# BUNAMFAN CLUSTER EXAMINATION - 2022 

## Kenya Certificate of Secondary Education

## 121/2 MATHEMATICS <br> - Paper 2 <br> June 2022-2½ hours

Name .Adm No......

Class Date.

## INSTRUCTIONS TO CANDIDATES

1. Write your Name, Admission number, Class and School.
2. The paper contains two sections: Section I and II
3. Answer ALL questions in section I and ANY FIVE questions from section II.
4. All working and answers must be written on the question paper in the spaces provided below each question.
5. Marks may be awarded for correct working even if the answer is wrong.
6. Negligent and slovenly work will be penatized.
7. Non-programmable silent electronigealculators and mathematical tables are allowed for use.

FOR EXAMINERS USE ONLY
SECTION 1

| 1 | 2 | 3 | 4 | 5 | 6 | a |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

SECTION II
GRAND TOTAL

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | This paper consists 16 of printed pages. |  |  |  |  |  |  |

Candidates should check the question paper to ensure that all the pages are printed as indicated and no questions are missing.

## SECTION 1 (50marks)

## (Answer all questions in this section)

1. The length and width of a rectangle were measured as 12.4 cm and 5.0 cm respectively. Find to 4 significant figures, the percentage error in calculating the area of the rectangle
2. The co-ordinates of a point $A$ is $(2,8,3)$ and $B$ is $(-4,-8,-5)$. A pgint $P$ divides $A B$ externally in the ratio 7: 3 . Determine the co-ordinates of P
3. Solve for x :

Solve for $x:\left(\log _{3} x\right)^{2}-1 / 2 \log _{8} x=3 / 2$
(3mks)
4. A circle is tangent to the $y$ - axis and intersects the $x$ - axis at $(2,0)$ and $(8,0)$. Obtain the equation of the circle in the form $\mathrm{x}^{2}+\mathrm{y}^{2}+\mathrm{ax}+\mathrm{by}+\mathrm{c}=0$, where $\mathrm{a}, \mathrm{b}$ and c are integers
(4mks)
5. Solve for X in the equation:
$2 \operatorname{Sin}^{2} x-1=\operatorname{Cos}^{2} x+\operatorname{Sin} x$, for $0^{0} \leq x \leq 360^{\circ}$ (3mks)
6. Make P the subject of the formula
7. The figure below represents aforwer garden ABC . A tap T is to be placed inside the triangle such that it is nearer A than B anid angle ATB is greater than $120^{\circ}$. By construction, show the region T where the tap can be gुositioned.
(4mks)

$\qquad$
8. PQRS is a rectangle whose area $170 \mathrm{~cm}^{2}$. The internal rectangle measures $(\mathrm{x}+5) \mathrm{cm}$ by $(\mathrm{x}-2) \mathrm{cm}$.


Determine the area of the shaded part if the thickness of this part is 0.1 x cm
(4mks)
9. Find the length of an arc of a circle whith subtends an angle of 0.8 radians at the center of the circle. The radius of the circle is $15^{\circ} \mathrm{cm}$.
(2mks)
10. A map has a scale of $1: 25000$. On this map a square piece of land is represented by an area of $2 \mathrm{~cm}^{2}$. Calculate the actual area in hectares of the land.
11. A dealer has two types of grades of tea, A and B. Grade A costs shs. 140 per kg while grade B costs shs. 160 per kg. Determine the ratio he should mix A and B so that he makes a $60 \%$ profit when he sells the mixture at shs. 232 per kg.
12. The data below shows marks scored by 8 form four students in Molo disfrict mathematics contest44, 32, 67, 52, 28, 39, 46, 64. Calculate the mean absolute deviation of the data. (3mks)
13. A variable $y$ varies ast the square of $x$ and inversely as the square root of $z$. Find the percentage change in y when x is changed in the ratio $5: 4$ and z reduced by $19 \%$
14. Simplify $\frac{2 \sqrt{2}}{1+\sqrt{2}}-\frac{\sqrt{2}}{1-\sqrt{2}}=a+b \sqrt{c}$ leaving your answer in the form $a+b \sqrt{c}$, where $\mathrm{a}, \mathrm{b}$ and c are rational numbers.
15. When a man is standing at a point $x$, he observes that the angle of eleyation of the top of a flag post is $13^{\circ}$, he walks 120 m towards the flag post and the angle of elevation is $30^{\circ}$. If the eyes of the man are 1.5 m from the ground, find the height of the flagyost.
(4mks)
16. Findthe value of x given that T is a singular matrix.

$$
\mathrm{T}=\left[\begin{array}{cc}
x+1 & 2 \\
4 x & 2 x
\end{array}\right]
$$

## SECTION II 50 marks

## (Answer only five questions in this Section)

17. A tank has two water taps $P$ and $Q$ and another tap R. When empty the tank can be filled by tap $P$ alone in 5 hours or by tap Q in 3 hours. When full the tank can be emptied in 8 hours by tap R.
a) The tank is initially empty. Find how long it would take to fill up the tank
i) If $\operatorname{tap} \mathrm{R}$ is closed and taps P and Q are opened at the same time.
ii) If all the three taps are opened at the same time.Giving your answer to the nearest minute.
b) Assume the tank initially empty and the thee taps are opened as follows;

P at 8:00 am, Q at 9:00 am and B Cat 9:00 am
i) Find the fraction of the tank that would be filled by 10:00 am.
ii) Find the time the tank would be fully filled up. Give your answer to the nearest minute.
(3mks)

18. In the figure below, G is the center of the circle. $\angle \mathrm{DCB}=50^{\circ}, \angle \mathrm{AGB}=63^{\circ}$ and $\angle \mathrm{FEC}=111^{\circ}$

(a)Determine the size of the following angles
i. FAC
ii. BAC
iii. ACB
iv. ACF
v. AFC

(b) DC is a tangent to the circle at C and its length is 6 cm . AD is a straight line and chord AB is 3.1 cm . Determine
(i) The length of BD
(2mks)
(ii) Area of triangle ABC
(3mks)
19. The table below shows the income tax rates in a certain year.

| Annual taxable income in <br> Kenya shillings | Tax rate in \% |
| :--- | :--- |
| $0-144000$ | $0 \%$ |
| $144001-300000$ | 10 |
| $300001-468000$ | 15 |
| $468001-648000$ | 20 |
| $648001-840000$ | 25 |
| Above 840000 | 30 |

During that year Kurenta’s annual gross tax in sixth band was Shs 108000.
(a) Determine Kurenta's annual gross tax.
(3mks)
(b) If he enjoyed annual relief of Shs. 21 000, determine his monthly net tax (P.A.Y.E)(2mks)
(c) Kurenta had a basic salary of Shs X Shs p.a. and enjoyed non-taxable allowances that is equivalent to $45 \%$ of basic salary. Determine Kurenta's gross salary p.m.
(d)The following deductions were also made from Kurenta's salary every month: Co-operative shares 8 000, Co-operative loans 12 000, Pension scheme 4 000, Union dues 2000.

Determine Kurenta's monthly net salary during that year.
20. (a)Complete the table below for the functions $y=-\frac{5}{2}+\frac{9}{2} \cos (2 x)$ and $y=3 \sin \left(\frac{7 x}{3}\right)$ to 1 d.p.for $\mathrm{O}^{0} \leq \mathrm{x} \geq 165^{0}$

| $x$ | 0 | 15 | 30 | 45 | 60 | 75 | 90 | 105 | 120 | 135 | 150 | 165 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y=-\frac{5}{2}+\frac{9}{2} \cos (2 x)$ | 2 | 1.4 |  | -2.5 | -4.8 | -6.4 | -7 | -6.4 |  | -2.5 |  | 1.4 |
| $y=3 \sin \left(\frac{7 x}{3}\right)$ | 0 | 1.7 | 2.8 | 2.9 | 1.9 |  |  | -2.7 | -2.9 | -2.1 |  | 1.3 |

(b)Draw the graphs of $y=-\frac{5}{2}+\frac{9}{2} \cos (2 x)$ and $y=3 \sin \left(\frac{7 x}{3}\right)$ on the same grid.
(use a scale of 1 cm to rep $10^{0}$ on the $x$-axis and 1 cm to rep 1unit on the $y$-axis.)
(5mks)

(c)Use your graph to solve $9 \cos (2 x)-6 \sin \left(\frac{7 x}{3}\right)=5$
(3mks)
21. The figure below shows a cuboid ABCDEFGH with $\mathrm{AB}=8 \mathrm{~cm}, \mathrm{BC}=6 \mathrm{~cm}$ and $\mathrm{CH}=5 \mathrm{~cm}$.


Calculate to $1 \mathrm{~d} . \mathrm{p}$
(a) The length $B E$
(b) The angle between BE and plane ABCD
(d) The acute angle between lines FH and BD
(1mks)
(e) The angle between place AGHD and planes ABCD
(f) Point K and L divides EH and $\mathscr{F G}$ respectively in the ratio 1: 3 . Determine the angle between planes ADKL and BCKL
(2mks)
22. Juice type Q is $60 \%$ tangerine and the rest is water. Juice type P is $30 \%$ water and the rest is pineapple.
(a) Jane mixes 8 litres of Q with 12 litres of P to produce a blend juice B . Find the percentage of water in blend B
(b) Janet makes 8L of a blend juice R that is $36 \%$ water by mixing fuice Q and P . Determine the amount of juice Q and P that she uses.
(c) 5L of B is now mixed with 3L of Q to produce blend W. Find the concentration of tangerine in blend W.

23. In triangle OAB below $\mathbf{O A}=\mathbf{a}, \mathbf{O B}=\mathbf{b}$ point $\mathbf{M}$ lies on $\mathbf{O N}$ such that $\mathbf{O M}: \mathbf{M A}=2: 3$ and point $N$ lies on $\mathbf{O B}$ such that $\mathbf{O N}=\frac{5}{6} \mathbf{O B}$ line $A N$ intersect line MB at X .

(a) Express in terms of $\mathbf{a}$ and $\mathbf{b}$
(i) AN
(1mk)
(ii) BM
(1mk)
b) Given that $A X=k A N$ and $B X=B M$ where $k$ and rare scalars.
i. write down two different expression for OX in terms of $\mathbf{a}, \mathbf{b}, \mathrm{k}$ and r.
ii. Find the vaine of $k$ and $r$.
(4mks)
iii. Determine the ratio in which $x$ divides line MB. (2mks)

24. The probability that it rains on a certain day is 0.8 . If it rains the probability that Onguti comes to school late is 0.7 but otherwise it is 0.4 . If he comes to school late, the probability that he fails an exercise is 0.8 but if he comes early, the probability of failing an exercise is 0.3
(a) Draw a tree diagram to represent this information
(b) Determine
(i) The probability that it rains, he comes to schools early and he fails the exercise (2mks)
(ii) The probability that he passes his exercise
(iii) The probability that he comes to school late
(iv) The probability that he comes to schools late and he passes his exercise

