considering acquiring Pelican Limited, a firm in the same industry, so as to consolidate its market share. Given below are financial data for both firms:

	<b>Eagle Limited</b>	Pelican Limited
Number of issued ordinary shares	10 million	5 million
Earnings per share (EPS)	Sh.4	Sh.2
Market price per share (MPS)	Sh.50	Sh.25
Price to earnings (P/E) ratio	12.5 times	12.5 times

Eagle Limited is considering financing acquisition of Pelican Limited on a share for share exchange. It is considering offering 2 new shares to the shareholders of Pelican Limited in exchange of 4 shares held.

Assume a corporation tax rate of 30%.

# Required:

(i) Non-diluting offer price. (2 marks)

(ii) Non-diluting maximum exchange ratio. (2 marks)

CF32 Page 2 Out of 4

- · (iii) The post acquisition EPS of Eagle Limited at the exchange ratio they are considering offering. (3 marks)
- (iv) If the price to earnings (P/E) ratio of Eagle Limited rises to 15 times after the acquisition, determine the post acquisition market price of a share of Eagle Limited. (2 marks)
- Double K Limited is concerned whether antitrust regulators would consider the acquisition of Tripple G Limited an (c) antitrust violation. The market in which the two companies operate consist of eight competitors. The largest company has a 25% market share. Double K Limited has the second largest market share of 20%. Five companies including Tripple G Limited each have a market share of 10%. The smallest company has a 5% market share.

# Required:

(i) Calculate the increase in the Herfindahl-Hirschman Index (HHI).

(4 marks)

(ii) Explain the probable action by the antitrust regulator based on your answer in (c) (i) above.

(2 marks)

(iii) Outline one strength and one weakness of the HHI model.

(2 marks)

(Total: 20 marks)

#### **QUESTION FOUR**

Explain four distinct features of Islamic Finance. (a)

(4 marks)

(b) Describe two sources of Islamic Finance that are an alternative to a right issue and a can note. (4 marks)

The following is an extract of the statement of financial position of Tausi Limited, a company quoted at the Securities (c) Exchange:

	Sh."million"	Sh."million"
Equity and liabilities:		6.0
Equity:		4.7
Share capital	17	nun!
Retained earnings	15	
Total equity		32
Liabilities:		ntent 92
Long term liabilities	13	de
Current liabilities	21	)*
Total liabilities		34
Total equity and liabilities	6 810	<del></del>
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# Additional information:

- The share capital of the company consists of Sh.12 million of ordinary shares and Sh.5 million irredeemable 1. preference shares.
- 2. The ordinary shares have a nominal value of Sh.0.50 per share, an ex-dividend market price of Sh.7.07 per share and a cum-dividend market price of Sh.7.52 per share.
- 3. The dividend for the year 2019 will be paid in the near future.
- Dividends paid in recent years have been as follows: 4.

2018 2017 2016

2015 Dividend per share (Sh) 0.43 0.41 0.39 0.37

- 5. The 5% preference shares have a nominal value of Sh.0.50 per share and an ex-dividend market price of Sh.0.31 per share.
- 6. The long-term borrowings for the company consist of Sh.10 million of loan notes and a Sh.3 million bank loan. The bank loan has variable interest rate.
- 7. The 7% loan notes have a nominal value of Sh.100 per loan note and a market price of Sh.102.34 per loan note. Annual interest has just been paid and the loan notes are redeemable in four year's time at a 5% premium to nominal value.
- 8. The corporation tax rate is 30%.

# Required:

The after tax weighted average cost of capital (WACC) on a market value basis.

(12 marks)

(Total: 20 marks)

#### **OUESTION FIVE**

- (a) Explain the following terms as used in corporate restructuring:
  - (i) Management buyout (MBO). (1 mark)
  - (ii) Leveraged buyout (LBO). (1 mark)
  - (iii) Employee buyout. (1 mark)
  - (iv) Spin out. (1 mark)
- (b) Ndovu Limited is considering the purchase of a new machine with an operating life of three years. The new machine could be leased for three payments of Sh.55,000 payable annually in advance.

Alternatively, the machine could be purchased for Sh.160,000 using a bank loan at a cost of 8% per year. If the machine is purchased, Ndovu Limited will incur maintenance costs of Sh.8,000 per year, payable at the end of each year of operation. The machine would have a residual value of Sh.40,000 at the end of its three year life.

The company's production manager estimates that if maintenance cost routines were upgraded, the new machine could be operated for a period of four years with maintenance costs increasing to Sh.12,000 per year payable at the end of each year of operation. If operated for four years, the machine's residual value would fall to Sh.11,000.

The cost of capital is 8%.

#### Required:

- (i) Advise Ndovu Limited on whether it should lease or purchase the machine assuming that it is operated for a period of three years. (6 marks)
- (ii) Calculate the equivalent annual cost of purchasing and operating the machine for both three years and four years and recommend which replacement interval should be adopted. (6 marks)
- (c) A company's present capital structure consists of Sh.20,000,000 shares of equity stock. The company requires Sh.100,000,000 of external financing for which it is considering two alternatives:

Alternative A. Issue 5,000,000 equity shares of Sh.10 par at Sh.20 each.

Alternative B Issue 3,000,000 equity shares of Sh.10 par at Sh.20 each and 4,000,000 preference shares of Sh.10 par carrying 11% dividend.

The company tax rate is 30%.

# Required:

Determine the earnings per share-profit before interest and taxes (EPS-PBIT) indifference point for alternative A and alternative B. (4 marks)

(Total: 20 marks)

CF32 Page 4 Out of 4

# Present Value of 1 Received at the End of *n* Periods:

$$PVIF_{r,n} = 1/(1+r)^n = (1+r)^{-n}$$

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	35 .7894	.7307	.6768	.6274	.5820	.5403	.5019	.4665	.4039	.3506	.3269	.3050	.2660					.0854
43 .836	.7664	.7026	.6446	.5919	.5439	.5002	.4604	.4241	.3606	3075	2843	.2630	.2255					.0628
53 .820	.7441	.6756	.6139	.5584	.5083	.4632	.4224	.3855	.3220	.2697	2472	.2267	.1911	.1615	.1164	.0847	.0623	.0462
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        .3855         .3220         .2697         .2472         .2267           83         8043         .7224         .6496         .5847         .5268         .4751         .4289         .3875         .3505         .2875         .2366         .2149         .1954           74         .7885         .7014         .6246         .5568         .4970         .4440         .3971         .3555         .3186         .2567         .2076         .1869         1685           87         .7730         .6810         .6006         .5303         .4688         .4150         .3677         .3262         .2897         .2292         .1821         .1625         .1452</td> <td>35         8535         7894         ,7307         ,6768         ,6274         ,5820         ,5403         ,5019         ,4665         ,4039         ,3506         ,3269         ,3050         ,2660           43         8368         ,7664         ,7026         ,6446         ,5919         ,5439         ,5002         ,4604         ,4241         ,3606         ,3075         ,2843         ,2630         ,2255           53         8203         ,7441         ,6756         ,6139         ,5584         ,5083         ,4632         ,4224         ,3855         ,3220         ,2697         ,2472         ,2267         ,1911           63         8043         ,7224         ,6496         ,5847         ,5268         ,4751         ,4289         ,3875         ,3505         ,2875         ,2366         ,2149         ,1954         ,1619           74         ,7885         ,7014         ,6246         ,5568         ,4970         ,4440         ,3971         ,3555         ,3186         ,2567         ,2076         ,1869         1685         ,1372           87         ,7730         ,6810         ,6006         ,5303         ,4688         ,4150         ,3677         ,3262         ,2897         &lt;</td> <td>27 8706 813 1737 8768 8274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 43 8368 7664 7026 6446 5919 5439 5002 4604 4241 3606 3075 2843 2630 2255 1938 53 8203 7441 6756 6139 5584 5083 4632 4224 3855 3220 2697 2472 2267 1911 1615  83 8043 7224 6496 5847 5268 4751 4289 3875 3505 2875 2366 2149 1954 1619 1346 74 7885 7014 6246 5568 4970 4440 3971 3555 3186 2567 2076 1869 1685 1372 1122 87 7730 6810 6006 5303 4688 4150 3677 3262 2897 2292 1821 1625 1452 1163 0935 00 7579 6611 5775 5051 4423 3878 3405 2992 2633 2046 1597 1413 1252 0985 0779 13 7430 6419 5553 4810 4173 3624 3152 2745 2394 1827 1401 1229 1079 0835 0649  28 7284 6232 5339 4581 3936 3387 2919 2519 2176 1631 1229 1069 0930 0708 0541 44 77142 6050 5134 4363 3714 3166 2703 2311 1978 1456 1078 0929 0802 0600 0451 66 7002 3674 4936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0808 0376 77 6864 5703 4746 3357 3305 2765 2317 1945 1635 1161 0829 0703 0556 0431 098 6095 4776 3751 2953 2330 1842 1460 1160 0923 0588 0378 0379 0037 0026 0013 0014 17 4529 3066 2083 1420 0972 0668 0460 0318 0221 0107 0053 0037 0026 0013 0007 180 3715 2281 1407 0872 0543 0339 0213 0134 0085 0035 0014 0009 0000 0000 0001</td> <td>27 8706 813 1737 17307 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 43 8368 7664 7026 6446 5919 5439 5002 4604 4241 3606 3075 2843 2630 2255 1938 1443 53 8203 7441 6756 6139 5584 5083 4632 4224 3855 3220 2697 2472 2267 1911 1615 1164 83 8043 7224 6496 5847 5268 4751 4289 3875 3505 2875 2366 2149 1954 1619 1346 0938 74 7885 7014 6246 5568 4970 4440 3971 3555 3186 2567 2076 1869 1685 1372 1122 0757 87 7730 6810 6006 5303 4688 4150 3677 3262 2897 2292 1821 1625 1452 1163 0935 0610 00 7579 6611 5775 5051 4423 3878 3405 2992 2633 2046 1597 1413 1252 0985 0779 0492 13 7430 6419 5553 4810 4173 3624 3152 2745 2394 1827 1401 1229 1079 0835 0649 0397 28 7284 6232 5339 4581 3936 3387 2919 2519 2176 1631 1229 1069 0930 0708 0541 0320 60 7002 5674 4936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 4936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 6936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 6936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 6936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7503 5537 4564 3769 3118 2584 2145 1784 1486 1037 0728 0611 0514 0365 0261 0135  98 6095 4776 3751 2953 2330 1842 1460 1160 0923 0588 0378 0378 0307 0026 0013 0007 0002  80 3715 2281 1407 0872 0543 0339 0213 0134 0085 0035 0034 0009 0006 0003 0001</td> <td>27 8706 8131 7397 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 1388 358 8535 7894 7307 6768 6274 5820 5403 5019 4665 4039 3506 3075 2843 2630 2255 1938 1443 1084 633 8203 7441 6756 6139 5584 5083 4632 4224 3855 3220 2697 2472 2267 1911 1615 1164 0847 683 8043 7224 6496 5847 5268 4751 4289 3875 3505 2875 2366 2149 1954 1619 1346 0938 0662 74 7885 7014 6246 5568 4970 4440 3971 3555 3186 2567 2076 1869 1685 1372 1122 0757 0517 87 7730 6810 6006 5303 4688 4150 3677 3262 2897 2292 1821 1625 1452 1163 0935 0610 0404 00 7579 6611 5775 5051 4423 3878 3405 2992 2633 2046 1597 1413 1252 0985 0779 0492 0316 13 7430 6419 5553 4810 4173 3624 3152 2745 2394 1827 1401 1229 1079 0835 0649 0397 0247 6441 6560 5134 4363 3714 3166 2703 2311 1578 1456 1078 0929 0802 0600 0451 0320 0193 0708 0441 0320 0193 0708 0518 0500 0549 0337 0247 0500 0500 0500 0500 0500 0500 0500 0451 0320 0193 0500 0500 0500 0500 0500 0500 0500 05</td> <td>27 8706 8131 7397 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 1388 1085 8535 7894 7307 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 1388 1085 43 8368 7664 7026 6446 5919 5439 5002 4604 4241 3606 3075 2843 2630 2255 1938 1443 1084 0822 1085 1085 1085 1085 1085 1085 1085 1085</td>	35         8535         7894         .7307         .6768         .6274         .5820         .5403         .5019         .4665         .4039         .3506           43         8368         .7664         .7026         .6446         .5919         .5439         .5002         .4604         .4241         .3606         .3075           53         8203         .7441         .6756         .6139         .5584         .5083         .4632         .4224         .3855         .3220         .2697           63         8043         .7224         .6496         .5847         .5268         .4751         .4289         .3875         .3505         .2875         .2366           74         .7885         .7014         .6246         .5568         .4970         .4440         .3971         .3555         .3186         .2567         .2076           87         .7730         .6810         .6006         .5303         .4688         .4150         .3677         .3262         .2897         .2292         .1821           13         .7430         .6419         .5553         .4810         .4173         .3624         .3152         .2745         .2394         .1827         .1401      <	35         8535         .7894         .7307         .6768         .6274         .5820         .5403         .5019         .4665         .4039         .3506         .3269           43         8368         .7664         .7026         .6446         .5919         .5439         .5002         .4604         .4241         .3606         .3075         .2843           53         8203         .7441         .6756         .6139         .5584         .5083         .4632         .4224         .3855         .3220         .2697         .2472           83         8043         .7224         .6496         .5847         .5268         .4751         .4289         .3875         .3505         .2875         .2366         .2149           74         .7885         .7014         .6246         .5568         .4970         .4440         .3971         .3555         .3186         .2567         .2076         .1869           87         .7730         .6810         .6006         .5303         .4688         .4150         .3677         .3262         .2897         .2292         .1821         .1625           90         .7579         .6611         .5775         .5051         .4423         .3	35         8535         .7894         .7307         .6768         .6274         .5820         .5403         .5019         .4665         .4039         .3506         .3269         .3050           43         8368         .7664         .7026         .6446         .5919         .5439         .5002         .4604         .4241         .3606         .3075         .2843         .2630           53         8203         .7441         .6756         .6139         .5584         .5083         .4632         .4224         .3855         .3220         .2697         .2472         .2267           83         8043         .7224         .6496         .5847         .5268         .4751         .4289         .3875         .3505         .2875         .2366         .2149         .1954           74         .7885         .7014         .6246         .5568         .4970         .4440         .3971         .3555         .3186         .2567         .2076         .1869         1685           87         .7730         .6810         .6006         .5303         .4688         .4150         .3677         .3262         .2897         .2292         .1821         .1625         .1452	35         8535         7894         ,7307         ,6768         ,6274         ,5820         ,5403         ,5019         ,4665         ,4039         ,3506         ,3269         ,3050         ,2660           43         8368         ,7664         ,7026         ,6446         ,5919         ,5439         ,5002         ,4604         ,4241         ,3606         ,3075         ,2843         ,2630         ,2255           53         8203         ,7441         ,6756         ,6139         ,5584         ,5083         ,4632         ,4224         ,3855         ,3220         ,2697         ,2472         ,2267         ,1911           63         8043         ,7224         ,6496         ,5847         ,5268         ,4751         ,4289         ,3875         ,3505         ,2875         ,2366         ,2149         ,1954         ,1619           74         ,7885         ,7014         ,6246         ,5568         ,4970         ,4440         ,3971         ,3555         ,3186         ,2567         ,2076         ,1869         1685         ,1372           87         ,7730         ,6810         ,6006         ,5303         ,4688         ,4150         ,3677         ,3262         ,2897         <	27 8706 813 1737 8768 8274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 43 8368 7664 7026 6446 5919 5439 5002 4604 4241 3606 3075 2843 2630 2255 1938 53 8203 7441 6756 6139 5584 5083 4632 4224 3855 3220 2697 2472 2267 1911 1615  83 8043 7224 6496 5847 5268 4751 4289 3875 3505 2875 2366 2149 1954 1619 1346 74 7885 7014 6246 5568 4970 4440 3971 3555 3186 2567 2076 1869 1685 1372 1122 87 7730 6810 6006 5303 4688 4150 3677 3262 2897 2292 1821 1625 1452 1163 0935 00 7579 6611 5775 5051 4423 3878 3405 2992 2633 2046 1597 1413 1252 0985 0779 13 7430 6419 5553 4810 4173 3624 3152 2745 2394 1827 1401 1229 1079 0835 0649  28 7284 6232 5339 4581 3936 3387 2919 2519 2176 1631 1229 1069 0930 0708 0541 44 77142 6050 5134 4363 3714 3166 2703 2311 1978 1456 1078 0929 0802 0600 0451 66 7002 3674 4936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0808 0376 77 6864 5703 4746 3357 3305 2765 2317 1945 1635 1161 0829 0703 0556 0431 098 6095 4776 3751 2953 2330 1842 1460 1160 0923 0588 0378 0379 0037 0026 0013 0014 17 4529 3066 2083 1420 0972 0668 0460 0318 0221 0107 0053 0037 0026 0013 0007 180 3715 2281 1407 0872 0543 0339 0213 0134 0085 0035 0014 0009 0000 0000 0001	27 8706 813 1737 17307 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 43 8368 7664 7026 6446 5919 5439 5002 4604 4241 3606 3075 2843 2630 2255 1938 1443 53 8203 7441 6756 6139 5584 5083 4632 4224 3855 3220 2697 2472 2267 1911 1615 1164 83 8043 7224 6496 5847 5268 4751 4289 3875 3505 2875 2366 2149 1954 1619 1346 0938 74 7885 7014 6246 5568 4970 4440 3971 3555 3186 2567 2076 1869 1685 1372 1122 0757 87 7730 6810 6006 5303 4688 4150 3677 3262 2897 2292 1821 1625 1452 1163 0935 0610 00 7579 6611 5775 5051 4423 3878 3405 2992 2633 2046 1597 1413 1252 0985 0779 0492 13 7430 6419 5553 4810 4173 3624 3152 2745 2394 1827 1401 1229 1079 0835 0649 0397 28 7284 6232 5339 4581 3936 3387 2919 2519 2176 1631 1229 1069 0930 0708 0541 0320 60 7002 5674 4936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 4936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 6936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 6936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7002 5674 6936 4155 3503 2959 2502 2120 1799 1300 0946 0808 0691 0508 0376 0258 60 7503 5537 4564 3769 3118 2584 2145 1784 1486 1037 0728 0611 0514 0365 0261 0135  98 6095 4776 3751 2953 2330 1842 1460 1160 0923 0588 0378 0378 0307 0026 0013 0007 0002  80 3715 2281 1407 0872 0543 0339 0213 0134 0085 0035 0034 0009 0006 0003 0001	27 8706 8131 7397 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 1388 358 8535 7894 7307 6768 6274 5820 5403 5019 4665 4039 3506 3075 2843 2630 2255 1938 1443 1084 633 8203 7441 6756 6139 5584 5083 4632 4224 3855 3220 2697 2472 2267 1911 1615 1164 0847 683 8043 7224 6496 5847 5268 4751 4289 3875 3505 2875 2366 2149 1954 1619 1346 0938 0662 74 7885 7014 6246 5568 4970 4440 3971 3555 3186 2567 2076 1869 1685 1372 1122 0757 0517 87 7730 6810 6006 5303 4688 4150 3677 3262 2897 2292 1821 1625 1452 1163 0935 0610 0404 00 7579 6611 5775 5051 4423 3878 3405 2992 2633 2046 1597 1413 1252 0985 0779 0492 0316 13 7430 6419 5553 4810 4173 3624 3152 2745 2394 1827 1401 1229 1079 0835 0649 0397 0247 6441 6560 5134 4363 3714 3166 2703 2311 1578 1456 1078 0929 0802 0600 0451 0320 0193 0708 0441 0320 0193 0708 0518 0500 0549 0337 0247 0500 0500 0500 0500 0500 0500 0500 0451 0320 0193 0500 0500 0500 0500 0500 0500 0500 05	27 8706 8131 7397 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 1388 1085 8535 7894 7307 6768 6274 5820 5403 5019 4665 4039 3506 3269 3050 2660 2326 1789 1388 1085 43 8368 7664 7026 6446 5919 5439 5002 4604 4241 3606 3075 2843 2630 2255 1938 1443 1084 0822 1085 1085 1085 1085 1085 1085 1085 1085

\* The factor is zero to four decimal places

Present Value of an Annuity of Period for n Periods:

$$PVIF_{rt} = \sum_{i=1}^{n} \frac{1}{(1+r)^{i}} = \frac{1}{(1+r)^{i}}$$

payments	1%	2%	3%	4%	5%	S6%	7%	8%	9%	10%	12%	14%	15%	16%	18%	20%	24%	28%	32%
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.8929	0.8772	0.8696	0.8621	0.8475	0.8333	0.8065	0.7813	0.7576
2	1.9704	1.9416	1.9135	1,8861	1.8594	1.8334	1.8080	1.7833	1.7591	1.7355	1.6901	1.6467	1,6257	1.6052	1.5656	1.5278	1.4568	1.3916	1.3315
3	2,9410	2.8839	2.8286	2.7751	27232	2.6730	2,6243	2.5771	2.5313	2.4869	2.4018	2.3216	2.2832	2.2459	2.1743	2.1065	1.9813	1.8984	1.7663
4	3.9020	3,8077	3.7171	3.6299	3.5460	3.4651	3.3872	3.3121	3.2397	3.1699	3.0373	2.9137	2.8550	2.7982	2.6901	2.5887	2.4043	2.2410	2.0957
5	4.8534	4.7135	4,5797	4.4518	4.3295	4.2124	4.1002	3.9927	3.8897	3.7908	3.6048	3.4331	3.3522	3.2743	3.1272	2.9906	2.7454	2.5320	2.3452
6	5,7955	5,6014	5.4172	5.2421	5.0757	4.9173	4.7665	4.6229	4.4859	4.3553	4.1114	3.8887	3.7845	3.6847	3.4976	3.3255	3.0205	2.7594	2.5342
7	6.7282	6.4720	6.2303	6.0021	5.7864	5.5824	5.3893	5,2064	5.0330	4.8684	4.5638	4.2883	4.1604	4.0386	3.8115	3.6046	3.2423	2.9370	2.6775
8 ′	7.6517	7,3255	7.0197	6.7327	6.4632	6.2098	5.9713	5.7466	5.5348	5.3349	4.9676	4.6389	4.4873	4.3436	4.0776	3.8372	3.4212	3.0758	2.7860
9	8,5660	8.1622	7.7861	7.4353	7.1078	6.8017	6.5152	6.2469	5.9952	5.7590	5.3282	4.9464	4.7716	4.6065	4.3030	4.0310	3.5655	3.1842	2.8681
10	9,4713	8.9826	8.5302	8.1109	7.7217	7.3601	7.0236	6.7101	6.4177	6.1446	5.6502	5.2161	5.0188	4.8332	4.4941	4.1925	3.6819	3.2689	2.9304
11	10.3676	9.7868	9.2526	8.7605	8.3064	7.8869	7.4987	7.1390	6.8052			5.4527	5.2337	5.0286	4.6560	4.3271	3.7757	3.3351	2.9776
12	11.2551	10.5753	9.9540	9.3851	8.8633	8.3838	7.9427	7.5361	7.1607	6.8137	6.1944	5.6603	5.4206	5.1971	4.7932	4.4392	3.8514	3.3868	3.0133
13	12.1337	11.3484	10.6350	9,9856	9.3936	8.8527	8.3577	7.9038	7.4869	7.1034	6.4235	5.8424	5.5831	5.3423	4.9095	4.5327	3.9124	3.4272	3.0404
14	13,0037	12,1062	11.2961	10.5631	9.8986	9.2950	8.7455	8.2442	7.7862	7.3667	6.6282	6.0021	5.7245	5.4675	5,0081	4.6106	3.9616	3.4587	3.0609
15	13.8651	12.8493	11.9379	11.1184	10.3797	9.7122	9.1079	8.5595	8.0607	7.6061	6.8109	6.1422	5.8474	5.5755	5.0916	4.6755	4.0013	3.4834	3.0764
16	14.7179	13.5777	12.5611	11.6523	10.8378	10.1059	9.4466	8.8514	8.3126	7.8237	6.9740	6.2651	5.9542	5.6685	5.1624	4.7296	4,0333	3.5026	3.0882
17	15.5623	14.2919	13.1661	12.1657	11.2741	10.4773	9.7632	9.1216	8.5436	8.0216	7.1196	6.3729	6.0472	5.7487	5.2223	4.7746	4.0591	3.5177	3.0971
18	16.3983	14.9920	13.7535	12.6593	11.6896	10.8276	10.0591	9.3719	8.7556	8.2014	7.2497	6.4674	6.1280	5.8178	5.2732	4.8122	4.0799	3.5294	3,1039
19	17.2260	15.6785	14.3238	13.1339	12.0853	11.1581	10.3356	9.6036	8.9501	8.3649	7.3658	6.5504	6.1982	5.8775	5.3162	4.8435	4.0967	3.5386	3.1090
20	18.0456	16.3514	14.8775	13.5903	12.4622	11.4699	10.5940	9,8181	9.1285	8.5136	7.4694	6.6231	6.2593	5.9288	5.3527	4.8696	4,1103	3.5458	3.1129
25	22.0232	19.5235	17,4131	15.6221	14.0939	12.7834	11.6536	10.6748	9.8226	9.0770			6.4641	6.0971	5.4669	4.9476	4.1474	3.5640	3.1220
30					15.3725						8.0552		6.5660	6.1772	5.5168	4.9789	4.1601	3.5693	3.1242
40					17.1591							7.1050	6.6418	6,2335	5.5482	4.9966	4.1659	3.5712	3.1250
50					18.2559							7.1327	6.6605	6.2463	5.5541	4.9995	4.1666	3.5714	3.1250
60	44.9550	34.7609	27.6756	22.6235	18.9293	16,1614	14.0392	12.3766	11.0480	9.9672	8.3240	7.1401	6,6651	6.2402	5.5553	4.9999	4.1667	3.5714	3 1250