

Name.....

121/2

Marking Scheme

Mathematics

Paper 2

2 ½ Hours

June 2022

KASSU JET EXAMINATIONS

Kenya Certificate of Secondary Education (K.C.S.E)

INSTRUCTIONS TO CANDIDATES

- Write your name and Admission number in the spaces provided at the top of this page.
- This paper consists of two sections: Section I and Section II.
- Answer ALL questions in section 1 and ONLY FIVE questions from section II
- All answers and workings must be written on the question paper in the spaces provided below each question.
- Show all the steps in your calculation, giving your answer at each stage in the spaces below each question.
- Non – Programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.

FOR EXAMINERS USE ONLY

SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | TOTAL |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|-------|
| | | | | | | | | | | | | | | | | |

SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | TOTAL |
|----|----|----|----|----|----|----|----|-------|
| | | | | | | | | |

GRAND TOTAL

| |
|--|
| |
|--|

SECTION I. Answer all the questions (50 marks)

1. A student spends $\frac{3}{8}$ of his time playing basketball, $\frac{1}{4}$ of the remaining in playing table tennis and $\frac{3}{4}$ of the remaining time playing volleyball. The rest is spent on reading novels. What fraction of the time is spent on reading novels. (3 mks)

| | | |
|--|---|---|
| $\frac{3}{8} \Rightarrow \text{b. ball}$ $\frac{1}{4} \times \frac{5}{8}$ $= \frac{5}{32} \text{ M}_1$ | $\frac{3}{8} + \frac{5}{32}$ $= \frac{17}{32} \text{ M}_1$ <p>Remaining</p> $\frac{15}{32} \text{ M}_2$ | $\frac{3}{4} \times \frac{15}{32} = \frac{45}{128}$ $\frac{17}{32} + \frac{45}{128} = \frac{113}{128}$ $1 - \frac{113}{128}$ $= \frac{15}{128} \text{ A}_1$ |
|--|---|---|

2. Simplify; $\frac{\sqrt{5}-1}{\sqrt{5}+1}$ (3 marks)

| | |
|---|--|
| $\frac{\sqrt{5}-1}{\sqrt{5}+1} \times \frac{\sqrt{5}+1}{\sqrt{5}+1} \text{ M}_1$ <p>Numerator</p> $6-2\sqrt{5} \text{ M}_1$ | <p>Denominator</p> $\frac{5-1}{4}$ $\frac{6-2\sqrt{5}}{4} = \frac{3}{2} - \frac{1}{2}\sqrt{5}$ <p>or</p> $\Rightarrow 1.5 - 0.5\sqrt{5} \text{ A}_1$ |
|---|--|

3. Solve the equation $2 \log 3 + \log(x-2) = 2 \log x$ (3marks)

$$\log \{ 3^2(x-2) \} = \log x^2 \text{ M}_1$$

$$9(x-2) = x^2$$

$$x^2 - 9x + 18 = 0 \text{ M}_1$$

$$(x-6)(x-3) = 0$$

$$x = 6 \text{ A}_1$$

$$x = 3$$

4. The base and perpendicular height of a triangle measured to the nearest millimetre are 15.0 cm and 9.5 cm respectively. Find

(a) The absolute error in calculating the area of the triangle (1 mark)

| Min prod | Actual | Max product |
|----------|--------|-------------|
| 14.95 | 15.0 | 15.05 |
| 9.45 | 9.5 | 9.55 |
| 141.2775 | 142.5 | 143.7275 |

$$A.E = \frac{143.7275 - 141.2775}{2} = 1.225 \text{ A}_1$$

(b) The percentage error in the area, giving the answer to 1 decimal place. (2mks)

$$\frac{1.225}{142.5} \times 100 \text{ M}_1$$

$$= 0.859$$

$$0.9\% \text{ A}_1$$

5. Find the value of θ , given that; $\frac{1}{2} \sin \theta = 0.35$ for $0^\circ \leq \theta \leq 360^\circ$

(3 mks)

$$\sin \theta = 0.70 \text{ M}_1$$

$$\theta = \sin^{-1} 0.70$$

$$\theta = 44.43^\circ \text{ A}_1$$

$$180 - 44.43$$

$$= 135.57 \text{ A}_1$$

6. Make Q the subject of formula $P = \sqrt{\frac{Q^2}{Q^2-1}}$

3marks

$$P^2 = \left(\frac{Q^2}{Q^2-1} \right) \text{ M}_1$$

$$P^2 Q^2 - P^2 = Q^2$$

$$P^2 Q^2 - Q^2 = P^2 \text{ M}_1$$

$$Q^2 (P^2 - 1) = P^2$$

$$Q^2 = \frac{P^2}{P^2 - 1}$$

$$Q = \pm \sqrt{\frac{P^2}{P^2 - 1}} \text{ A}_1$$

7. The coordinates of the end points of a diameter of a circle are $A(2,4)$ and $B(-2,6)$.
Find the equation of the circle in the form $ax^2 + by^2 + cx + dy + e = 0$
(4marks)

Centre
 $\left(\frac{2+(-2)}{2}, \frac{4+6}{2}\right)$

$(0, 5)$ B_1

Radius =
 $\sqrt{(0-2)^2 + (5-4)^2}$

$r = \sqrt{5}$ B_1

$(x-0)^2 + (y-5)^2 = (\sqrt{5})^2$ M_1

$x^2 + y^2 - 10y + 25 = 5$

$x^2 + y^2 - 10y + 20 = 0$ A_1

8. Kimani wants to buy a TV on hire purchase. It has a cash price of Ksh.30,000. He makes a down payment of Ksh.9,000 and 12 monthly instalments of ksh. 2,200 each. Calculate the rate of compound interest charged per month. (Give your answer to 1 dp). (3 mks)

$P = 30,000 - 9,000$
 $= 21,000$

$A = 12 \times 2,200$
 $= 26,400$ M_1

$26,400 = 21,000 \left(1 + \frac{r}{100}\right)^{12}$ M_1

$1.257 = \left(1 + \frac{r}{100}\right)^{12}$

$\sqrt[12]{1.257} = 1.0193$ M_1

$1.0193 = 1 + \frac{r}{100}$

$r = 1.93$

$r = 1.9$ A_1

9. Expand $(3+3x)^6$ in ascending powers of x . Hence use the expansion up to the 3rd term, to find the value of $(3.03)^6$ correct to 2 decimal places. (3mks)

$(3+3x)^6$

$729 + 4356x + 10935x^2 + 14580x^3 + 10935x^4 + 4356x^5 + 729x^6$ M_1

$3+3x = 3.03$

$x = 0.01$ M_1

$729 + 4356x + 10935x^2 \rightarrow 729 + 4356(0.01) + 10935(0.01)^2$

$= 773.6535$ A_1

≈ 773.65 (2 dp) 4

10. The following are ages of students in a class 7,9,8,9,11,12,10,9,8,6,7,10,11,12,6,9,7, and 11.

a). Complete the frequency distribution table below

(1mark)

| | | | | | | | |
|-------------------|----|----|----|---|----|----|----|
| Ages x | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| No of students | 2 | 3 | 2 | 4 | 2 | 3 | 2 |
| $(x - \bar{x})$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| $(x - \bar{x})^2$ | 9 | 4 | 1 | 0 | 1 | 4 | 9 |

$$\bar{x} = \frac{162}{18} = 9$$

b). Calculate the standard deviation of their ages in five years' time. (2mks)

$$V = \frac{\sum d^2}{N}$$

$$= \frac{28}{18} M_1$$

$$= 1.5$$

$$s.d = 1.247 A_1$$

11. Find the possible values of x given that $\begin{pmatrix} x+8 & 8 \\ 6 & x \end{pmatrix}$ is a **singular** matrix.

(3 mks)

$$x^2 + 8x - 48 = 0 \quad M_1$$

$$x^2 + 12x - 4x - 48 = 0 \quad M_1$$

$$x(x+12) - 4(x+12) = 0$$

$$(x+12)(x-4) = 0$$

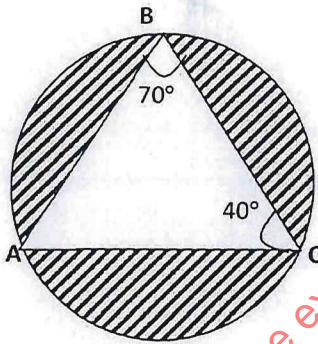
$$\left. \begin{array}{l} x = -12 \\ x = 4 \end{array} \right\} A_1$$

12. Evaluate using the logarithm table;

$$\left(\frac{\log 9.814}{4.283 \times (0.009478)^2} \right)^{-\frac{1}{2}} = \left(\frac{4.283 \times (0.009478)^2}{0.9931} \right)^{\frac{1}{2}} M_1$$

| N O | Log. |
|----------|---|
| 4.283 | 0.6317. $M_1 \rightarrow$ All logs correct. |
| 0.009478 | $\bar{3}.9767$ $\times 2$ |
| | $\bar{4}.5882 M_1$ |
| | $\bar{5}.9534 +$ |
| | $0.6317 +$ |
| | $\bar{4}.5851$ |
| 0.9931 | $\bar{1}.9969 -$ |
| | $\bar{4}.5882$ |
| | $= \bar{2}.2941$ Antilog |
| | $= 0.01969$ A_1 |

13. The figure below is that of a circumcircle of the triangle ABC. The radius of the circle is 5cm. Given that $\angle ABC = 70^\circ$ and $\angle ACB = 40^\circ$. Calculate the area of $\triangle ABC$. (3 mks)



$$BC = AC = a$$

$$\frac{a}{\sin 70^\circ} = 2 \times 5$$

$$a = 10 \times \sin 70^\circ M_1$$

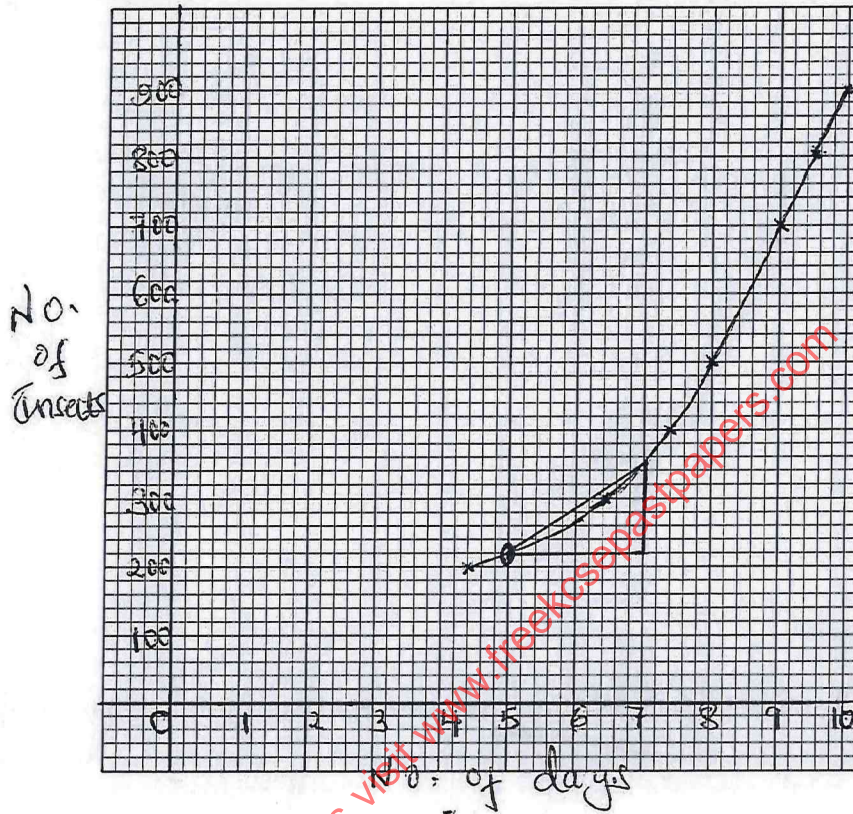
$$A = \frac{1}{2} \times (10 \sin 70^\circ)^2 \times \sin 40^\circ M_1$$

$$A = 28.38 \text{ cm}^2 A_1$$

14. The table below shows the number of insects and corresponding number of days in breeding.

| Number of insects | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 |
|-------------------|-----|-----|-----|-----|-----|-----|-----|-----|
| days | 4.4 | 6.4 | 7.4 | 8.0 | 8.5 | 9.0 | 9.5 | 10 |

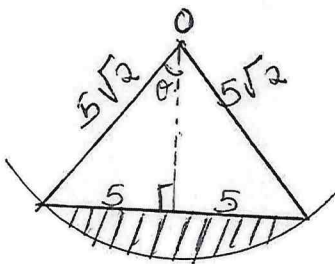
- a). On the grid provided, draw the graph of number of insects against the number of days. (1 mark)



- b). Determine the rate of breeding between 5th and 7th day. (2 marks)

$$\begin{aligned}
 5^{\text{th}} &\rightarrow 220 \\
 7^{\text{th}} &\rightarrow 350 \\
 \frac{350 - 220}{7 - 5} &= 65 \pm 1 \text{ A}_1
 \end{aligned}$$

15. Calculate the area of the minor segment of a circle of radius $5\sqrt{2}\text{cm}$, cut off by a chord of length 10cm .



$$\sin \theta = \frac{5}{5\sqrt{2}}$$

$$\sin \theta = \frac{1}{\sqrt{2}}$$

$$\theta = 45^\circ \text{ M}_1$$

$$\frac{90}{360} \times 3.142 \times (5\sqrt{2})^2 \text{ (3marks) M}_1$$

$$= 39.275$$

$$\frac{1}{2} (5\sqrt{2})^2 \times \sin 90^\circ$$

$$= 25$$

$$39.275 - 25$$

$$= 14.275 \text{ A}_1$$

16. A quantity P varies partly as the cube of Q and partly varies inversely as the square of Q. when Q = 2, P = 108 and when Q = 3, P = 259. Find the value of P when Q = 6.
(3mks)

$$P = Q^3 k + \frac{n}{Q^2}$$

$$108 = 8k + \frac{n}{4}$$

$$259 = 27k + \frac{n}{9}$$

$$432 = 32k + \frac{n}{2}$$

$$2331 = 243k + n$$

$$\frac{2331}{-1899} = \frac{243k + n}{-211k}$$

$$K = 9$$

$$108 = 8(9) + \frac{n}{4}$$

$$n = 144$$

$$P = 6^3(9) + \frac{144}{36}$$

$$P = 1948 \text{ A}_1$$

SECTION II: Answer any 5 questions from this section. (50 marks)

17. Income rates for income earned were charged as shown in the table alongside:

A civil servant earns a monthly salary of Ksh. 27,000. He was also given a house allowance of Ksh. 12,000, transport allowance Ksh. 1,800 and medical allowance Ksh. 2,000. He is entitled to a family relief of Kshs. 1040 per month.

| Income in Ksh. pm | Rate in Ksh. Per Shs. 20 |
|----------------------|-----------------------------|
| 1 - 8400 | 2 |
| 8401 - 18,000 | 3 |
| 18,001 - 30,000 | 4 |
| 30,000 - 36,000 | 5 |
| 36,000 - 48,000 | 6 |
| 48,001 and above | 7 |

Determine:

- a) (i) His taxable income per month in Ksh. (2 mks)

$$27,000 + 12,000 + 1,800 + 2,000$$

$$= 42,800 \text{ A}_1$$

(ii) His net tax.

(6 mks)

| | | | |
|----|------------------------------|--------|---|
| M1 | $\frac{8400}{20} \times 2$ | = 840 | Total 840 + 1440 + 2400 + 1500 + 2040 = 8,220 M1 8220 - 1040 = 7180 A1 |
| | $\frac{9600}{20} \times 3$ | = 1440 | |
| M1 | $\frac{12,000}{20} \times 4$ | = 2400 | |
| | $\frac{6,000}{20} \times 5$ | = 1500 | |
| M1 | $\frac{6,800}{20} \times 6$ | = 2040 | |
| | | | |

b) In addition, the following deductions were made

| | |
|----------------|-------------|
| NHIF | shs. 430 |
| Loan repayment | Kshs. 6500 |
| Bank shares | Kshs. 1000. |

Calculate his net pay per month. (2 mks)

Total deductions
= 7930 + 7180 M1
= 15110

42800 - 15110
= 27,690 A1

18. a). In the figure below, $OY:YA = 1:3$, $AX:XB = 1:2$, $OA = a$ and $OB = b$. n is the point of intersection of BY and OX .

Determine;

i. OX (2 marks)

$$\begin{aligned} \vec{OX} &= \vec{OA} + \vec{AX} \\ &= a + \frac{1}{3} \vec{AB} \end{aligned}$$

$$\vec{AB} = -a + b$$

$$\vec{OX} = a + \frac{1}{3}(-a + b)$$

$$\vec{OX} = \frac{2}{3}a + \frac{1}{3}b$$

ii. BY

$$\vec{BY} = \frac{1}{4}a - b$$

(1 marks)

- b) Given that $BN = mBY$ and $ON = nOX$, express ON in two ways in terms of

a, b, m and n (3 marks)

$$\begin{aligned} \vec{BN} &= m\left(\frac{1}{4}a - b\right) \\ &= \frac{1}{4}ma - mb \end{aligned}$$

$$\begin{aligned} \vec{ON} &= \vec{OB} + \vec{BN} \\ &= b - mb + \frac{1}{4}ma \end{aligned}$$

$$\begin{aligned} \vec{ON} &= n\left(\frac{2}{3}a + \frac{1}{3}b\right) \\ &= \frac{2}{3}na + \frac{1}{3}nb \end{aligned}$$

- c) Find the values of m and n

(4 marks)

$$(1-m)b + \frac{1}{4}ma = \frac{2}{3}na + \frac{1}{3}nb$$

$$\frac{1}{4}m = \frac{2}{3}n$$

$$m = \frac{8}{3}n \quad \text{--- (i)}$$

$$1-m = \frac{1}{3}n$$

$$3-3m = n$$

$$3-3\left(\frac{8}{3}n\right) = n$$

$$3 = 9n$$

$$n = \frac{1}{3}$$

$$m = \frac{8}{3}\left(\frac{1}{3}\right)$$

$$m = \frac{8}{9}$$

19. (a) In a geometrical progression the sum of the second and third term is 12 and the sum of the third and fourth terms is -36. Find the first term and the common ratio.

$$\begin{array}{l}
 ar + ar^2 = 12 \quad M_1 \\
 ar^2 + ar^3 = -36 \\
 \hline
 ar(1+r) = 12 \\
 ar^2(1+r) = -36 \\
 \hline
 \frac{ar^2}{ar} = \frac{-36}{12} \quad M_1
 \end{array}
 \quad \left| \quad
 \begin{array}{l}
 (4\text{marks}) \\
 r = -3. \quad A_1 \\
 \text{From } ar + ar^2 = 12 \\
 -3a + 9a = 12 \\
 a = 2 \quad A_1
 \end{array}$$

- (b) In an arithmetic progression the 12th term is 25 and the 7th term is three times the second term, find;

- i) The first term and the common difference

(4marks)

$$\begin{array}{l}
 M_1 \left\{ \begin{array}{l} a + 11d = 25 \\ (a+d)3 = a + 6d \end{array} \right. \\
 \left. \begin{array}{l} a + 11d = 25 \\ 2a = 3d \\ a = \frac{3}{2}d \quad (i) \end{array} \right. \\
 \frac{3}{2}d + 11d = 25
 \end{array}
 \quad \left| \quad
 \begin{array}{l}
 3d + 22d = 50 \\
 25d = 50 \\
 d = 2 \quad A_1 \\
 a = \frac{3}{2}(2) \\
 a = 3 \quad A_1
 \end{array}$$

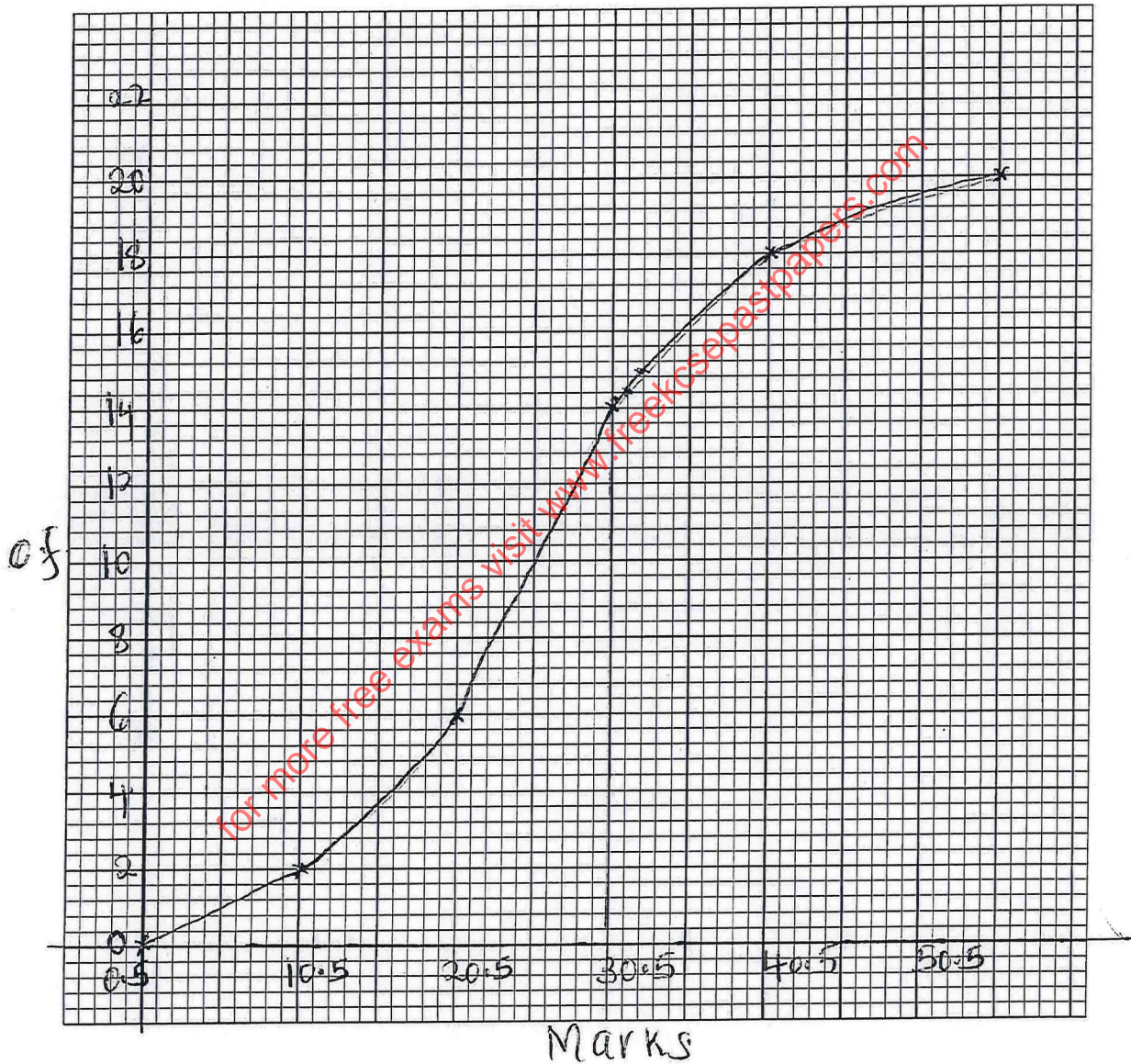
- ii) The sum of the first 10 terms of the arithmetic progression. (2marks)

$$\begin{aligned}
 S_n &= \frac{n}{2}(2a + (n-1)d) \\
 &= \frac{10}{2}(2 \times 3 + (10-1) \times 2) \quad M_1 \\
 &= 120 \quad A_1
 \end{aligned}$$

20. The table below shows the frequency distribution of marks scored by students in a test.

| | | | | | | |
|-----------|------|-------|-------|-------|-------|----|
| | cf | 2 | 6 | 14 | 18 | 20 |
| Marks | 1-10 | 11-20 | 21-30 | 31-40 | 41-50 | |
| Frequency | 2 | 4 | 8 | 4 | 2 | |

a). On the grid provided, draw a cumulative frequency curve for the data. (4 mks)



b). Use your graph to determine;

(i). The pass mark if only 6 students passed the exam. (2 mks)

$$20 - 6 = 14 \quad \checkmark \text{ M1}$$

$$= 30.5 \quad \text{A1}$$

(ii). The upper quartile mark

(1 mk)

$$\frac{3}{4} \times 50$$

$$\frac{3}{4} \times 20$$

$$= 15^{\text{th}} \text{ value}$$

$$= 31.5 \text{ marks}$$

c). Find the percentage change if the upper quartile in b(ii) above was found by calculation. (3 mks)

$$= 30.5 + \left(\frac{15 - 14}{4} \right) 10 \quad \checkmark \text{ M1}$$

$$= 30.5 + 2.5 \quad \checkmark \text{ M1}$$

$$= 33 \quad \checkmark \text{ M1}$$

$$\left(\frac{33 - 31.5}{31.5} \right) \times 100 = 4.76\% \quad \text{A1}$$

21. A gold urn contains 3 red balls and 4 white balls and a silver urn contains 5 red balls and 2 white balls. A die is rolled and if a 6 shows, balls will be selected at random from the gold urn. Otherwise balls are selected from the silver urn.

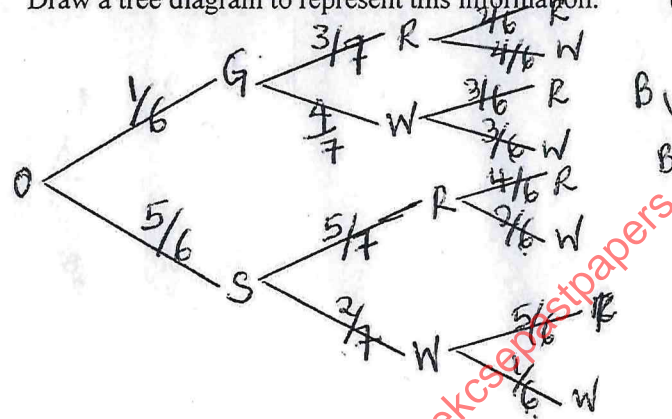
- a. Find the probability of selecting a red ball. (3marks)

$$\frac{1}{6} \times \frac{3}{7} \text{ or } \frac{5}{6} \times \frac{5}{7} \quad M_1$$

$$\left(\frac{1}{14} + \frac{25}{42} \right) M_1 = \frac{2}{3} \quad A_1$$

- b. If two balls are selected at random without replacement,

- i. Draw a tree diagram to represent this information. (2marks)



- ii. Find the probability that two balls are white. (2marks)

$$P(SWW) \text{ or } P(GWW)$$

$$= \left(\frac{5}{6} \times \frac{2}{7} \times \frac{1}{6} \right) + \left(\frac{1}{6} \times \frac{4}{7} \times \frac{3}{6} \right) M_1$$

$$\frac{5}{126} + \frac{1}{21} = \frac{11}{126} \quad A_1$$

- iii. Find the probability that there is at most one white ball from the silver urn. (3marks)

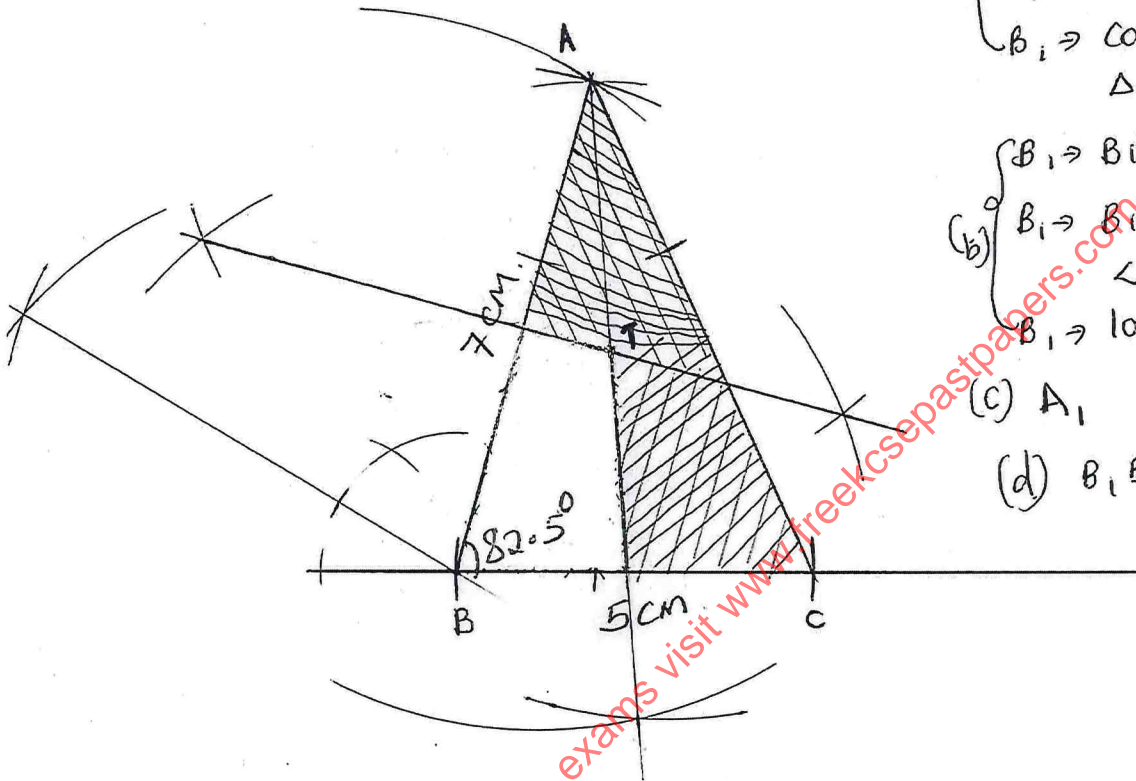
$$P(SRR) \text{ or } P(SWR) \text{ or } P(SRW)$$

$$= \frac{5}{6} \times \frac{5}{7} \times \frac{4}{6} + \frac{5}{6} \times \frac{2}{7} \times \frac{5}{6} + \frac{5}{6} \times \frac{5}{7} \times \frac{2}{6} \quad M_1$$

$$= \frac{25}{63} + \frac{25}{126} + \frac{25}{126} \quad M_1$$

$$= \frac{50}{63} \quad A_1$$

22. a) Using a ruler and a compass only construct triangle ABC where $AB = 7\text{cm}$, Angle $CBA = 82.5^\circ$ and $BC = 5\text{cm}$ (4mks)



(a) $\left\{ \begin{array}{l} B_1 \rightarrow \overline{BC} \\ B_1 \rightarrow \overline{AB} \\ B_1 \rightarrow \angle CBA \\ B_1 \rightarrow \text{complete } \triangle ABC. \end{array} \right.$

(b) $\left\{ \begin{array}{l} B_1 \rightarrow \text{Bisecting } AB \\ B_1 \rightarrow \text{Bisecting } \angle BAC. \\ B_1 \rightarrow \text{locating } I \end{array} \right.$

(c) A_1

(d) $B_1, B_1 \rightarrow$ locating region \Rightarrow shading the unwanted region.

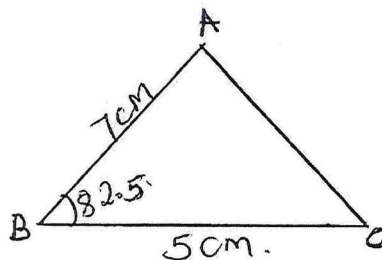
b) i) Locate a point T inside the triangle which is equidistant from points A and B and also equidistant from lines AB and AC (3mks)

ii) Measure TB

(1mk)

$(3.7 \pm 0.1)\text{cm.}$

c) By shading the unwanted region show the area inside the triangle where P lies if it is nearer to point B than to point A and also nearer to the line AB than line AC . (2mks)



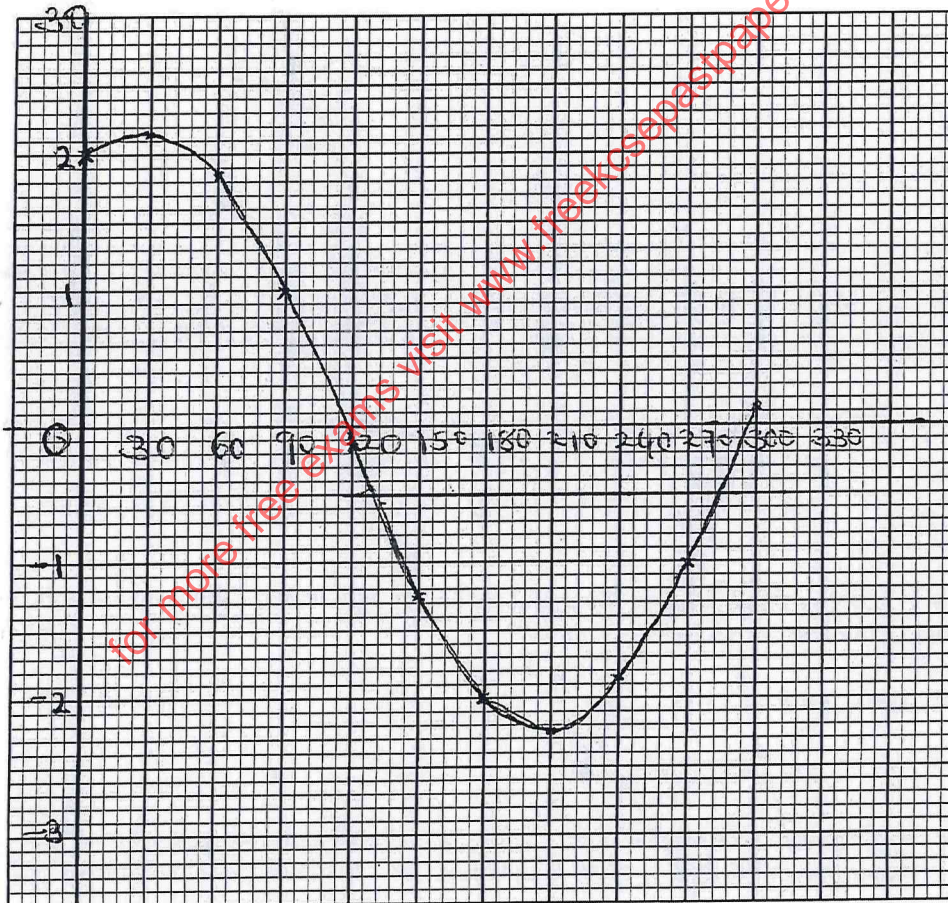
23. (a) Complete the table for $y = \sin x + 2 \cos x$.

(2marks)

| x° | 0 | 30 | 60 | 90 | 120 | 150 | 180 | 210 | 240 | 270 | 300 |
|------------|------|------|------|------|-------|-------|-------|-------|-------|-------|-------|
| $\sin x$ | 0.00 | 0.50 | 0.87 | 1.00 | 0.87 | 0.50 | 0.00 | -0.50 | -0.87 | -1.00 | -0.87 |
| $2 \cos x$ | 2.00 | 1.73 | 1.00 | 0.00 | -1.00 | -1.73 | -2.00 | -1.73 | -1.00 | 0.00 | 1.00 |
| y | 2.00 | 2.23 | 1.87 | 1.00 | -0.13 | -1.23 | -2.00 | -2.23 | -1.87 | -1.00 | 0.13 |

(b) Draw the graph of $y = \sin x + 2 \cos x$.

(3marks)



P₁
C₁
S₁

c). Solve $\sin x + 2 \cos x = 0$ using the graph.

(2marks)

$$114 \pm 2^{\circ}, 294 \pm 2^{\circ}$$

d). Find the range of values of x for which $y < -0.5$

(3marks).

$$132^{\circ} - 280^{\circ}$$

24. A triangle ABC with vertices at $A(1, -1)$, $B(3, -1)$ and $C(1, 3)$ is mapped onto triangle $A^1B^1C^1$ by a transformation whose matrix is $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$. Triangle $A^1B^1C^1$ is then mapped onto $A^{11}B^{11}C^{11}$ with vertices at $A^{11}(2, 2)$, $B^{11}(6, 2)$ and $C^{11}(2, -6)$ by a second transformation.

(i) Find the coordinates of $A^1B^1C^1$. M_1 (3 marks)

$$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 3 & 1 \\ -1 & -1 & 3 \end{pmatrix} = \begin{pmatrix} A^1 & B^1 & C^1 \\ -1 & -3 & -1 \\ -1 & -1 & 3 \end{pmatrix} M_1$$

$$A^1(-1, -1), B^1(-3, -1), C^1(-1, 3)$$

(ii) Find the matrix which maps $A^1B^1C^1$ onto $A^{11}B^{11}C^{11}$. (3 marks)

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} -1 & -3 & -1 \\ -1 & -1 & 3 \end{pmatrix} = \begin{pmatrix} 2 & 6 & 2 \\ 2 & 2 & -6 \end{pmatrix} M_1$$

$$M_1 \left\{ \begin{array}{l} -a - b = 2 \\ -3a - b = 6 \\ a = -2, b = 0 \end{array} \right. \left\{ \begin{array}{l} -c - d = 2 \\ -3c - d = 2 \\ c = 0 \\ d = -2 \end{array} \right. \begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix} A_1$$

(iii) Determine the ratio of the area of triangle $A^1B^1C^1$ to triangle $A^{11}B^{11}C^{11}$. (1 mark)

$$\begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix}$$

$$\text{determinant} = 4 A_1$$

(iv) Find the transformation matrix which maps $A^{11}B^{11}C^{11}$ onto ABC . (3 marks)

$$M = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \quad N = \begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix} \rightarrow N \cdot M$$

$$\begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & -2 \end{pmatrix} M_1$$

$$\text{Inverse of } \begin{pmatrix} 2 & 0 \\ 0 & -2 \end{pmatrix} = \frac{-1}{4} \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} M_1$$

$$\det = -4$$

$$= \begin{pmatrix} \frac{1}{2} & 0 \\ 0 & -\frac{1}{2} \end{pmatrix} A_1$$

Other method allowed.